

# CONTROL OF SPATIAL QUANTUM FLUCTUATIONS USING PHOTONIC CRYSTALS

MARIA MORENO, DAMIA GOMILA and ROBERTA ZAMBRINI

funding by:  
'Quantum light in microdevices'  
'Quantum effects in complex systems'

 IFISC

## ***OUTLINE***

### ***1. INTRODUCTION:***

- QUANTUM STATES OF LIGHT***
- NON-LINEAR SYSTEMS***
- PHOTONIC CRYSTALS***

### ***2. DESCRIPTION OF THE MODEL AND METHODOLOGY***

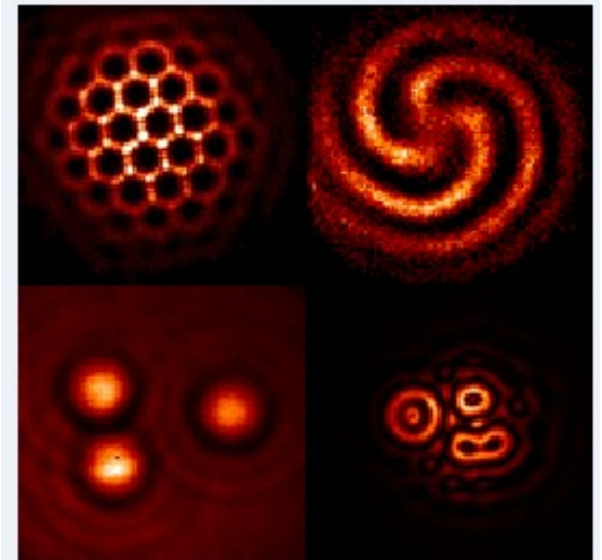
### ***3. MAIN RESULTS***

### ***4. CONCLUSIONS AND OUTLOOK***



# NON-LINEAR SYSTEMS

## SPONTANEOUS PATTERN FORMATION



<http://www.uni-muenster.de/Physik>

### HIGHER ORDER POLARIZATION:

RESPONSIBLE OF NON-LINEARITY BY COUPLING DIFFERENT WAVES

$$P = \chi E + \chi^{(2)} E^{(2)} + \chi^{(3)} E^{(3)} \dots$$

Lugiato, L.A. & Lefever, R PRL **58** (1984)

# PHOTONIC CRYSTALS

movement of  $e^-$  in a semiconductor

PERIODICITY of CRYSTAL:

BAND-GAP for  $e^-$

light in a photonic crystal

PERIODICITY of  $n$ :

BAND-GAP for photons

## Photonic Crystals in Nature

*Morpho rhetenor* butterfly

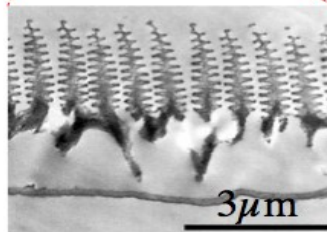


<http://ab-initio.mit.edu/index.html>

<http://www.bugguy012002.com/MORPHIDAE.html>

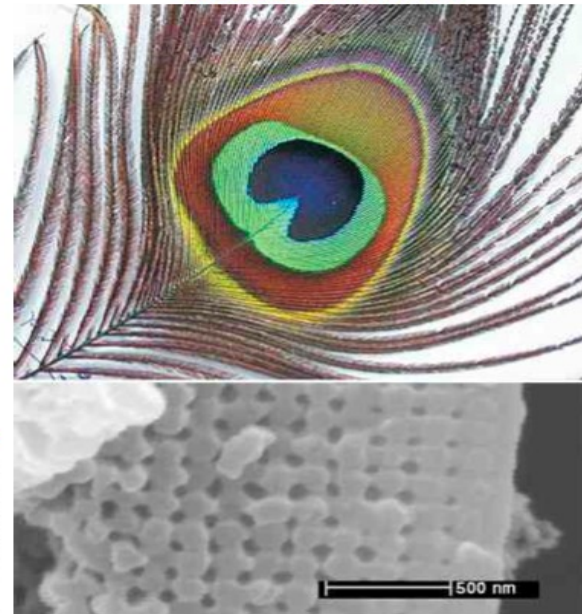
wing scale:

[ P. Vukosic *et al.*,  
*Proc. Roy. Soc: Bio. Sci.* **266**, 1403  
(1999) ]



[ also: B. Gralak *et al.*, *Opt. Express* **9**, 567 (2001) ]

Peacock feather



[ J. Zi *et al.*, *Proc. Nat. Acad. Sci. USA*,  
**100**, 12576 (2003) ]

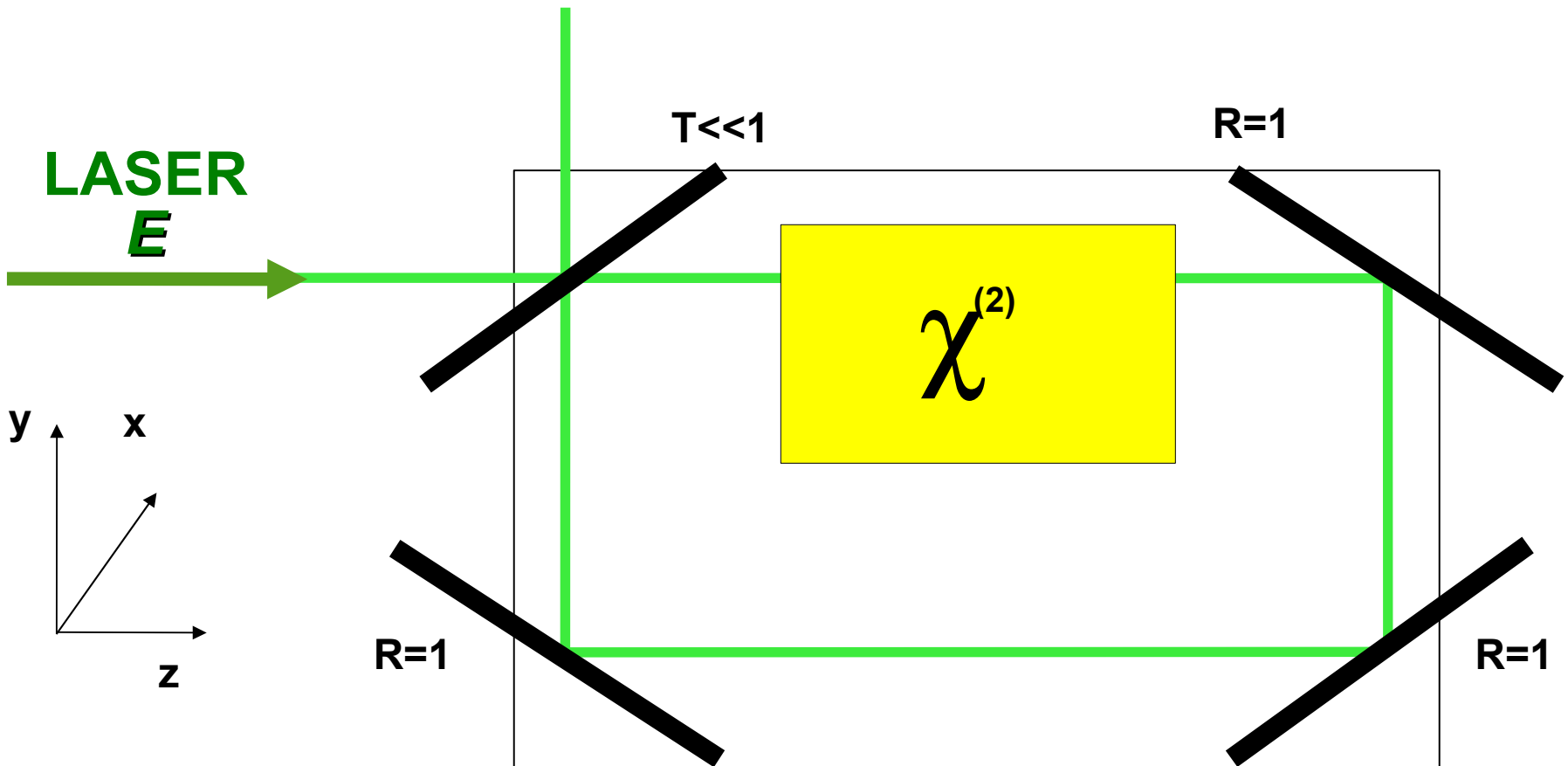
[ figs: Blau, *Physics Today* **57**, 18 (2004) ]

