

Dephasing and heat currents in flux qubits

Janine Splettstößer

Samuele Spilla, Fabian Hassler, and Anna Napoli

Applied Quantum Physics, MC2, Chalmers University of Technology

Institute for Theory of Statistical Physics, RWTH Aachen University

Institute for Quantum Information, RWTH Aachen University

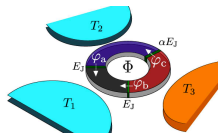
Dipartimento di Fisica e Chimica, Università di Palermo

2nd Quantum Thermodynamics Conference, 19-24 April 2015, UIB
Campus, Mallorca, Spain

Phase-sensitivity of heat currents in superconducting junctions (flux qubits)

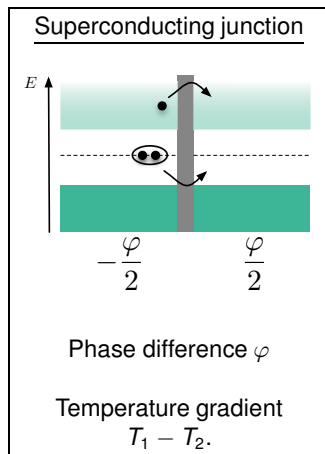
S. Spilla, F. Hassler, and J. Splettstoesser, New J. Phys. **16**, 045020 (2014).

S. Spilla, F. Hassler, A. Napoli, and J. Splettstoesser, arXiv:1503.04489.



- ▶ Introduction
 - ▶ Heat currents in superconducting junctions \Rightarrow Phase-dependence
 - ▶ Superconducting qubits: Delft qubit and fluxonium
- ▶ Sensitivity of heat currents to the qubit state
- ▶ Relate heat current sensitivity to dephasing time
 - ▶ Temperature **gradients**: decoherence due to qubit-state sensitive heat currents (example Delft qubit)
 - ▶ Heat currents as a **phenomenological tool** to study dephasing due to quasiparticle tunneling (example fluxonium)

(Heat) current through a superconducting junction



Josephson current carried by Cooper pairs forming the superconducting condensate:

$$I = I_0 \sin \varphi$$

Heat current carried by quasiparticles:

$$\begin{aligned} \dot{Q}^{\ell} &= \frac{d}{dt} \langle H_{\ell} - \mu_{\ell} N_{\ell} \rangle \\ &= -\frac{i}{\hbar} \langle [H, H_{\ell} - \mu_{\ell} N_{\ell}] \rangle \end{aligned}$$

⇒ Phase dependent through Andreev reflection processes.

(Phase-dependent quasiparticle tunneling.)

- K. Maki and A. Griffin, Phys. Rev. Lett. **15**, 921 (1965).
E. Zhao, T. Löfwander, and J. A. Sauls, Phys. Rev. Lett. **91**, 077003 (2003).
E. Zhao, T. Löfwander, and J. A. Sauls, Phys. Rev. B **69**, 134503 (2004).

Phase-dependent heat current carried by quasiparticles

Weak tunneling - perturbative treatment

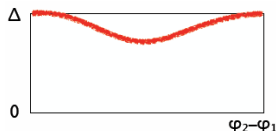
$$\dot{Q}(T_1, T_2) = \frac{2}{e^2 R} \int_{|\Delta_{\max}|}^{\infty} d\omega \omega \frac{\omega^2 - |\Delta(T_1)\Delta(T_2)| \cos(\varphi)}{\sqrt{\omega^2 - |\Delta(T_1)|^2} \sqrt{\omega^2 - |\Delta(T_2)|^2}} [f_1(\omega) - f_2(\omega)]$$

K. Maki and A. Griffin, Phys. Rev. Lett. **15**, 921 (1965).

- Pure quasiparticle contribution + interference part
- Temperature dependence enters via gaps and Fermi functions
- Divergent for small temperature gradients

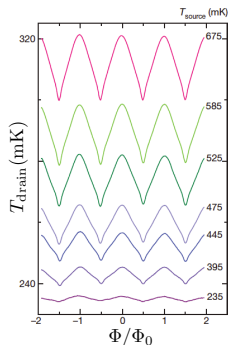
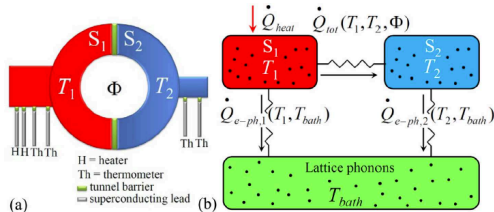
Non-perturbative result, dominated by a weakly bound Andreev state

$$\dot{Q}(T, \delta T) = - \left[\kappa_0 - \kappa_1 \sin^2 \left(\frac{\varphi}{2} \right) \ln \left(\sin^2 \left(\frac{\varphi}{2} \right) \right) + \kappa_2 \sin^2 \left(\frac{\varphi}{2} \right) \right] \delta T$$



