

Polarization Encoding through Vectorial Chaos Synchronization in VCSELs

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Motivation

A VCSEL with the active region surrounded by a saturable absorber can display *vectorial chaos*

The study of vectorial chaos and its synchronisation properties is useful to

- widen the dynamical systems knowledge
- study new cryptographic and encoding schemes
- enhance the transmission capacity in view of cryptographic applications

OUTLINE

- Vectorial chaos: characterisation

- Synchronisation

A continuous control synchronisation (CCS) required to achieve high quality synchronisation

- Encoding:

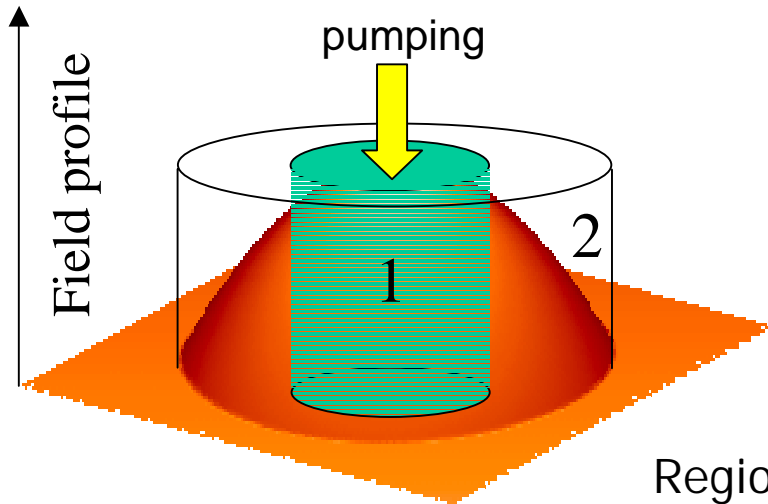
_____ a) CSK: Double-contact VCSEL simple modulation technique and lower P(E) at the receiver

-> talk Alessandro last year

_____ b) polarisation message encoding: bit rate not limited by relaxation oscillation freq.

- Conclusions

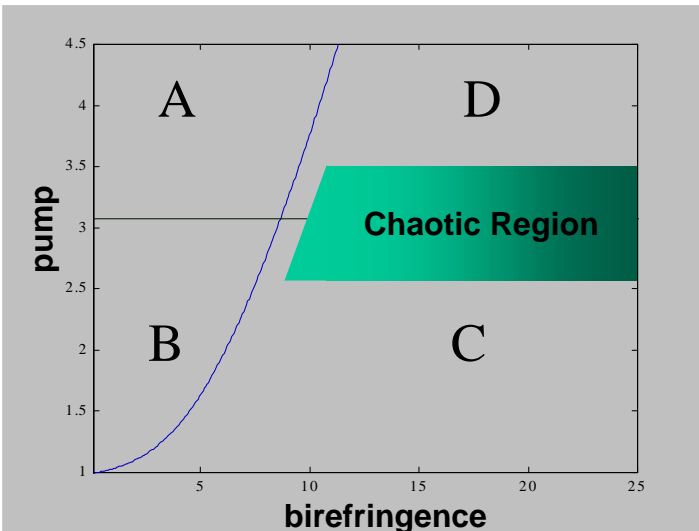
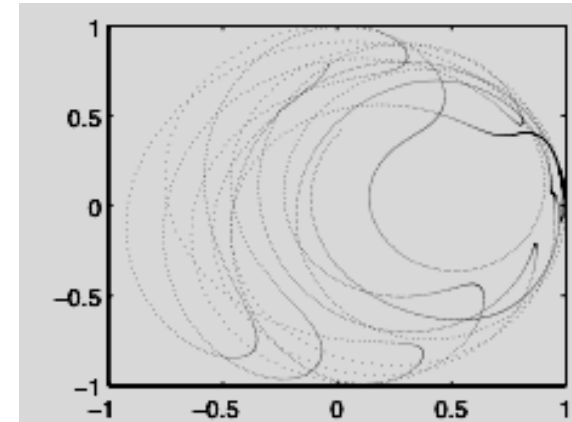
Characterising Vectorial Chaos



VCSEL with saturable absorber,
described by the SFM+ Yamada approach

A. Scirè et al., *Opt.Lett.* **27**, 391 (2002).

Region of the phase space:
chaos.