**CAN WE CONTROL SPATIAL QUANTUM  
FLUCTUATIONS AND CORRELATIONS?**

**WE CONSIDER A DEGENERATED  
TYPE I OPO EMBEDDING A  
PHOTONIC CRYSTAL**

# DESCRIPTION OF THE MODEL

## Optical Parametric Oscillator



# DESCRIPTION OF THE MODEL

## Degenerated TYPE I Optical Parametric Oscillator

**PARAMETRIC DOWN CONVERSION**

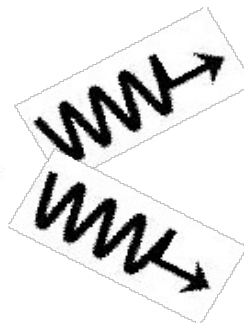
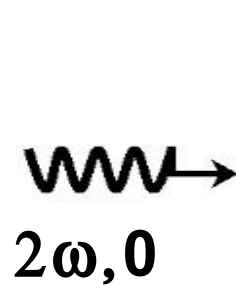
$$\omega_{pump} \longleftrightarrow \omega_{signal} + \omega_{idler}$$

**DEGENERATED**

$$2\omega \longleftrightarrow \omega + \omega$$

$$\hat{H}_{int} \propto \hat{A}_{pump}(x, y) \hat{A}_{signal}^{\dagger 2}(x, y)$$

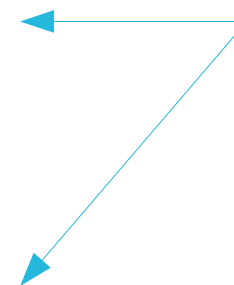
**PUMP:**  
ordinary  
polarization



$\omega, k$

$\omega, -k$

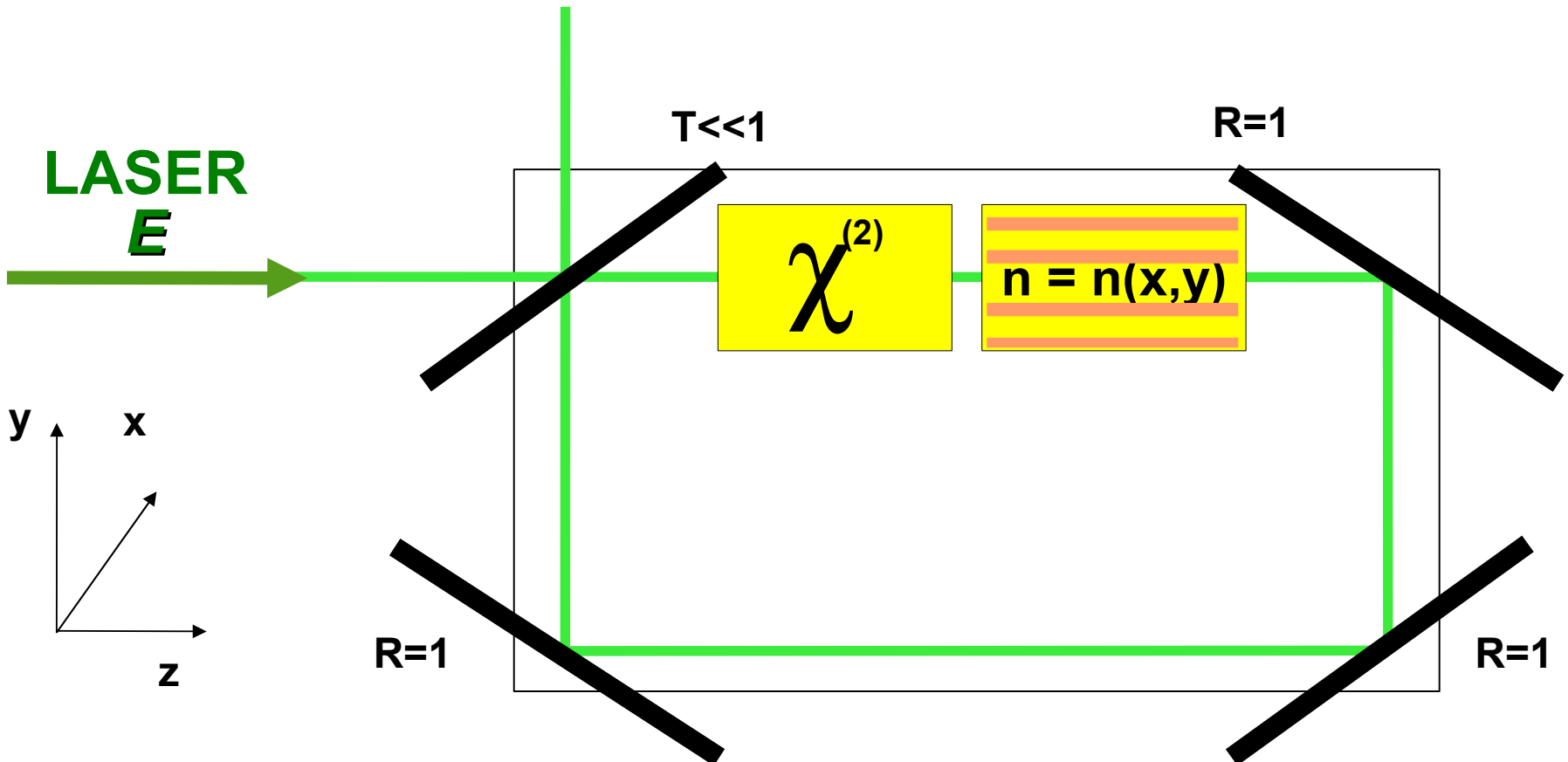
**SIGNAL and IDLER:**  
extraordinary  
polarization