E. Zhao, T. Löfwander, and J. A. Sauls, Phys. Rev. Lett. **91**, 077003 (2003).
E. Zhao, T. Löfwander, and J. A. Sauls, Phys. Rev. B **69**, 134503 (2004).

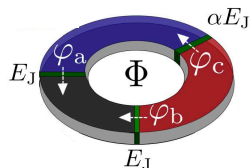
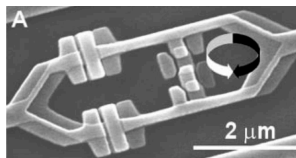
Measurement of phase-dependent heat currents



- ▶ Use the tunability of the superconducting phase in a SQUID.
- ▶ Measurement of temperature differences.
- ⇒ Flux-dependent heat current proves Maki's result.
- ▶ Heat currents are coherently tunable.

F. Giazotto and M. J. Martínez-Pérez, Nature **492**, 401 (2013).
F. Giazotto and M. J. Martínez-Pérez, Appl. Phys. Lett. **101**, 102601 (2012).
M. J. Martínez-Pérez, P. Solinas, F. Giazotto, J. Low Temp. Phys. **175**, 813 (2014).

Flux qubit (Delft design)



I. Chiorescu, *et al.*, Science **299**, 1869 (2003);
J. E. Mooij *et al.*, Science **285**, 1036 (1999).

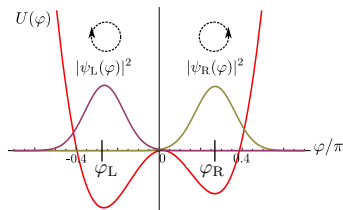
Fluxoid quantization

$$\varphi_a - \varphi_b + \varphi_c = -2\pi \frac{\Phi}{\Phi_0}$$

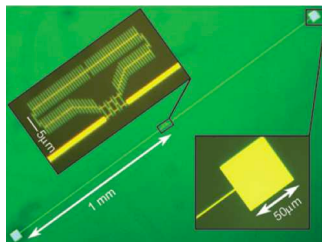
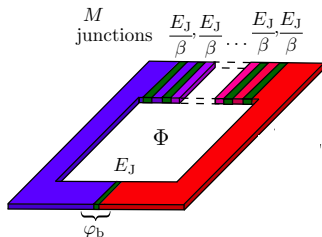
Charging + Josephson energy

$$H = -4E_C \frac{\partial^2}{\partial \varphi^2} + U(\varphi)$$

- ▶ Sweet spot at $f = \frac{\Phi}{\Phi_0} = \frac{1}{2}$: States are degenerate and placed at $\pm\varphi^*$.
- ▶ Small changes in the flux lead to shifts of the minima: $\delta\varphi \propto \delta f$
- ▶ Approximate well-localized states $|\psi_L\rangle$ and $|\psi_R\rangle$ by oscillator states.



Improving the performance: fluxonium



Effective fluxonium Hamiltonian

$$H = -4E_C \frac{\partial^2}{\partial \varphi^2} + \frac{1}{2} E_L \varphi^2 - E_J \cos(\varphi + 2\pi f)$$

with fluxoid quantization $\varphi = M\varphi_L = -\varphi_b - 2\pi f$

and effective superinductance

$$E_L = \frac{E_J}{\beta M} = \frac{(\Phi_0/2\pi)^2}{L_{\text{eff}}} \ll E_J$$

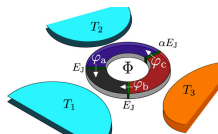
V. E. Manucharyan, *et al.*, *Science* **326**, 113 (2009).

