

Semiconductor Ring Laser dynamics

IFISC seminar

5.00um

S4700 30.0kV 12.5mm x9.00k SE(M)



- Introduction
- Basic properties (directional bistability)
- Modal Properties
- <u>TW-modelling</u>
- Directional switching
- Noise properties

Langevin formulation, noise spectra Mode hopping

Applications

Inertial rotation sensing

Hardware Random Number Generation

New structures

Snail laser Active Photonic Molecules

Conclusions

Sources of light



- Natural
- Direct chemical
- Combustion-based
- Electric powered
- Incandescent lamps
- Electroluminescent lamps
- Gas discharge lamps
- High-intensity discharge lamps
- LASER



Gas lasers

- Chemical lasers
- Dye lasers
- Metal-vapor lasers
- Solid-state lasers
- Semiconductor lasers
- X-rays



- Edge-emitter
- Vertical Cavity
- Ring









- Research
 - Multimode properties
 - Non-linear dynamics
 - - -
- Applications
 - Telecom
 - Data storage/reading
 - Measuring instruments
 - Laser absorption spectrometry





















SIXTH FRAMEWORK PROGRAMME

FP6-2005-IST-5

PRIORITY 2 - INFORMATION SOCIETY TECHNOLOGIES



Contract for:

SPECIFIC TARGETED RESEARCH PROJECT

Annex I - "Description of Work"

Project acronym: IOLOS

Project full title: Integrated Optical Logic and Memory using Ultra-fast Micro-ring Bistable Semiconductor Lasers

Proposal/Contract no.: 34743

Partic. Role*	Partic. no.	Participant name	Participant short name	Country
CO	1	University of Bristol	UNIVBRIS	UK
CR	2	University of Glasgow	GU	UK
CR	3	Università degli Studi di Pavia	UNIPV	Italy
CR	4	Universitat de les Illes des Balears	UIB	Spain
CR	5	Vrije Universiteit Brussel	VUB	Belgium
CR	6	Intense Ltd	Intense	UK
CR	7	Siemens SA	Siemens	Portugal

"Development of Theoretical Model and Simulation Tools for SRL bistable device: develop theoretical framework and numerically implement mathematical models to provide understanding and guidance for the design and optimisation of the bistability and switching speed of micro-SRLs."











PUBLICATIONS

MODAL STRUCTURE, DIRECTIONAL AND WAVELENGTH JUMPS OF INTEGRATED SEMICONDUCTOR RING LASERS: EXPERIMENT AND THEORY

Fürst, Sandor; Pérez-Serrano, Antonio; Scirè, Alessandro; Sorel, Marc; Balle, Salvador Applied Physics Letters **93**, 251109 , (2008)



Modes in a Ring Cavity

Electric field:

$$E(z,\omega) = A_F(\omega)e^{iq(\omega)z} + A_B(\omega)e^{-iq(\omega)z}$$

Boundary conditions:

 $\left\{ \begin{array}{l} A_F = RA_B + TA_F e^{iq(\omega)L} \\ A_B e^{-iq(\omega)L} = RA_F e^{iq(\omega)L} + TA_B \end{array} \right. \label{eq:AF}$



Ideal ring (R = 0, T = 1):

$$q=\frac{2\pi m}{L} \quad m=0,\pm 1,\pm 2,\ldots$$

General case ($R \neq 0$, $T \neq 0$):

$$q_{\pm} = \frac{2\pi m}{L} + \frac{i}{L}\ln(T\pm R) \qquad m = 0, \pm 1, \pm 2, \dots$$

Two branches of solutions



Theoretical Analysis

Round Trip Condition:

$$e^{2iqL} - ae^{iqL} + b = 0$$



$$b = (r_u r'_u - t_u t'_u)^{-1} (r_d r'_d - t_d t'_d)^{-1} \qquad a = (r_u r_d + r'_u r'_d + t'_u t_d + t_u t'_d) b$$