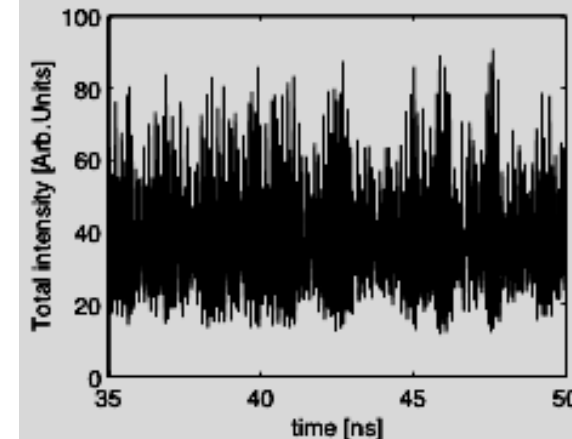


A: stable y-LP

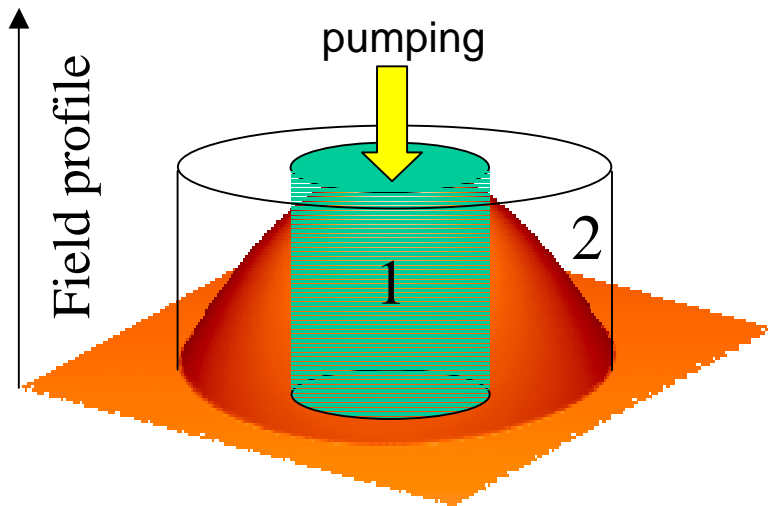
B: pulsations in one
polarization

C: coupled pulsations

D: polarization
pulsations



Characterising Vectorial Chaos



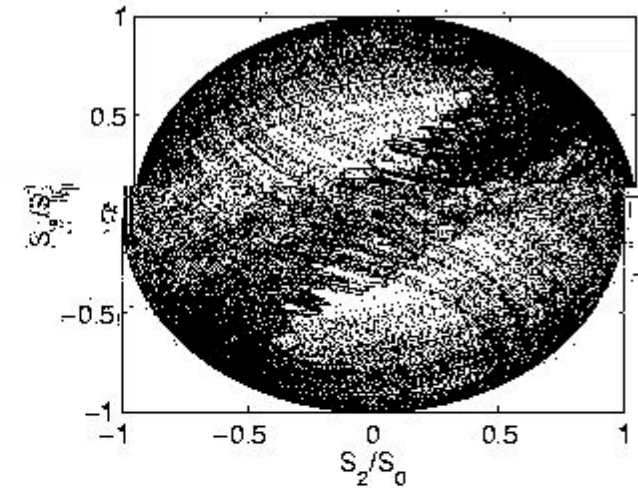
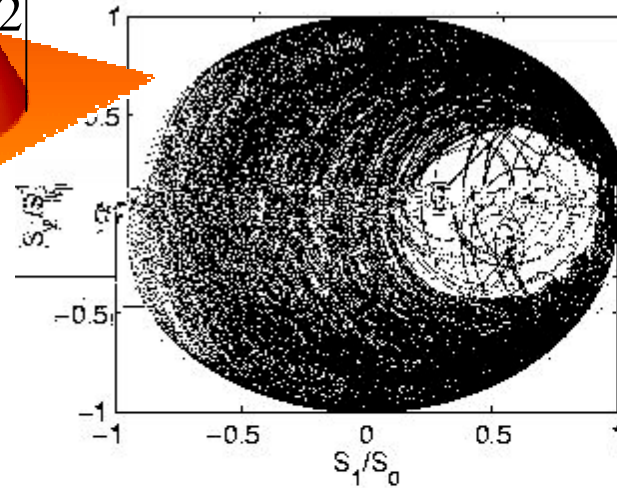
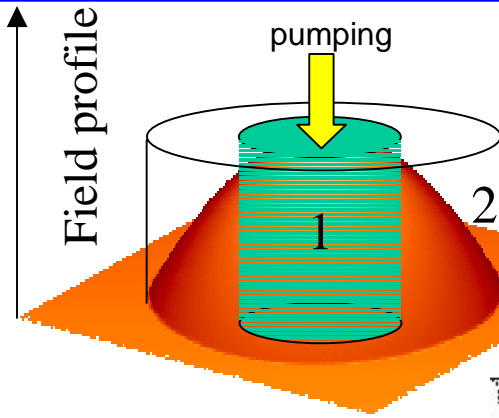
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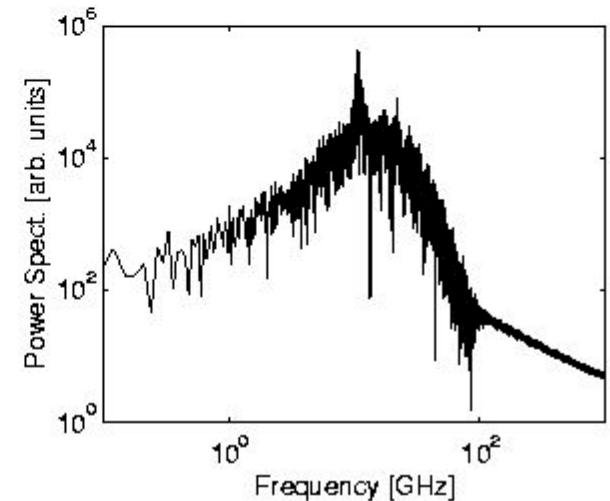
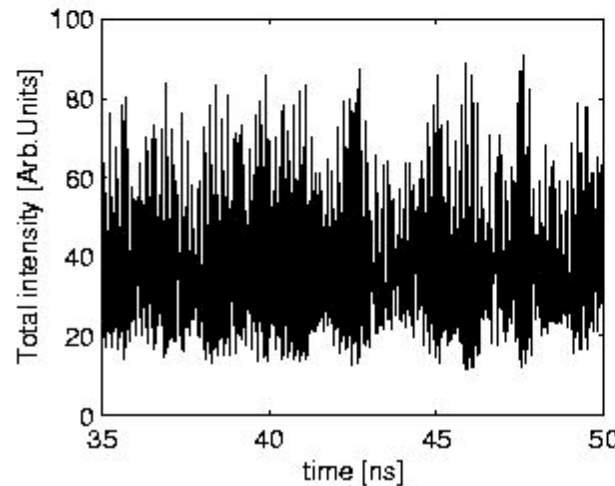
$$\dot{F}_{\pm} = \frac{1}{2}(1 + i\alpha) [D_1 + D_2 \pm d_1 \pm d_2 - 1] F_{\pm} - (\varepsilon_a + i\varepsilon_p) F_{\mp},$$