U. Vool, *et al.*, *Phys. Rev. Lett.* **113**, 247001 (2014).

Phase-sensitivity of heat currents in superconducting junctions (flux qubits)

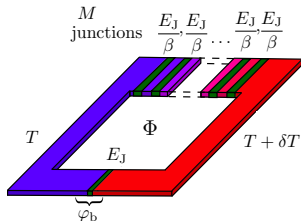
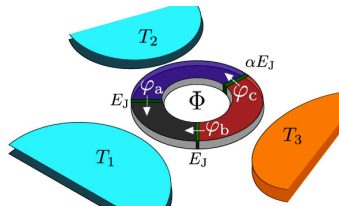
S. Spilla, F. Hassler, and J. Splettstoesser, New J. Phys. **16**, 045020 (2014).

S. Spilla, F. Hassler, A. Napoli, and J. Splettstoesser, arXiv:1503.04489.



- ▶ Introduction
 - ▶ Heat currents in superconducting junctions \Rightarrow Phase-dependence
 - ▶ Superconducting qubits: Delft qubit and fluxonium
- ▶ Sensitivity of heat currents to the qubit state
- ▶ Relate heat current sensitivity to dephasing time
 - ▶ Temperature **gradients**: decoherence due to qubit-state sensitive heat currents (example Delft qubit)
 - ▶ Heat currents as a **phenomenological tool** to study dephasing due to quasiparticle tunneling (example fluxonium)

Qubit arms at different temperatures



Different "quasiparticle baths"

- ▶ Quasiparticle coherence length \ll arm length.

Different temperatures

- ▶ Heating due to operation.
- ▶ Model for non-equilibrium distribution of quasiparticles.

Heat current into different arms:

$$\dot{Q}^{\ell} = \frac{i}{\hbar} \langle [H, H_{\ell} - \mu_{\ell} N_{\ell}] \rangle = \dot{Q}_{\text{qp}} - \dot{Q}_{\text{int}}(\Delta\varphi)$$

Sensitivity of the heat currents to the qubit state

Expectation value of the heat currents in the two qubit states:

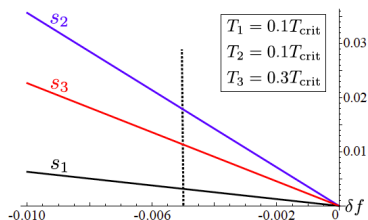
$$\begin{aligned}\dot{Q}_{L/R}^{\ell} &= \langle \psi_{L/R} | \dot{Q}_{\text{qp}}^{\ell} + \dot{Q}_{\text{int}}^{\ell}(\varphi) | \psi_{L/R} \rangle \\ &\propto \dot{Q}_{\text{qp}}^{\ell} + \dot{Q}_{\text{int}}^{\ell}(\varphi_{L/R})\end{aligned}$$

- Microscopic details of the junctions in \dot{Q} , qubit properties in $|\psi_{L/R}\rangle$.

Sensitivity of the heat current detected in "reservoir" ℓ

$$s_{\ell} = \frac{\dot{Q}_{\text{R}}^{\ell} - \dot{Q}_{\text{L}}^{\ell}}{\dot{Q}_{\text{R}}^{\ell} + \dot{Q}_{\text{L}}^{\ell}}$$

For the Delft qubit:



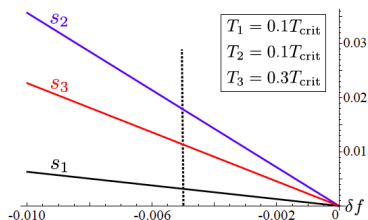
Sensitivity of the heat currents to the qubit state

- ▶ Heat currents **are indeed** sensitive to the qubit state!
- ▶ Approximately linear dependence of s_ℓ on the flux δf .
- ▶ No sensitivity at the sweet spot (at $f = 1/2$ qubit states are degenerate and have $\varphi_{R/L} = \pm\varphi^*$).
- ▶ What is the impact on / relation to the phase coherence of the qubit?

Sensitivity of the heat current detected in "reservoir" ℓ

$$s_\ell = \frac{\dot{Q}_R^\ell - \dot{Q}_L^\ell}{\dot{Q}_R^\ell + \dot{Q}_L^\ell}$$

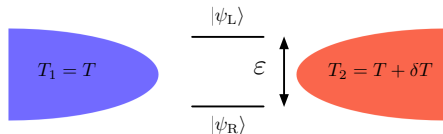
For the Delft qubit:



Toy model for the qubit in contact with quasiparticle baths

State/Phase-dependent coupling takes account for heat current sensitivity!

