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# ***Spatio-temporal Dynamics of Nonlinear Optical Systems***

 ***GENERAL ASPECTS OF OPTICAL PATTERNS***

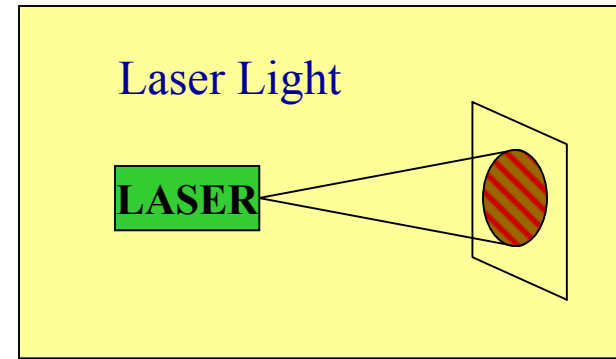
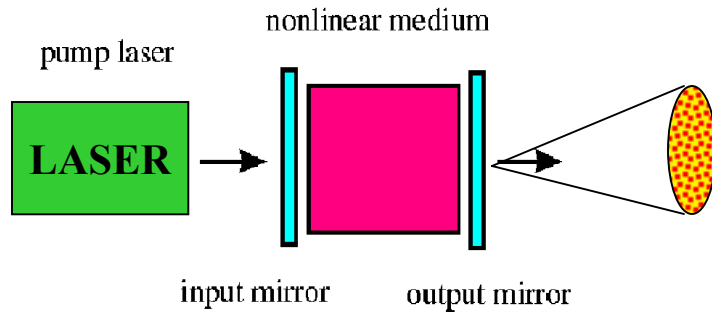


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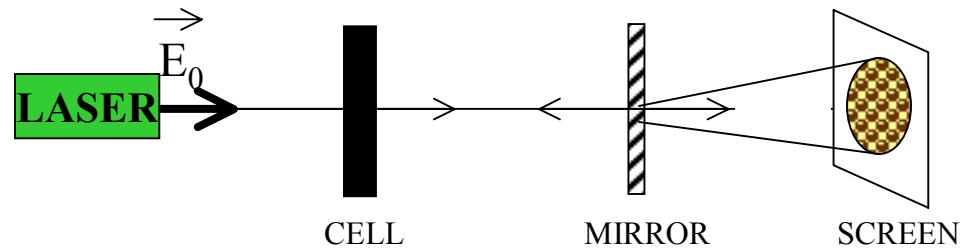


# OPTICAL TRANSVERSE PATTERNS

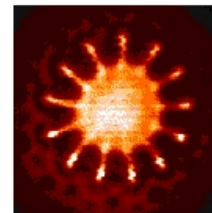
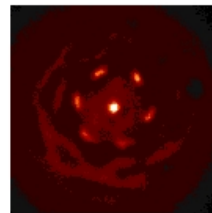
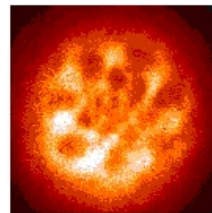
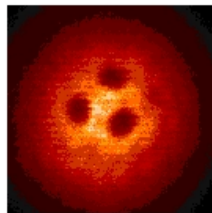
## Nonlinear medium in optical cavity