$$\dot{d}_{1,2} = -\gamma_{s1,2} d_{1,2} - \gamma_{1,2} [(D_{1,2} + d_{1,2}) |F_+|^2 - (D_{1,2} - d_{1,2}) |F_-|^2 - c_{21,12} d_{2,1}],$$

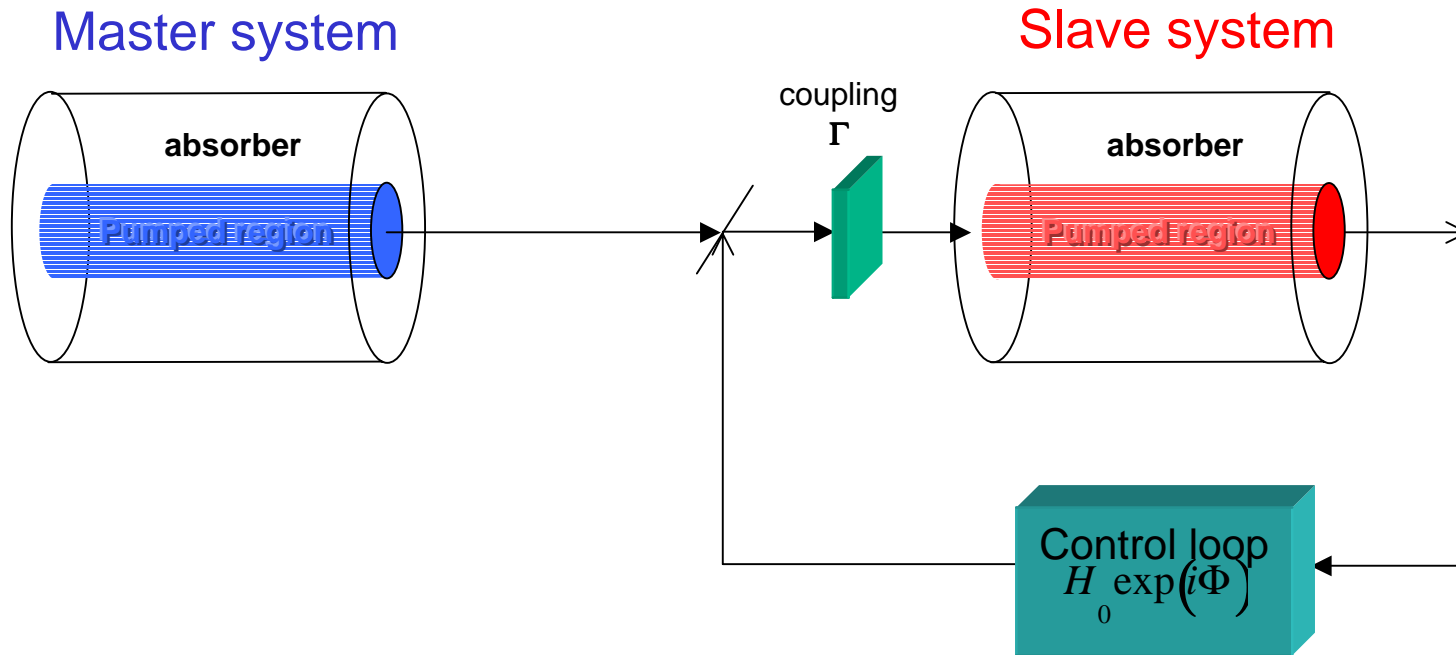
Characterising Vectorial Chaos



2 positive Lyapounov exponents:
total intensity
& pol. instab.)