$$H_{\text{toy}} = -\frac{\varepsilon}{2}\tau^3 - \frac{W}{2}\tau^1 + \sum_{l=1,3} \sum_{k,\sigma} (\varepsilon_{l,k} - \mu_l) a_{l,k\sigma}^\dagger a_{l,k\sigma} + \sum_{k,q,\sigma} \left[a_{1,k\sigma}^\dagger a_{3,q\sigma} (V_0\tau^0 + V_3\tau^3) + \text{H.c.} \right].$$



Reproduce the macroscopic thermal current with:

$$\dot{Q}_{L/R}^{\text{toy}} = \frac{\pi}{\hbar} \int_{-\infty}^{\infty} d\omega \omega (|V_0|^2 \pm |V_3|^2) N_1(\omega) N_2(\omega) [f_1(\omega) - f_2(\omega)]$$

\Rightarrow **Extract $V_0(\varphi_L, \varphi_R)$ and $V_3(\varphi_L, \varphi_R)$!**

Time-evolution of the qubit-state pseudo-spin

Qubit reduced density matrix:

$$\mathbf{S} = \begin{pmatrix} \rho_{LR} + \rho_{RL} \\ i(\rho_{LR} - \rho_{RL}) \\ \rho_{LL} - \rho_{RR} \end{pmatrix}$$

Pauli rate equation:

$$\dot{\mathbf{S}}(t) = \mathbf{S}(t) \times \begin{pmatrix} (w \approx 0) \\ 0 \\ \epsilon \end{pmatrix} - \frac{1}{\tau_\phi} \begin{pmatrix} S_1(t) \\ S_2(t) \\ 0 \end{pmatrix}$$

The phase-sensitive heat current constitutes a measurement process!

$$\begin{aligned} \rho_{LL}(t) &\approx \rho_{LL}(0) & \rho_{RR}(t) &\approx \rho_{RR}(0) \\ \rho_{LR}(t) &\approx \rho_{LR}(0)e^{-i\epsilon t}e^{-t/\tau_\phi} & \rho_{RL}(t) &\approx \rho_{RL}(0)e^{+i\epsilon t}e^{-t/\tau_\phi} \end{aligned}$$

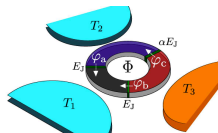
With the dephasing time τ_ϕ

- ▶ Temperature **gradients** leading to heat currents cause decoherence.
- ▶ With the study of heat conductances we are able to capture (a part of) the dephasing mechanism due to quasiparticle tunneling.

Phase-sensitivity of heat currents in superconducting junctions (flux qubits)

S. Spilla, F. Hassler, and J. Splettstoesser, New J. Phys. **16**, 045020 (2014).

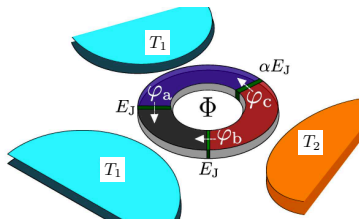
S. Spilla, F. Hassler, A. Napoli, and J. Splettstoesser, arXiv:1503.04489.



- ▶ Introduction
 - ▶ Heat currents in superconducting junctions \Rightarrow Phase-dependence
 - ▶ Superconducting qubits: Delft qubit and fluxonium
- ▶ Sensitivity of heat currents to the qubit state
- ▶ Relate heat current sensitivity to dephasing time
 - ▶ Temperature **gradients**: decoherence due to qubit-state sensitive heat currents (example Delft qubit)
 - ▶ Heat currents as a **phenomenological tool** to study dephasing due to quasiparticle tunneling (example fluxonium)

Dephasing of the Delft qubit due to a temperature gradient

- Delft qubit with two different temperatures $T_1 \neq T_2$.
- Large temperature gradient, $\Delta(T_1) \neq \Delta(T_2)$



$$\frac{1}{\tau_\phi} = \frac{4\pi |V_3|^2 N_1^0 N_2^0}{\hbar} \int_{|\Delta|}^{\infty} d\omega \omega^2 \frac{[1 - f_1(\omega)]f_2(\omega) + [1 - f_2(\omega)]f_1(\omega)}{\sqrt{\omega^2 - |\Delta(T_1)|^2} \sqrt{\omega^2 - |\Delta(T_2)|^2}}$$