## Single feedback mirror configuration



Na cell



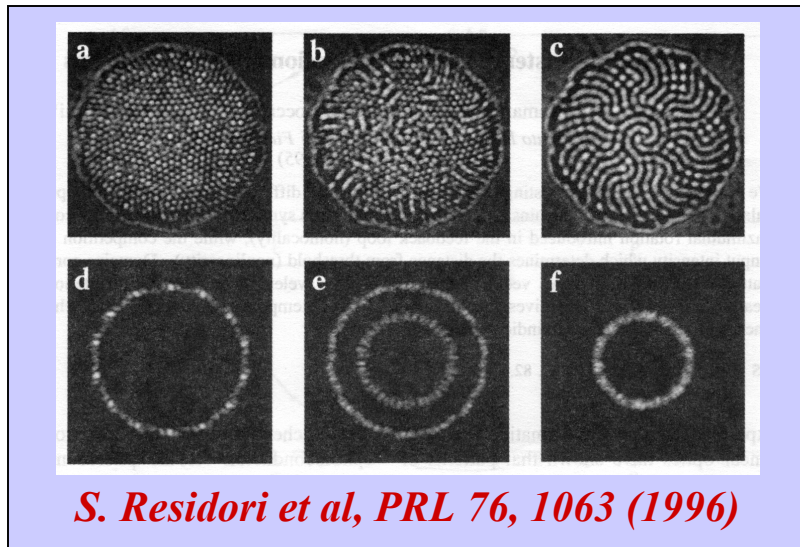
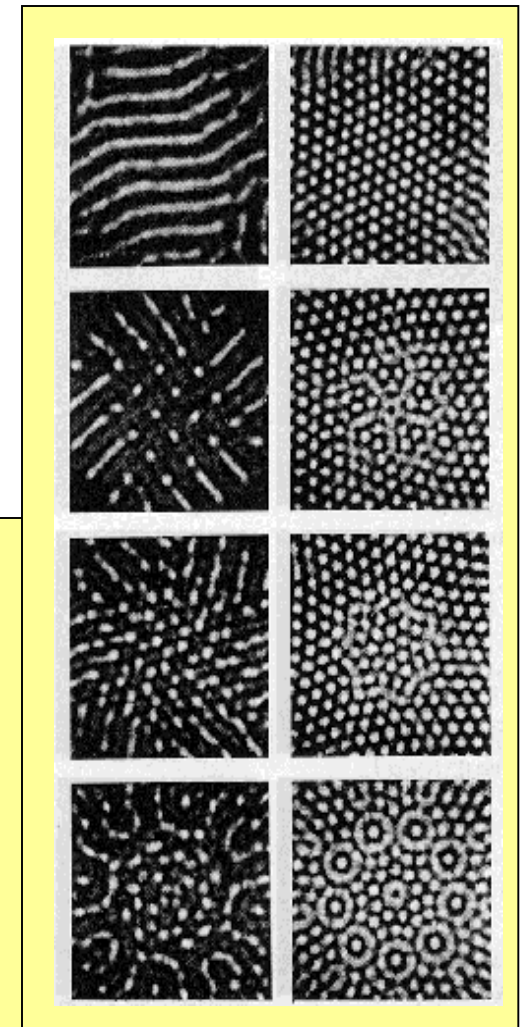
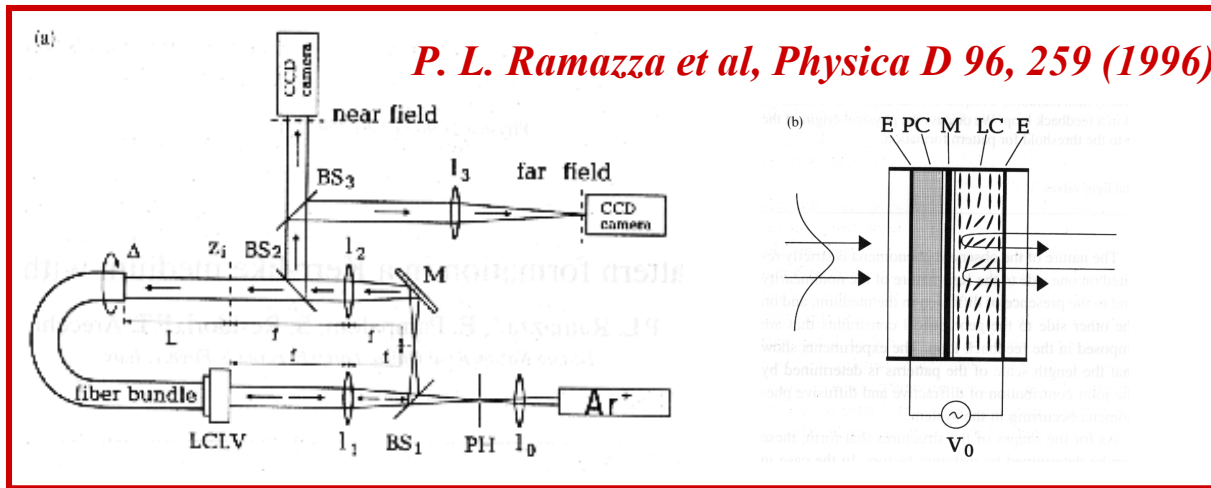
*T. Ackemann et al.  
PRL 75, 3450(1995)*



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# OPTICAL PATTERNS: LCLV

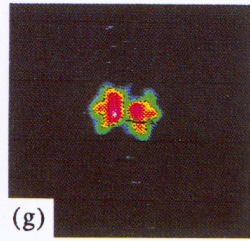




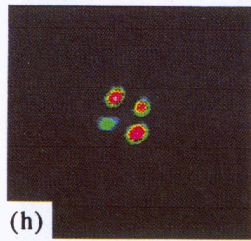
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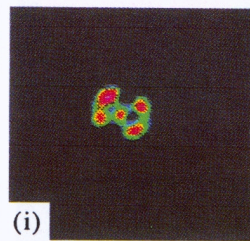
# TRANSVERSE PATTERNS in VCSELS



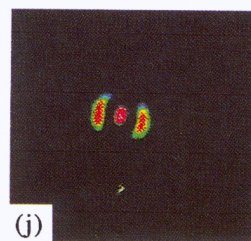
(g) I = 15.3mA, the modes of 0-4th order.



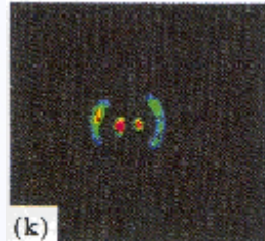
(h) I = 15.3mA, 2nd order mode. Etalon 1 was inserted.



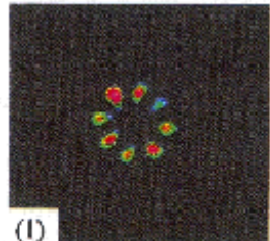
(i) I = 15.3mA, one component of the 2nd order mode. Etalon 1+2 were inserted.



(j) I = 15.3mA, another component of the 2nd order mode. Etalon 1+2 were inserted.