Coupled system



$$\dot{F}_{\pm}^M = f_{\pm}(D_{1,2}^M, d_{1,2}^M)F_{\pm}^M + (\gamma_a + i\gamma_p)F_{\mp}^M + \xi_{\pm}^M(t)$$

$$\dot{F}_{\pm}^S = f_{\pm}(D_{1,2}^S, d_{1,2}^S)F_{\pm}^S + (\gamma_a + i\gamma_p)F_{\mp}^S + \xi_{\pm}^S(t) + \Gamma(F_{\pm}^M)$$

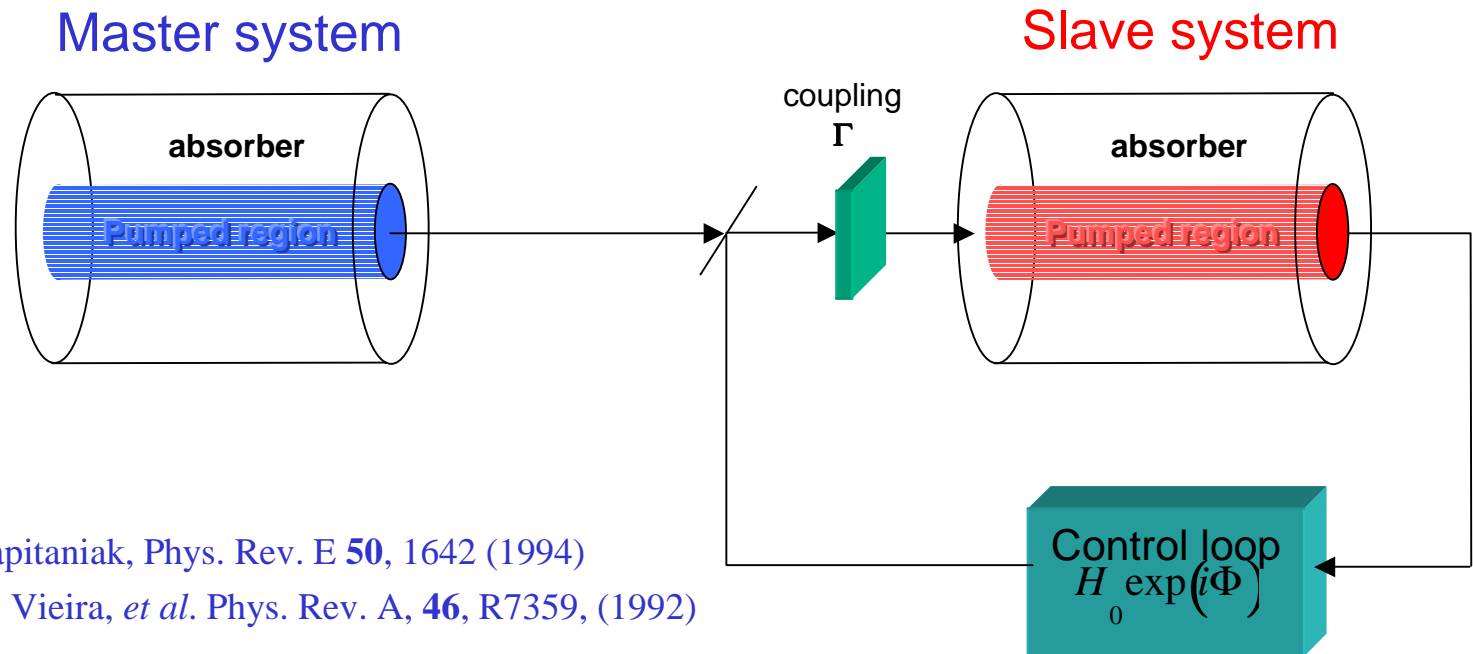
direct coupling: no robust synchronisation

Continuous Control Synchronisation Scheme

=> A Continuous Control of the Synchronisation is required.

The optimum phase condition is $\phi = \pi$ and $H_0 = 1$ [1]

- Phase condition introduces a dissipative term in the Slave system [2]
- The coupling Γ governs the transition from unsynchr. to synchronised behaviour.