Modes:

$$q_m^{\pm}L = 2\pi m - i \ln Q_{\pm}$$
 $Q_{\pm} = a/2 \pm [(a/2)^2 - b]^{1/2}$

Splitting:
$$\Delta = \frac{1}{2\pi} \left\{ \operatorname{Im} \left[\ln \left(\frac{Q_{-}}{Q_{+}} \right) \right] - \alpha \operatorname{Re} \left[\ln \left(\frac{Q_{-}}{Q_{+}} \right) \right] \right\}$$

laser



Experimental Setup

lensed PC tunable bias $\odot \odot \odot$ fiber - Wafer: Multiple QW laser PORT1 PORT2 AlGaInAs/InP structure grown by MOCVD. stage lock-in amplifier - Waveguides defined by electron beam lithography bias circuit reference R=300µm and transferred to a PECVD SiO₂ layer, using CHF₃ RIE. - Shallow etched ridge-PORT3 PORT4 waveguide defined by RIE, using -3V CH_4 / H_2 / O_2 process. lock-in amplifier bias circuit

- Deposition of SiO₂ layer and contact window definition
- Metal contacts deposited on epitaxial and substrate sides of the wafer section.



IFISC











Ultrafast All-Optical Switching of Bistable Semiconductor Ring Lasers

- J. Javaloyes₁, A. Trita₂, G. Mezosi₁, F. Bragheri₂, I. Cristiani₂, G. Giuliani₂, M. Sorel₁, A.Scirè₃ and S. Balle₄
- 1. Dept. of Electronics and Electrical Engineering, U. of Glasgow, Rankine Building, Oakfield Avenue, Glasgow G12 8LT, UK
- 2. Dip. di Elettronica, Università di Pavia, I-27100 Pavia, Italy
- 3. Instituto de Física Interdisciplinar y Sistemas Complejos (CSIC-UIB), Ctra. Valldemossa km. 7'5, E-07122 Palma de Mallorca, Spain
- 4. Institut Mediterrani d'Estudis Avançats (CSIC-UIB), C/. Miquel Marqués 21, E-07190 Esporles, Spain

IFISC Laser description. Active medium.

Medium Polarization:

$$\mathcal{P} = \varepsilon_0 \Gamma_x \chi(\omega, N) E(z, \omega)$$

Lorentzian Susceptibility:

$$\chi(\omega, N) = \frac{\chi_0 N}{\omega - \omega_0 + i\gamma}$$



- Quasimonochromatic approximation

 $A(z,\omega) \sim \delta(\omega-\Omega)$

- Slowly varying amplitude approximation

$$\begin{split} \lambda^2 \frac{\partial^2 A_{B,F}}{\partial z^2} \ll \lambda \frac{\partial A_{B,F}}{\partial z} \ll A_{B,F} \\ \lambda \frac{\partial A_{B,F}}{\partial z} \sim 0 \end{split}$$



 $-lm(\chi)/\chi$

- Analytic optical susceptibility from equilibrium manybody theory for Quantum-Well semiconductor lasers
- Nonlinear dependence on the carrier density, providing both a broad gain spectrum and a dispersion curve, "so it can be used to analyze the dynamics of multimode devices or devices with large carrier density variations".
- [S.Balle Phys. Rev. A 37 1304 (1999)]



$$\chi(\omega,N) = -\chi_0 \left[2\ln\left(1 - \frac{D}{u+i}\right) - \ln\left(1 - \frac{b}{u+i}\right) \right], \quad (6)$$





Directional switching in Semiconductor Ring Laser induced by pulse injection



18 ps round trip



 $\mathcal{E}(x, y, z, t) = \left[A_{+}(z, t)e^{iq_{0}z} + A_{-}(z, t)e^{-iq_{0}z}\right] \times \Phi(x, y, \omega_{0})e^{-i\omega_{0}t} + c. c.$ $N(z, t) = N_{0}(z, t) + \left[N_{2}(z, t)e^{2iq_{0}z} + c. c.\right] + \cdots$