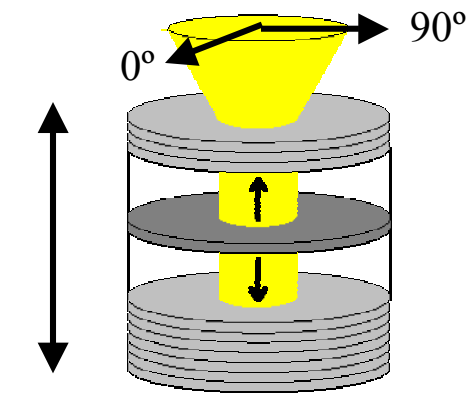
(k) I = 15.3mA, 3rd order mode. Etalon 1 was inserted.



(l) I = 15.3mA, 4th order mode. Etalon 1 was inserted.

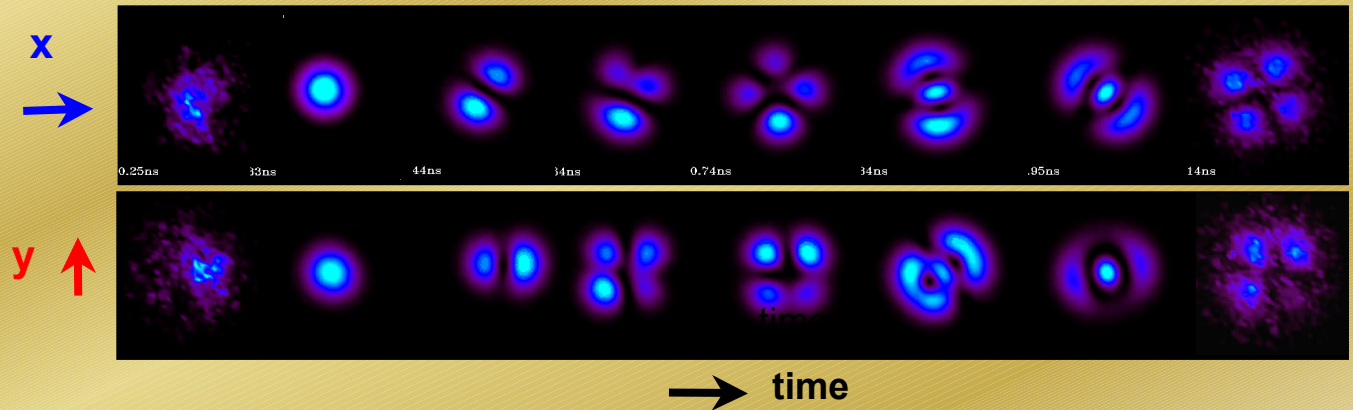
*H. Li et al Chaos, Solitons and Fractals 4, 1619 (1994)*

## VCSEL



$L \sim 1\mu\text{m}$

## Sub-nanosecond electric excitation



*J. Mulet et al, IEEE J. Quantum Electron. 38, 291 (2002)*



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# Optical Patterns

## ☀ ***DIFFRACTION, TIME SCALES, CLEAN SYSTEMS...***

## ☀ ***INFORMATION PROCESSING:***

- **Localized Structures /Cavity Solitons**
- **All-optical image processing**

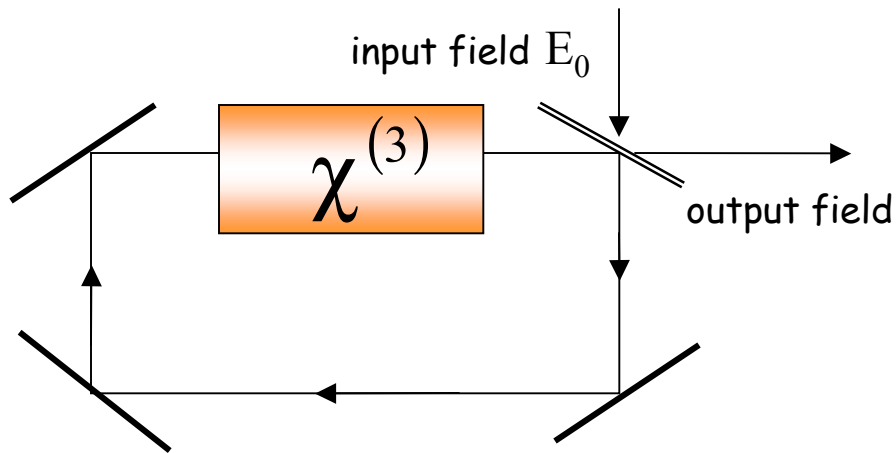
## ☀ ***POLARIZATION OF LIGHT:***

- **Vectorial Spatio-Temporal Phenomena**
- **Correlated Patterns, Phase separation, Symmetry Tuning**

## ☀ ***QUANTUM ASPECTS:***

- **Macroscopic quantum correlations in patterns.**
- **PARALLEL Quantum Information**

## Self-focusing Kerr medium in a ring cavity



$$\vec{E}(\vec{x}, z, t) = \underbrace{\vec{E}(\vec{x}, t)}_{\text{field envelope}} e^{i(k_0 z - \omega_0 t)}$$