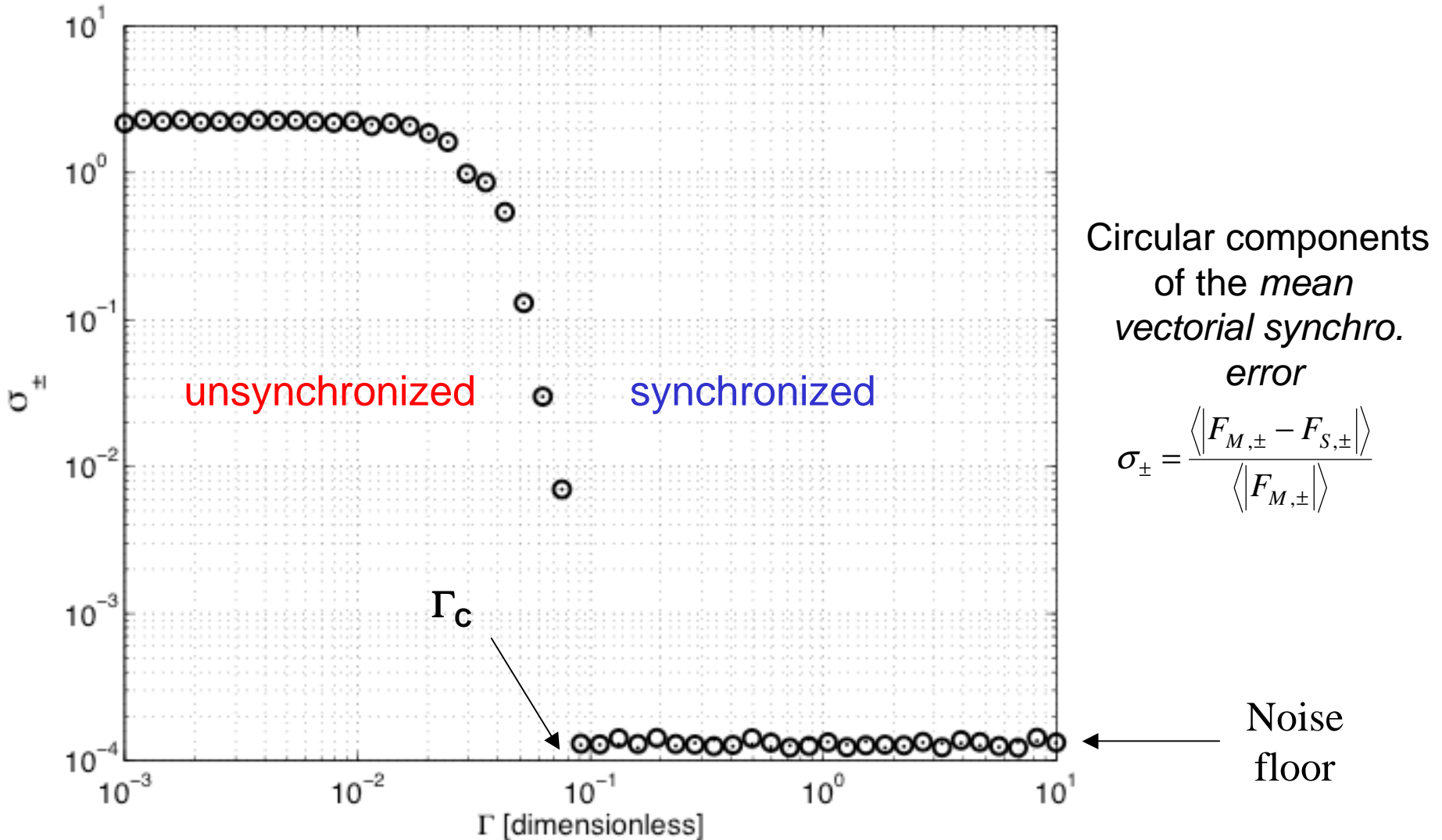


[1] T. Kapitaniak, Phys. Rev. E **50**, 1642 (1994)

[2] M. S. Vieira, *et al.* Phys. Rev. A, **46**, R7359, (1992)