$$\begin{split} \left(\pm \partial_{z} + \frac{1}{v_{g}} \partial_{t} \right) A_{\pm} &= i \frac{\omega_{0}}{2\varepsilon_{0}cn} B_{\pm}(z,t) - \frac{\alpha_{i}}{2} A_{\pm} \\ \partial_{t} N_{0} &= \frac{I}{eV_{a}} - R(N_{0}) + \mathcal{D}\partial_{z}^{2}N_{0} - \frac{2i}{\hbar S_{a}} (A_{+}^{*}B_{+} + A_{-}^{*}B_{-} - c. c.) \\ \partial_{t} N_{2} &= - \left[R'(N_{0}) + 4\mathcal{D}q_{0}^{2} \right] N_{2} - \frac{2i}{\hbar S_{a}} (A_{-}^{*}B_{+} - A_{+}B_{-}^{*}) \\ ib(N_{0})\partial_{t} B_{\pm} &= - B_{\pm} + \varepsilon_{0}\Gamma \left[\chi(\omega_{0}, N_{0})A_{\pm} + ia(N_{0})\partial_{t}A_{\pm} \right] \\ &- \varepsilon g_{NL}(\omega_{0}, N_{0})(|A_{\pm}|^{2} + 2|A_{\mp}|^{2})A_{\pm} \\ &+ \chi_{N}(\omega_{0}, N_{0})N_{\pm}2A_{\mp} \end{split}$$

$$a(N) = \chi_{\omega}(\omega_0, N) + b(N) \chi(\omega_0, N)$$

$$b(N) = -\frac{1}{2} \frac{\chi_{\omega\omega}(\omega_0, N)}{\chi_{\omega}(\omega_0, N)}$$

$$g_{NL}(\omega, N) = [\chi(\omega, N) - c.c.]/4$$





Dynamics as a function of the Pulse Energy



<u>High Pulse energy</u> Fast switching with relaxation oscillation

Resonant pulse, fixed FWHM (47 ps) variable Energy Low Pulse energy No switching



Dynamics as a function of the Pulse Energy



<u>High Pulse energy</u> Fast switching with relaxation oscillation

Low Pulse energy No switching

Resonant pulse, fixed FWHM (47 ps) variable Energy



Dynamics as a function of the Pulse Energy



Experimental Results (5ps Pulses)

High Pulse energy Fast switching with relaxation oscillation

Low Pulse energy

No switching



Dynamics as a function of the Pulse width



Resonant pulse, fixed Energy (2.e-09) variable FWHM

slow Pulse

All the energy goes

into the lasing mode

Fast Pulse

Energy is shared

between adjacent modes



Dynamics as a function of the Pulse width



Experimental Results (5ps Pulses)

slow Pulse All the energy goes into the lasing mode

Fast Pulse

Energy is shared

between adjacent modes



Dynamics as a function of the pulse detuning



To mitigate

With higher energy one can switch with high detuning With short pulses (broad spectrum), detuning is irrelevant Resonant Pulse

All the energy goes into the lasing mode

<u>AntiResonant Pulse</u> Energy can not enter the cavity



Dynamics of a Set-Reset operation



Set-Reset operation

is limited by the

- Rise time of the pulse
- Rise time of the laser
- High speed \implies Short pulse



Fast pulse response and Scaling Down Laser Size



No improvment on the rise time while decreasing the size

Small devices are more complicated (thermal managment)



Fast pulse response and Scaling Down Laser Size



1 = Flip-Flop0 = Nothing

Reliable Set-Reset operation up to <u>20 Gbits/s</u> Limit depends on coding and energy



Fast pulse response and Scaling Down Laser Size



1 = Flip-Flop0 = Nothing

Reliable Set-Reset operation up to <u>20 Gbits/s</u> Limit depends on coding and energy



- Minimal Pulse Energy to trigger the reversal
- Large Pulse Energies induce Relaxation Oscillations
- Shorter Pulses may encompass several modes
- Detuning is important for slow pulses
- Shorter devices don't give an immediate improvement
- Set-Reset at 20 Gbit/s seems an attainable regime
- Rise time is governed by pulse width & pulse energy



PUBLICATIONS

NOISE SPECTRA OF A SEMICONDUCTOR RING LASER IN THE BIDIRECTIONAL REGIME

Pérez-Serrano,Antonio;Zambrini,Roberta;Scirè,Alessandro;Colet,Pere Submitted to Physical Review A , (2009)