$\vec{x} = (x, y)$

Time evolution of field envelope

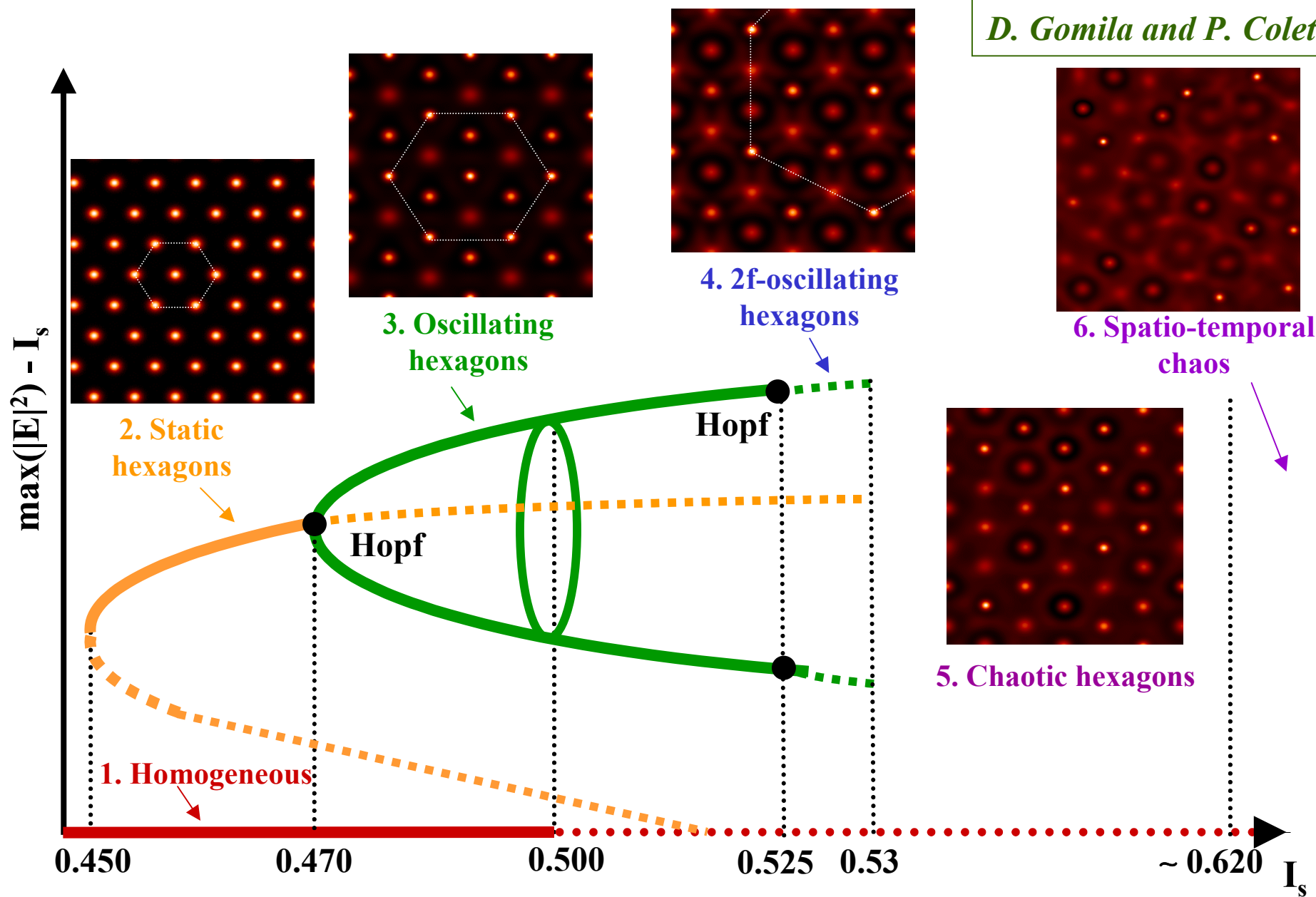
$$\frac{\partial E}{\partial t} = -(1 + i\theta)E + ia\nabla^2 E + E_0 + i2|E|^2 E$$

$\theta = 1$ : cavity detuning,  $E_0$ : input field

$\nabla^2$ : transverse Laplacian,  $a = 1$ : strength of diffraction

# Spatio - Temporal Regimes of Self-Focusing Kerr

*D. Gomila and P. Colet*



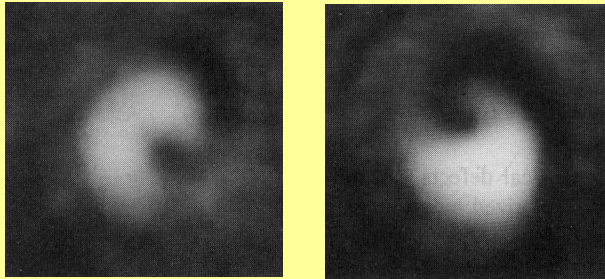


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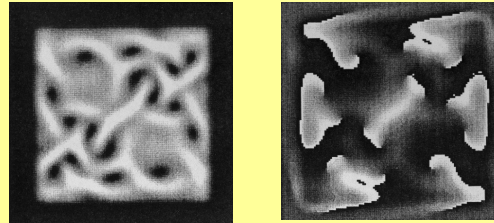
# LOCALIZED STRUCTURES