- ▶ Zero dephasing for vanishing phase-sensitivity, $V_3 \approx 0$.
- ▶ No dephasing at the sweet spot, where $s = 0$.
- ▶ Compare dephasing time to response to temperature gradient

$$d = \frac{\tau_\phi (\dot{Q}_L - \dot{Q}_R)}{|\Delta_{\max}|}$$

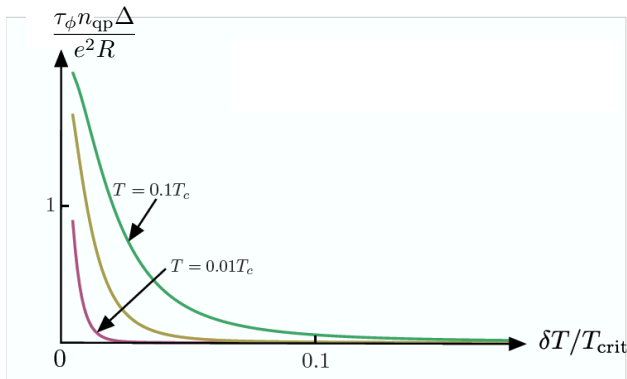
Dephasing times of the Delft qubit

$$d = \frac{\tau_\phi (\dot{Q}_L - \dot{Q}_R)}{|\Delta_{\max}|}$$

Independent of microscopic details of the device!

For large δT , we have $d \approx 1$

Qubit dephases after the time τ_ϕ , which it takes to transfer Δ by the heat current difference!



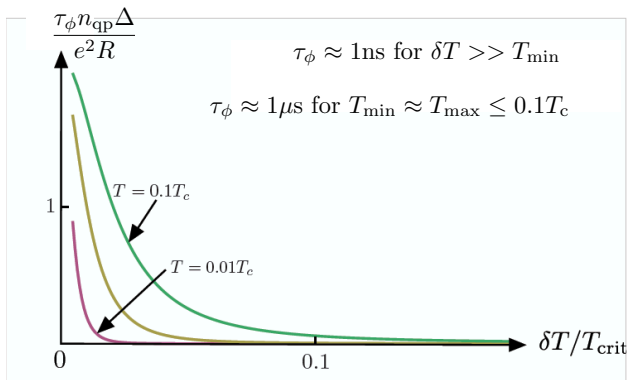
Dephasing times of the Delft qubit

$$d = \frac{\tau_\phi (\dot{Q}_L - \dot{Q}_R)}{|\Delta_{\max}|}$$

Independent of microscopic details of the device!

For large δT , we have $d \approx 1$

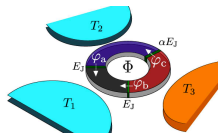
Qubit dephases after the time τ_ϕ , which it takes to transfer Δ by the heat current difference!



Phase-sensitivity of heat currents in superconducting junctions (flux qubits)

S. Spilla, F. Hassler, and J. Splettstoesser, New J. Phys. **16**, 045020 (2014).

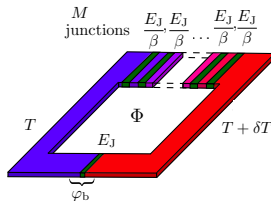
S. Spilla, F. Hassler, A. Napoli, and J. Splettstoesser, arXiv:1503.04489.



- ▶ Introduction
 - ▶ Heat currents in superconducting junctions \Rightarrow Phase-dependence
 - ▶ Superconducting qubits: Delft qubit and fluxonium
- ▶ Sensitivity of heat currents to the qubit state
- ▶ Relate heat current sensitivity to dephasing time
 - ▶ Temperature **gradients**: decoherence due to qubit-state sensitive heat currents (example Delft qubit)
 - ▶ Heat currents as a **phenomenological tool** to study dephasing due to quasiparticle tunneling (example fluxonium)

Dephasing of Fluxonium due to quasiparticles

- ▶ Small accidental temperature gradients – linear response.
- ▶ Heat **conductance** determines the dephasing.
- ▶ Heat conductance contains information about **quasiparticle occupation** and **phase-dependent quasiparticle tunneling**.



- ▶ **Phenomenological approach to dephasing!**

G. Catelani, J. Koch, L. Frunzio, R. J. Schoelkopf, M. H. Devoret and L. I. Glazman, Phys. Rev. Lett. **106**, 077002 (2011);
G. Catelani, S. E. Nigg, S. M. Girvin, R. J. Schoelkopf and L. I. Glazman, Phys. Rev. B **86**, 184514 (2012);
J. Leppäkangas and M. Marthaler, Phys. Rev. B **85**, 144503 (2012);
S. Zanker and M. Marthaler, arXiv:1410.8715.