SRL Model including spontaneous emission noise



 $\begin{cases} \dot{E}_{\pm}(t) = \mathcal{G}_{\pm}(N(t), |E_{\pm}(t)|^2) \ E_{\pm}(t) - \eta \ E_{\mp}(t) + \xi_{\pm}(t) \\ \dot{N}(t) = \gamma \ \mathcal{F}(N(t), |E_{\pm}(t)|^2) \end{cases}$ $\mathcal{G}_{\pm}(N(t), |E_{\pm}(t)|^2) = \frac{1}{2}(1 + i\alpha)\{N(t) \ \sigma_{\pm} - 1\}$ $\mathcal{F}(N(t), |E_{\pm}(t)|^2) = \mu - N(t) - N(t) \ \sigma_{\pm} \ |E_{\pm}(t)|^2 - N(t) \ \sigma_{-} \ |E_{-}(t)|^2 \\ \sigma_{\pm} = 1 - s \ |E_{\pm}(t)|^2 - c \ |E_{\mp}(t)|^2 \\ \eta = k_d + ik_c \end{cases}$

$$\begin{aligned} \langle \xi_{\pm}(t)\xi_{\pm}^{*}(t')\rangle &= 2D\delta(t-t')\\ \langle \xi_{\pm}(t)\xi_{\mp}^{*}(t')\rangle &= \langle \xi_{\pm}(t)\xi_{\pm}(t')\rangle = 0 \end{aligned}$$

$$\langle \xi_{\pm}(t)\xi_{\pm}^{*}(t')\rangle = 2\sqrt{\beta\tau_{p}N_{st}}\delta(t-t')$$



Linear Fluctuations Dynamics

$$E_{\pm}(t) = (Q + a_{\pm}(t))e^{i\omega t \pm i\phi} \qquad N(t) = \bar{N} + n(t)$$
Variable change \longrightarrow Block diagonalization
$$S(t) = a_{+}(t) + a_{-}(t) \qquad \begin{pmatrix} \dot{S}(t) \\ \dot{S}^{*}(t) \\ \dot{n}(t) \\ \dot{R}(t) = a_{+}(t) - a_{-}(t) \qquad \begin{pmatrix} \dot{S}(t) \\ \dot{S}^{*}(t) \\ \dot{R}^{*}(t) \end{pmatrix} = \begin{pmatrix} \boxed{3 \times 3} & \begin{smallmatrix} 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 & \boxed{2 \times 2} \end{pmatrix} \begin{pmatrix} S(t) \\ S^{*}(t) \\ n(t) \\ R(t) \\ R^{*}(t) \end{pmatrix} + \begin{pmatrix} \xi^{*}_{S}(t) \\ \xi^{*}_{S}(t) \\ \xi^{*}_{R}(t) \\ \xi^{*}_{R}(t) \end{pmatrix}$$
Physical interpretation $\bigwedge Re(S) \equiv I \longrightarrow$ Total intensity
 $Re(R) \equiv D \longrightarrow$ Intermodal power exchange







PUBLICATIONS

TOPOLOGICAL INSIGHT INTO THE NON-ARRHENIUS MODE HOPPING OF SEMICONDUCTOR RING LASERS

Beri,S.; Gelens,L.; Mestre, M.; Van der Sande, G.; Verschaffelt, G.; Scirè, A.; Mezosi, G., Sorel, M.; Danckaert, J. Physical Review Letters **101**, 093903 (1-4) (2008)







FIG. 2: Comparison between measured time series (a)-(c), simulated time series (d)-(f) and phase space trajectories (g)-(i) for different kind of transitions. In the experiment the ring was biased at $J_{ring} = 39.86$ mA; the waveguide was biased at 8.22mA and the temperature was 21.55°C. In the numerical simulation the following parameters were used: $\mu = 1.59$, $\alpha = 3.5$, s = 0.005, c = 0.01 k = 0.44ms⁻¹, $\phi_k = 1.5$, $D = 6.5 \cdot 10^{-5}$ ms⁻¹. The notation of (f)-(i) is as follow: *CW*, *CCW* are the stable states, *S* is the saddle; solid line: stable manifold of *S*, dashed line: unstable manifold of *S*, gray: projection of the time series (d)-(f).