## Photorefractive Crystals

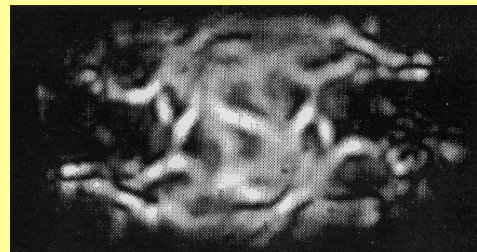


*Optical vortex and phase spiral*

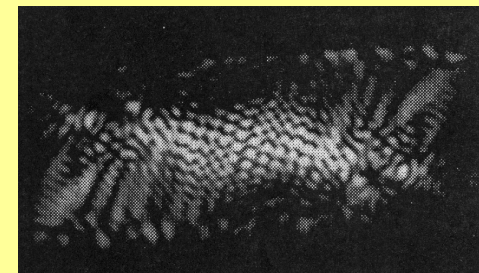
*Arecchi et al. PRL 67, 3751 (1991)*



*Vortices and shocks*



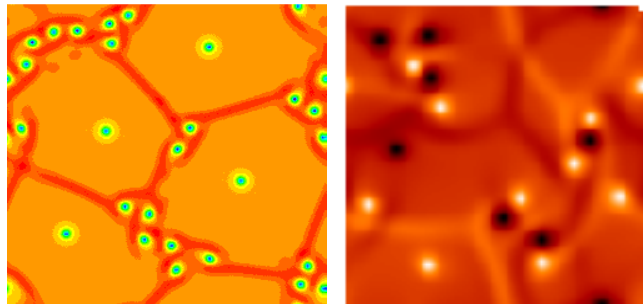
## Vortex lattice



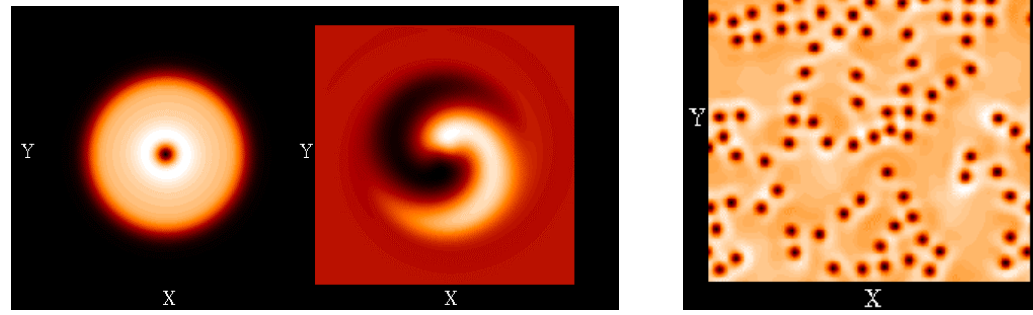
*Staliunas et al.*

*PRL 79, 265 (1997)*

## Broad Area Laser



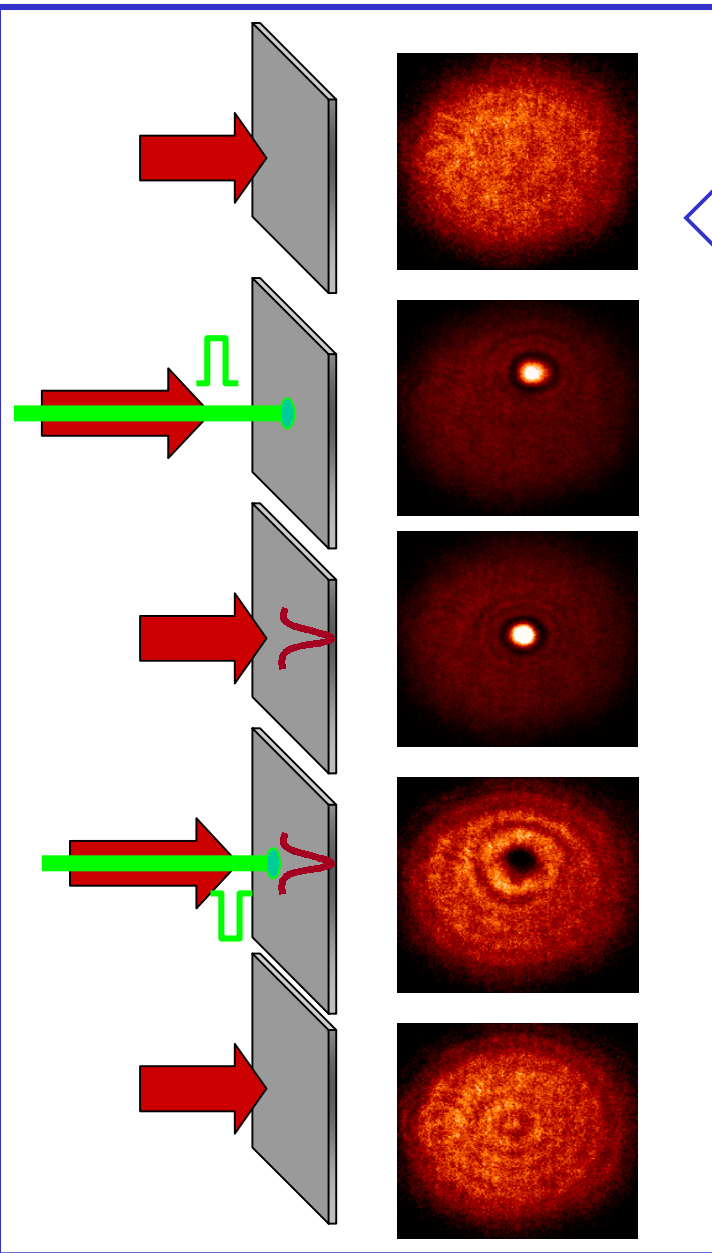
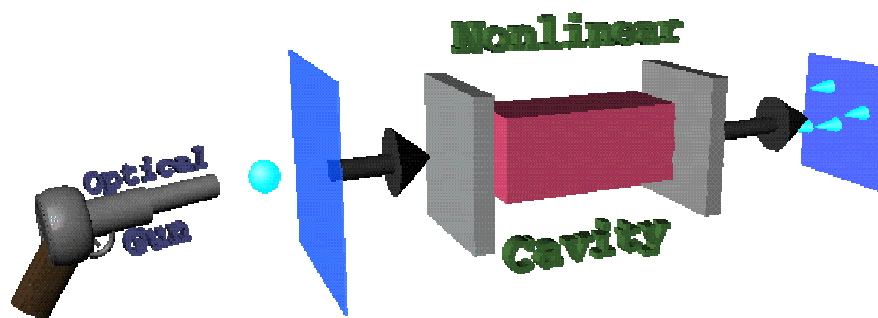
## Optical Parametric Oscillator