- ▶ Direct access to the **phase-dependent weak bound state**, dominant at small $T, \delta T$.

Response to small temperature gradients – linear response

$$\dot{Q}(\varphi, T, \delta T) = - \left(\kappa_0 - \kappa_1 \sin^2 \frac{\varphi}{2} \ln \left(\sin^2 \frac{\varphi}{2} \right) + \kappa_2 \sin^2 \frac{\varphi}{2} \right) \delta T$$

E. Zhao, T. Löfwander, and J. A. Sauls, Phys. Rev. Lett. **91**, 077003 (2003).
E. Zhao, T. Löfwander and J. A. Sauls, Phys. Rev. B **69**, 134503 (2004).

Dependence on the specific realization of the superinductance

Role of the superinductance for the dephasing? ($E_L = E_J/\beta M$)

Total heat current into one "reservoir":

$$\dot{Q} = \dot{Q}(-\varphi_b, T, \delta T) + \dot{Q}(\varphi_M, T_M, \delta T/M),$$

Sensitivity does not depend on M or β separately:

- ▶ Only second part of \dot{Q} can depend on M or β .
- ▶ $\varphi_M = -(\varphi_b + 2\pi f)/M$ is very small \Rightarrow only κ_0^M contributes.
- ▶ κ_0^M is independent of the qubit state.
- ▶ Contribution to $s = \frac{\dot{Q}_L - \dot{Q}_R}{\dot{Q}_L + \dot{Q}_R}$:
 $\kappa_0^M \delta T/M + \kappa_0^b \delta T$ is independent of M or β and only depends on E_L .

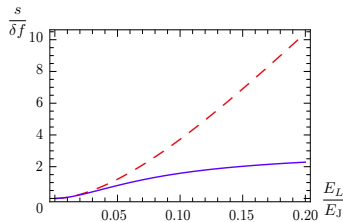
Response to small temperature gradients – linear response

$$\dot{Q}(\varphi, T, \delta T) = - \left(\kappa_0 - \kappa_1 \sin^2 \frac{\varphi}{2} \ln \left(\sin^2 \frac{\varphi}{2} \right) + \kappa_2 \sin^2 \frac{\varphi}{2} \right) \delta T$$

Sensitivity/Dephasing in the fluxonium limit $E_L \ll E_J$

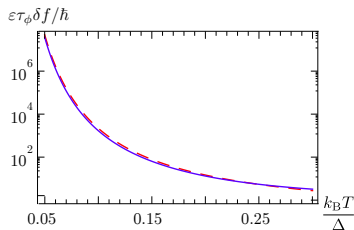
Sensitivity suppressed with E_L/E_J

$$s \approx 2 \frac{\kappa_1}{\kappa_0} \left(\pi \frac{E_L}{E_J} \right)^2 \left| \ln \left(\frac{\pi E_L}{2 E_J} \right) \right| \delta f$$



Allows for large number of operations with $\tau_\phi \propto s^{-1}$.

for $k_B T \leq 0.15\Delta$, more than 10^4 operations.



Response to small temperature gradients – linear response

$$\dot{Q}(\varphi, T, \delta T) = - \left(\kappa_0 - \kappa_1 \sin^2 \frac{\varphi}{2} \ln \left(\sin^2 \frac{\varphi}{2} \right) + \kappa_2 \sin^2 \frac{\varphi}{2} \right) \delta T$$

E. Zhao, T. Löfwander, and J. A. Sauls, Phys. Rev. Lett. **91**, 077003 (2003).

E. Zhao, T. Löfwander and J. A. Sauls, Phys. Rev. B **69**, 134503 (2004).

Conclusions

- ▶ Heat currents through superconducting junctions are phase-dependent.
- ▶ Heat currents in superconducting qubits are **sensitive to the qubit state**.
- ▶ **Temperature gradients** lead to dephasing in flux qubits due to quasiparticles.
- ▶ Dephasing times can become of the order of the actual, known limitations (Delft qubit).
- ▶ Study of the heat conductance for vanishing δT is a **powerful and insightful phenomenological approach** to dephasing due to quasiparticle tunneling.
- ▶ Fluxonium is well protected against this mechanism due to the superinductance!

S. Spilla, F. Hassler, and J. Splettstoesser, New J. Phys. **16**, 045020 (2014).

S. Spilla, F. Hassler, A. Napoli, and J. Splettstoesser, arXiv:1503.04489.