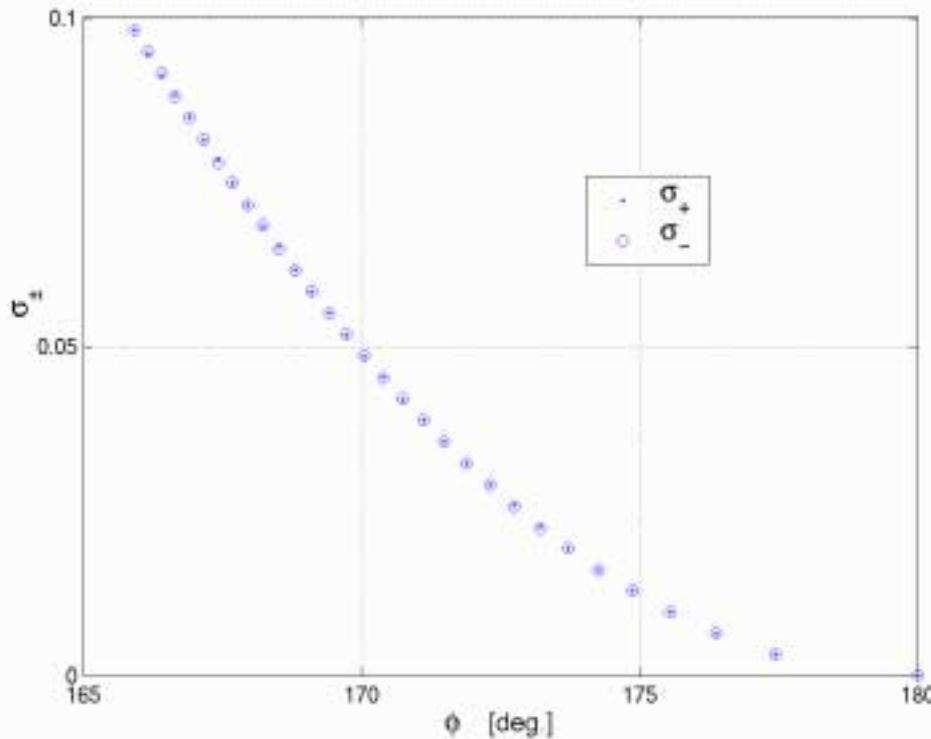
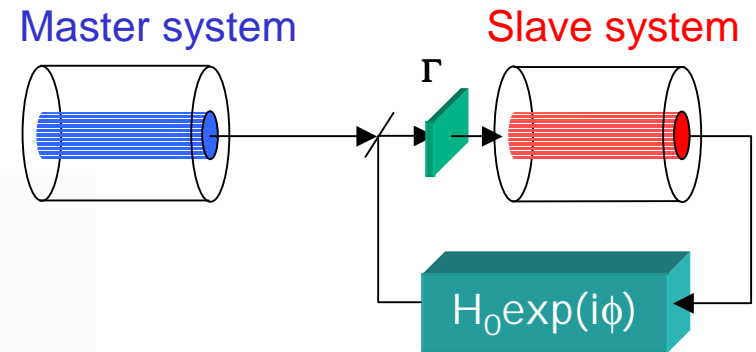
Synchronisation properties

Increasing the coupling Γ , a transition to a synchronized state in both circular components takes place at $\Gamma = \Gamma_c$



Control Loop Phase Mismatch

A phase mismatch with respect to the optimum condition lowers the synchronization quality.



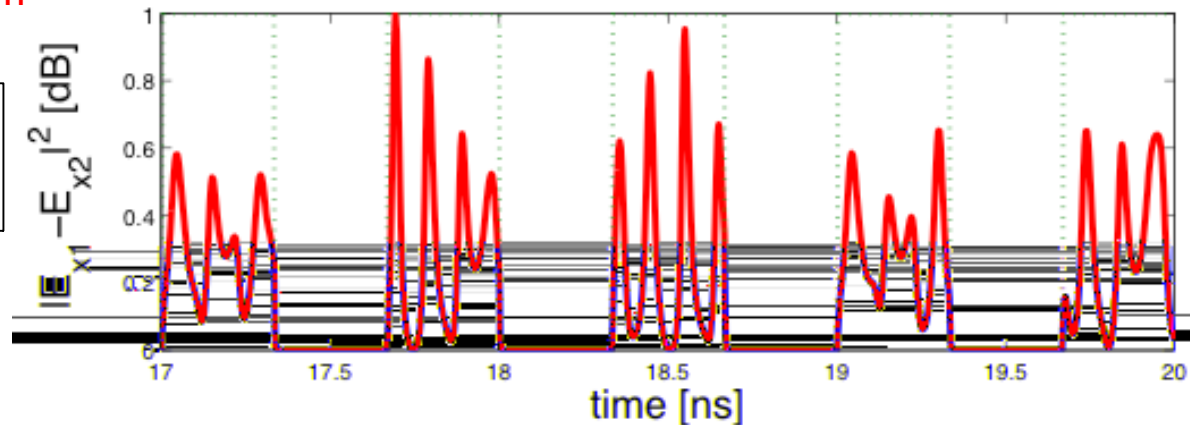
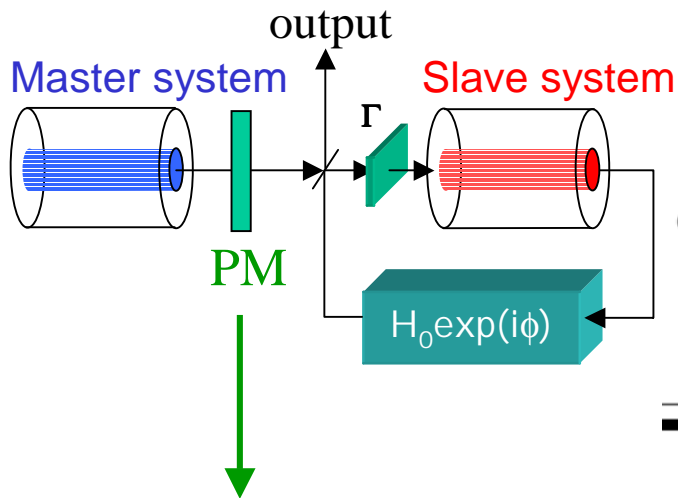
In practice, the accuracy level required to fulfil

$$\phi = \pi$$

is of the same order of magnitude as in coherent detection or interferometry.