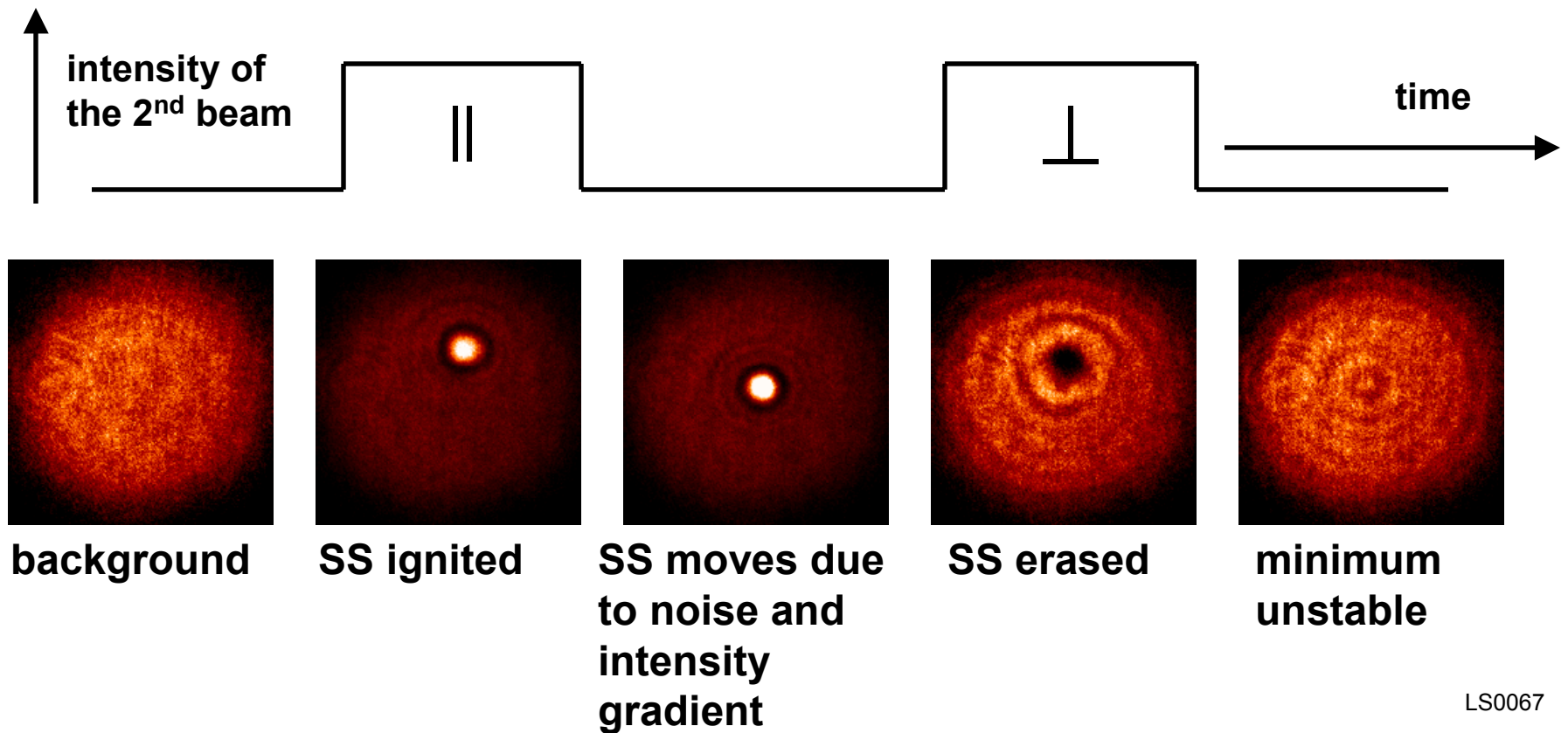
# OPTICAL PROCESSING WITH CAVITY SOLITONS