Applications

PUBLICATIONS

THEORETICAL ANALYSIS OF A NEW TECHNIQUE FOR INERTIAL ROTATION SENSING USING A SEMICONDUCTOR RING LASER

Pérez-Serrano, A;Scire,A; Photonics Technology Letters, vol. 21, issue 13, July 1 2009, pp. 917-919 , (2009)



THE RING LASER GYROSCOPE



The change in path length generates a frequency shift

A: area p: perimeter λ: laser wavelength



Because of backscattering the counterpropagating modes are coupled at low rotation rates



The locking frequency is proportional to the mode coupling strength

$$\Delta \upsilon$$
=4ΑΩ/p λ =RΩ

Not respected at low rotation rates



SRL Gyroscope modeling

$$\dot{E}_{\pm}(t) = \mathcal{G}_{\pm}(N(t), |E_{\pm}(t)|^2) E_{\pm}(t) - \eta E_{\mp}(t) \pm i\Delta E_{\pm}(t),$$

$$\dot{N}(t) = \gamma \mathcal{F}(N(t), |E_{\pm}(t)|^2),$$

$$\begin{aligned} \mathcal{G}_{\pm}(N(t), |E_{\pm}(t)|^2) &= \frac{1}{2}(1+i\alpha)\{N(t) \ \sigma_{\pm} - 1\}, \\ \mathcal{F}(N(t), |E_{\pm}(t)|^2) &= \mu - N(t) - N(t) \ \sigma_{\pm} \ |E_{\pm}(t)|^2 \\ -N(t) \ \sigma_{-} \ |E_{-}(t)|^2, \\ \\ \sigma_{\pm} &= 1 - s \ |E_{\pm}(t)|^2 - c \ |E_{\pm}(t)|^2, \\ \\ \eta &= k_d + ik_c \end{aligned}$$

$$+ \underbrace{D_{\pm}(v)}_{+}$$

$$\Delta = \frac{2\pi R\tau_p}{\lambda} \Omega_{rot}$$

$$E_{\pm}(t) = Q_{\pm}e^{i(\omega t \pm \psi/2)}, \ N(t) = \bar{N}.$$



SRL Responsivity to inertial rotation

 $\chi = \frac{|E_{-}|^{2} - |E_{+}|^{2}}{|E_{+}|^{2} + |E_{-}|^{2}} = \frac{2}{Q}\delta = \mathcal{R}\Omega_{rot} \quad \mathcal{R} = \frac{4\pi k_{c}R\tau_{p}}{\lambda(2k_{d}^{2} + 2k_{c}^{2} - (k_{d} + \alpha k_{c})Q^{2}\bar{N}(s - c))}$









Bistable SRL as a possible generator of optical random bits by current modulation

A.Scirè, A.Perèz-Serrano, G.VanDerSande, J.Danckaert

In progress...





IDEA: In Bi-SRLs the laser switch-on mechanism itself provides a non-linear fast amplification of the noisy seed of the spontaneous emission. Being spontaneous emission isotropic, the probability that each spontaneously emitted photon is coupled to the cw (resp. ccw) mode is ½ for fundamental reasons. So, when the laser switches on due to current modulation towards the bistable region, cw or ccw mode will be activated with the same probability. However, fluctuations in such process lead the directional mode selection to be a stochastic process itself, in which microscopic fluctuations are brought to a macroscopic level during the laser switch on.





Random Bits Generator, with simulations Two-mode Rate Equations





Electronic noise based RNGs (today produced and sold by INTEL) primarily sample thermal noise by amplifying the voltage measured across undriven resistors. The architecture is called *Dual Oscillator*

The thermal noise source is used to modulate the frequency of the slower clock. The variable, noise-modulated slower clock is used to trigger measurements of the fast clock. Drift between the two clocks thus provides the source of random binary digits.

[Velichko, S. "Random-number Generator Prefers Imperfect Clocks." *EDN Access*, 1996. (http://ednmag.com/reg/1996/112196/23_di04.cfm). Hoffman, Eric. *Random Number Generator*, 1996, U.S. Patent 5,706,208].

In the optical domain, existing RNGs are based on single-photon statistics (SPS) at a (ideally) 50% optical beam splitter

SPS take profit of the quantum discretization of light, so they need to operate in a range of optical power at which such discretization is visible, i.e. down to a single photon.

SPSs are limited in bandwith (MHz), bulky. SPS are produced and sold by QUANTIS

[US Patent 6393448, Deutche Telekom (2002); J.M. Mérolla et al., Single-Photon Interference in Sidebands of Phase-Modulated Light for Quantum Cryptography, Phys. Rev. Lett. 1656 (1999)].



Quantum Random Number Generator



When random numbers cannot be left to chance!