Polarisation message encoding

Van Wiggeren & Roy, PRL88, 097903, 2002



Polarisation message encoding
Off-state (bit 0): no phase shift
On-state (bit 1): phase shift

Demodulation: OOCSSK:

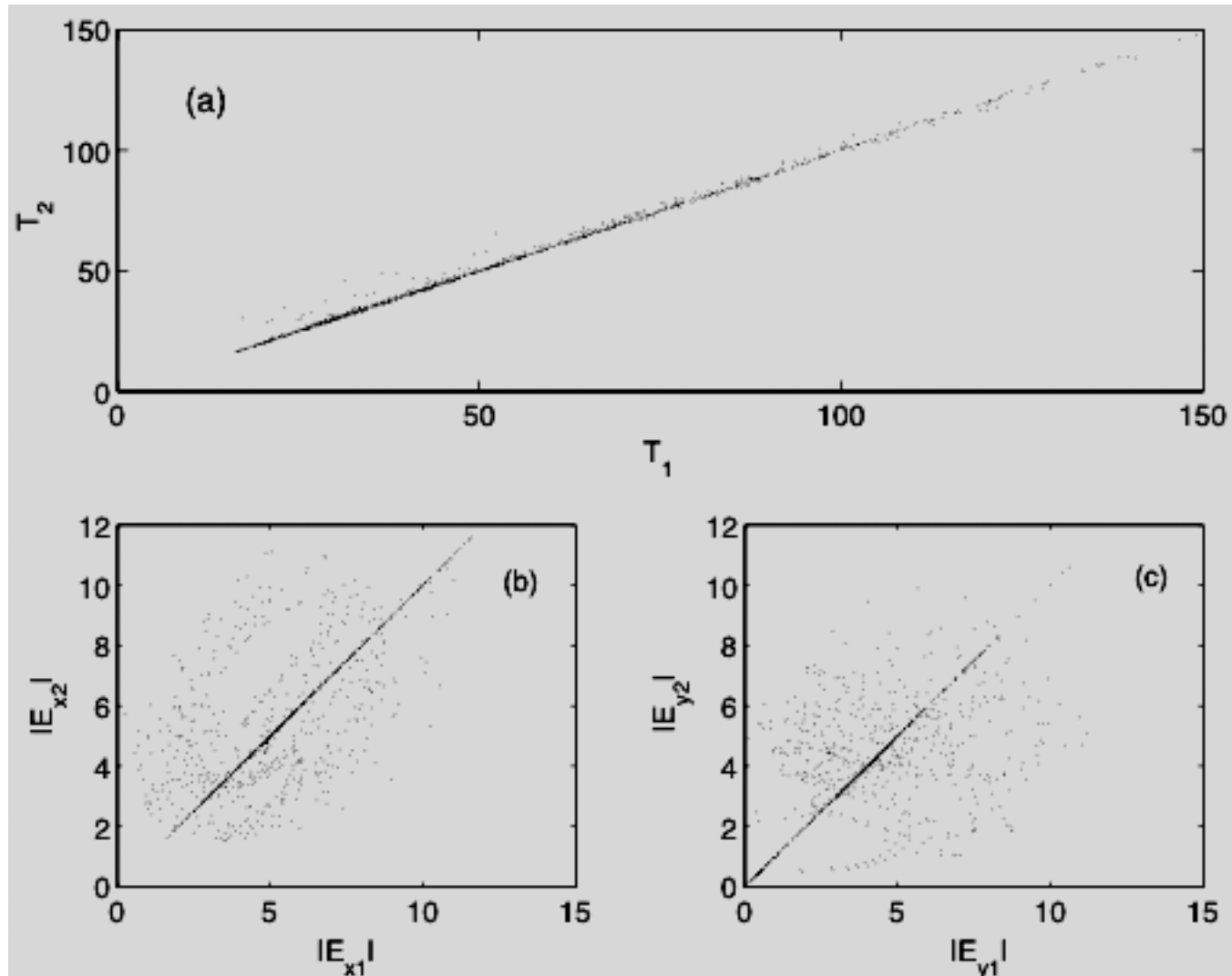
bit “0” : slave synchronises;