Write and erase solitons  
in an optical cavity

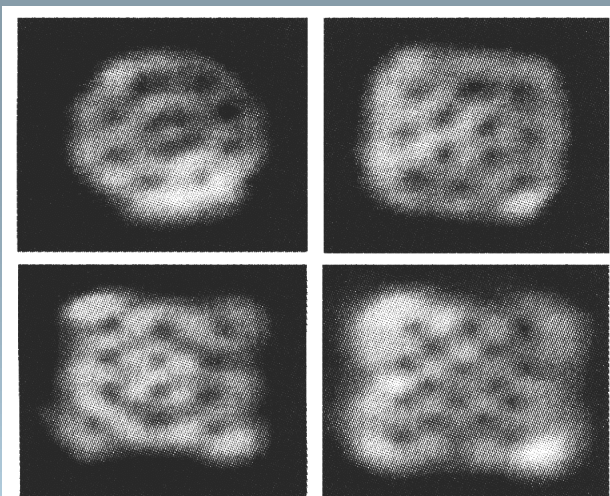


# Switching of Spatial Solitons, *Ackemann-Lange (Munster)*

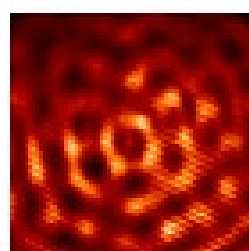
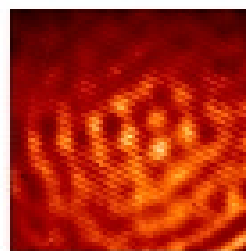
- Addressing: focused second beam (approximately the same size as soliton)
- **Ignition:** circular polarization **parallel** to holding beam
- **Erase:** circular polarization **orthogonal** to holding beam
- **Polarization** properties provide **phase insensitive** way of control (!)



## Patterns and Localized States in VCSELS



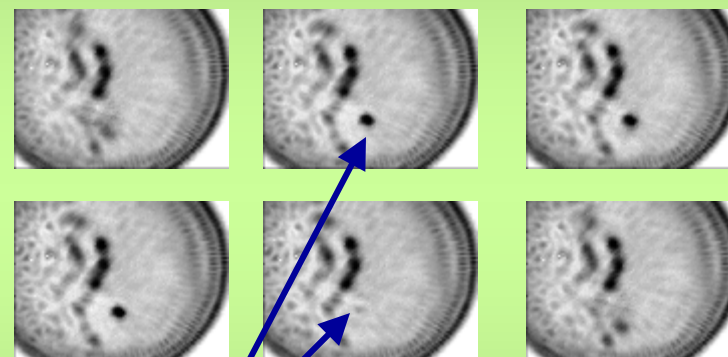
*J. Scheuer, M. Orenstein, Science 285, 230 (99)*