Although random numbers are required in many applications, their generation is often overlooked.

Being deterministic, computers are not capable of producing random numbers. A physical source of randomness is necessary. Quantum physics being intrinsically random, it is natural to exploit a quantum process for such a source. Quantum random number generators have the advantage over conventional randomness sources of being invulnerable to environmental perturbations and of allowing live status verification.

Quantis is a physical random number generator exploiting an elementary quantum optics process. Photons - light particles - are sent one by one onto a semi-transparent mirror and detected. The exclusive events (reflection - transmission) are associated to "0" - "1" bit values.

The operation of Quantis is continuously monitored. If a failure is detected the random bit stream is immediately disabled.

Quantis is available as a PCI card, an USB device and a component for mounting on a printed circuit board (see Quantis-OEM). Quantis is easily integrated in existing applications.

Main features

- True quantum randomness.
- Passes NIST and Diehard randomness tests
- High bit rate up to 16 Mbits/s
- Low cost
- Compact and reliable.
- Continuous status check.
- Easy integration in existing applications.

Applications

- Cryptography
- Gambling, lotteries
- Secure printing.
- PIN number generation.
- Mobile prepaid system.
- Statistical research
- Numerical simulations



	Electronic RNG (Intel)	Single Photon RNG (Quantis)	Bi-SRL
RNG rate	KHz	MHz	GHz
Cost	Low	100-1000 Eu	?
Size	100-1000 mm ²	10-100 mm ²	1 mm ²
Output signal	Electrical	Electrical	Optical
Physical process behind randomness	Thermal noise in a resistor	Single photon transmission at a 50% beam splitters	Spontaneous emission noise





Semiconductor Snail Lasers

- M. J. Strain¹, A. Pérez-Serrano², G. Mezösi¹, G. Verschaffelt³, A. Scirè², J. Danckaert³, M. Sorel¹, S. Balle⁴
- 1. University of Glasgow
- 2. IFISC (UIB-CSIC), Palma de Mallorca
- 3. Vrije Universiteit Brussel
- 4. IMEDEA (UIB-CSIC)



SNAIL – Semiconductor Ring Laser



Fig. 1 (a) SRL schematic design. Output facet with reflectivity r_j ($r_j < r_i$). (b) Snail Laser schematic design. Output facet with reflectivity r_j ($r_2 < r_j$). The waveguided of length L is pumped. The red line marks the resonant path.



Fig. 2 (a) Carrier density threshold (D_{th}) vs Coupling efficiency (δ) for different parameter values and configurations. (b) Output Power vs Coupling efficiency (δ) for different parameter values and configurations.



Modes given by

$$Z_{\pm} = \frac{-i\delta(1+Z_2Z_3)\pm(1-\delta^2)\sqrt{Z_2Z_3}}{\delta^2+Z_2Z_3}$$

$$Z = e^{iqL}$$

$$Z_2 = r_2 e^{2iq_2 L_2}$$

$$Z_3 = r_3 e^{2iq_3L_3}$$









ACPHOM: Active Photonic Molecules











ACKNOWLEDGMENTS

- SalvadorBalle
- JulienJavaloyes AntonioPérez-Serrano
- RobertaZambrini,PereColet,MarcSorel, SandorFurst, GaborMezosi, MichaelStrain, GuidoGiuliani, RiccardoMiglierina, Andrea Trita, IlariaCristiani, FrancescaBragheri, SilvanoDonati, SiyuanYu, GououiYuan, BeiLi, ZouranWang, JanDanckaert, GuyVanDerSande, LendertGelens, GuyVerschaffelt, StefanoBeri, MichaelWale, DanYanson, JorgeCastro, JeanBuus, AngelaThreinhardt, MarkusKorn.





SEMICONDUCTOR RING LASER DYNAMICS

- Modal Properties 1/ •
- <u>TW-modelling</u> $\sqrt{}$ ۲
- <u>Directional switching</u> $\sqrt{}$ •
- **Noise properties** ٠ Langevin formulation, noise spectra $\sqrt{}$ Mode hopping $\sqrt{}$
- **Applications** •

۲

Inertial rotation sensing $\sqrt{}$ Hardware Random Number Generation

New structures **Snail laser** Active Photonic Molecules