bit “1” : slave desynchronises partially: I_{tot} remains synchronised,

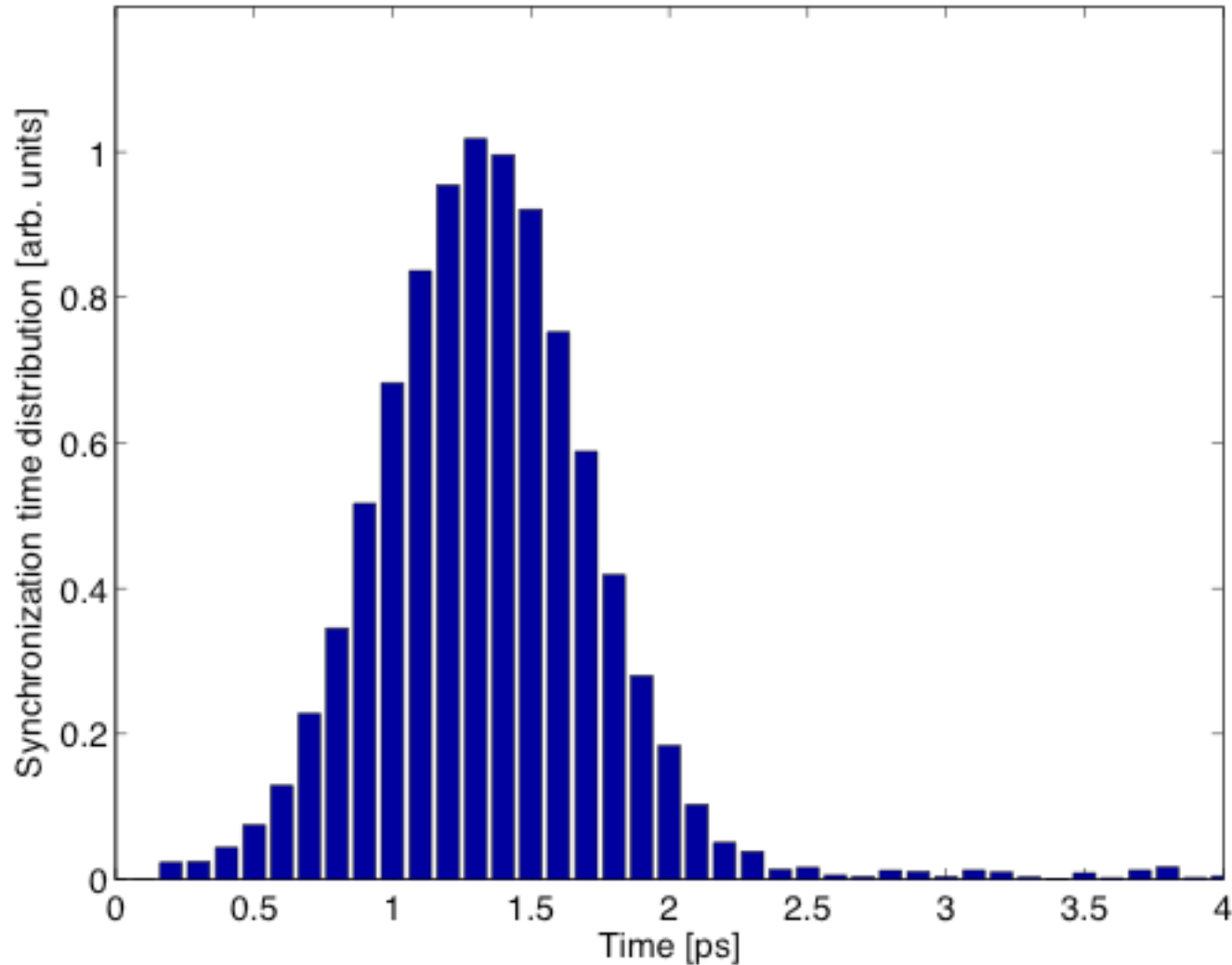
x,y- pol. comps desynchronise.

Bit recovery through On-Off Chaos Shift Keying (OOCSSK)

Synchronisation diagrams: total intensity and polarisation comp's



Synchronisation time



Very fast synchronisation: bit rates up to 100 Gbps possible

Conclusions

- VCSEL where active region is surrounded by saturable absorber can exhibit **vectorial chaos**: chaos in both intensity & pol. No feedback scheme required!
- synchronization properties of two such VCSELs:
 - direct coupling: no robust synchr.
 - continuous control scheme requireddue to **vectorial** nature of the chaotic field.
- **Novel encryption scheme, exploiting phase modulation:**
 - average I_{tot} remains unaffected
 - very fast synchr. -> 100 Gbps transmission possible
- -> other laser sources with vectorial chaos?
Cf Van Wiggeren & Roy, PRL 2002.

Scire et al. Phys. Rev. Lett. 90, 113901 (2003)