*T. Ackemann et al., IMEDEA-INLN (1999)*

**Control of localized states in  
broad area VCSELS (150  $\mu\text{m}$ )**

**Homogeneous beam +  
Local addressing perturbation**



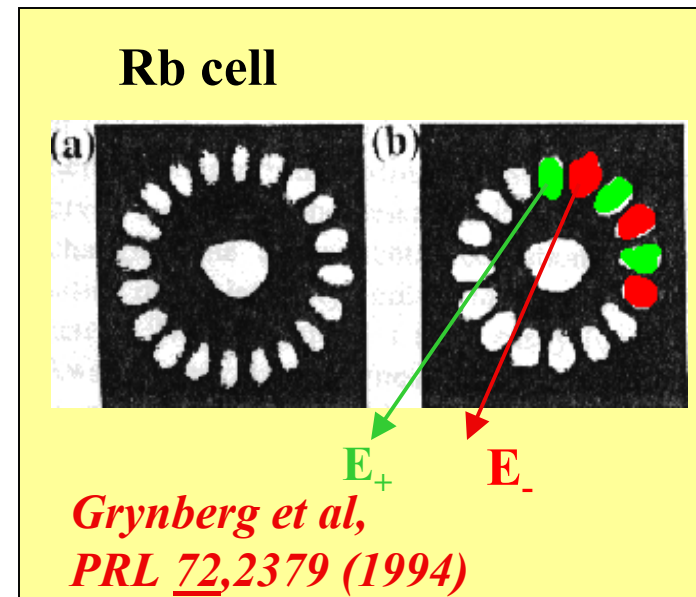
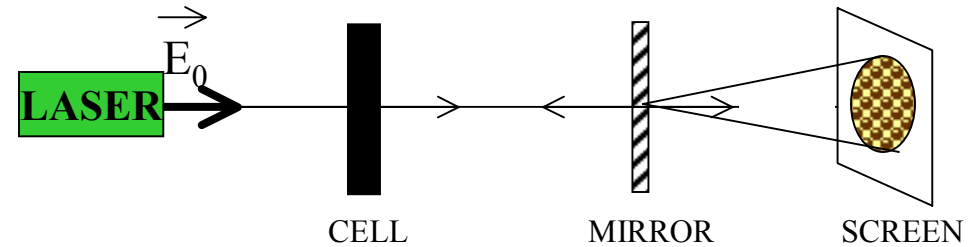
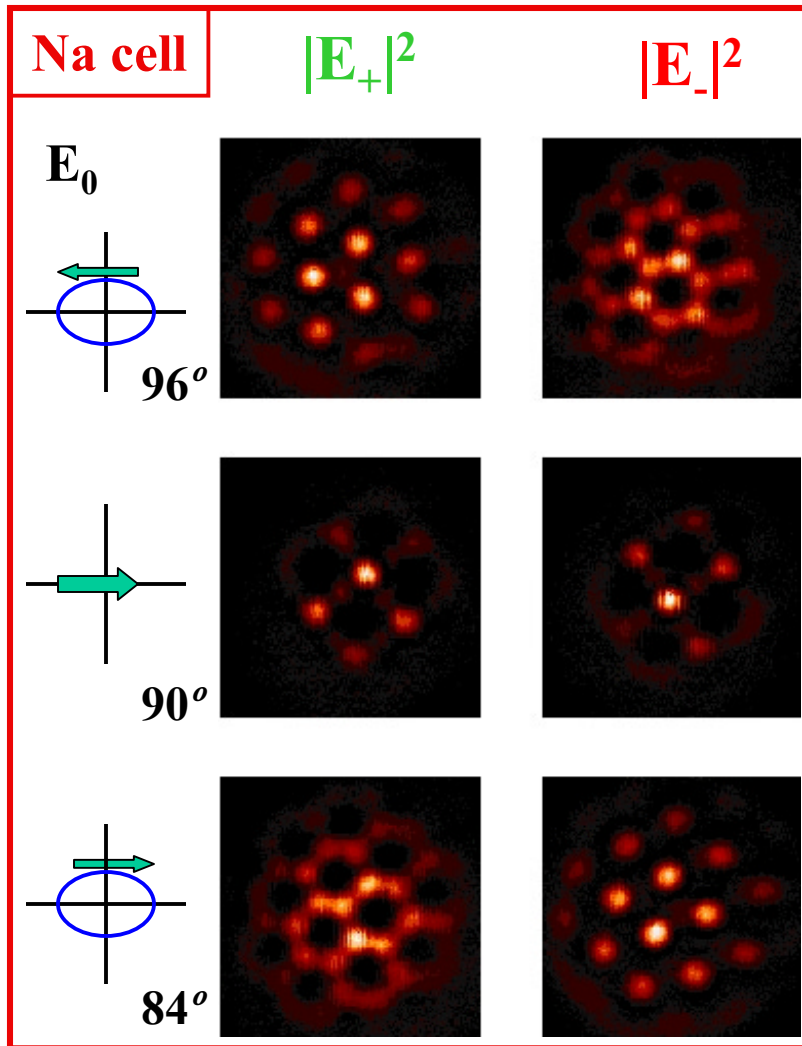
**Switch ON-OFF of LS**



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# POLARIZATION PATTERNS



Aumann et al, Phys. Rev. A 56, R1709 (1997)

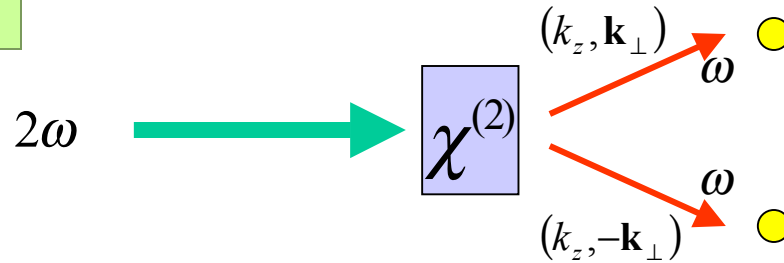


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**PARAMETRIC DOWN CONVERSION:**

**TWIN PHOTON EMISSION**



**Degenerate OPTICAL PARAMETRIC OSCILLATOR:**

**Optical Cavity**

Pump :  $A_0 \Rightarrow 2\omega$        $\partial_t A_0 = \gamma_0 \left[ -(1 + i\Delta_0)A_0 + E_0 + ia_0 \nabla^2 A_0 + 2iK_0 A_1^2 \right] + \sqrt{\epsilon_0} \xi_0(\mathbf{r}, t)$

Signal :  $A_1 \Rightarrow \omega$        $\partial_t A_1 = \gamma_1 \left[ -(1 + i\Delta_1)A_1 + ia_1 \nabla^2 A_1 + iK_0 A_1^* A_0 \right] + \sqrt{\epsilon_1} \xi_1(\mathbf{r}, t)$

**Stripe patterns**

$$A_1(\mathbf{r}, t) = A_+ e^{iq_M x} + A_- e^{-iq_M x} = R e^{i\phi} \cos(q_M x + \psi)$$

$$q_M(\Delta_1) = |\mathbf{k}_\perp|, \quad \phi(\Delta_0) \text{ fixed, } \psi \text{ arbitrary}$$

**FLUCTUATIONS:**  $\left\{ \begin{array}{l} I_+ - I_- \text{ small } \left( I_\pm = |A_\pm|^2 \right) \\ \psi \text{ large fluctuations} \end{array} \right\}$

**QUANTUM COMPLEMENTARITY**

**Squeezing in photon number difference**