# DESCRIPTION OF THE MODEL

## Degenerated TYPE I Optical Parametric Oscillator with Photonic Crystal



$$\Delta_0 \rightarrow \Delta_0 + I_0 \sin(k_{PC} x) \quad \text{and} \quad \Delta_1 \rightarrow \Delta_1 + I_1 \sin(k_{PC} x)$$

# METHODOLOGY

## REPRESENTATIONS OF QUANTUM STATES OF LIGHT

from bosonic operators  $\hat{A}_i, \hat{A}_i^\dagger$  to phase space  $\alpha_i, \alpha_i^*$

**MASTER EQUATION** for  
an open system

$$\frac{\partial \hat{\rho}}{\partial t} = \frac{1}{i\hbar} [\hat{H}, \hat{\rho}] + \hat{\Lambda} \hat{\rho}.$$

$$\hat{H} = f(\hat{A}_i, \hat{A}_i^\dagger, \dots)$$

depending on ordering

normal  $\langle \hat{A}^\dagger \hat{A} \rangle \leftrightarrow \langle \alpha^* \alpha \rangle_P$

anti-normal  $\langle \hat{A} \hat{A}^\dagger \rangle \leftrightarrow \langle \alpha^* \alpha \rangle_Q$

**FOKKER-PLANCK**  
EQUATION  
in Q  
under some  
approximations  
(non-linear system)

**LANGEVIN**  
EQUATION

**STOCHASTIC**  
DIFFERENTIAL  
EQUATION WITH  
QUANTUM NOISE  
SUITABLE TO  
NUMERICAL  
SIMULATIONS

# DESCRIPTION OF THE MODEL AND METHODOLOGY

## KEY CONCEPTS

$E > E_{\text{threshold}}$



**SIGNAL EMISSION**

# DESCRIPTION OF THE MODEL AND METHODOLOGY

## KEY CONCEPTS

$$E > E_{\text{threshold}}$$



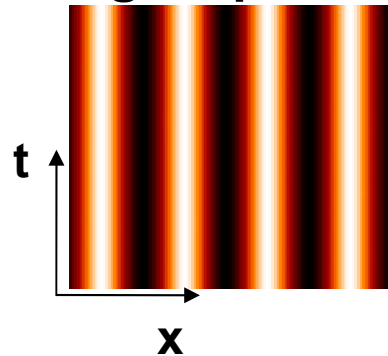
**SIGNAL EMISSION**

spatial dependence

$$\Delta_1 < 0$$



signal pattern



$$k_c = \frac{1}{\lambda_c} = \sqrt{\frac{-\Delta_1}{2}}$$

# DESCRIPTION OF THE MODEL AND METHODOLOGY

## KEY CONCEPTS

$$E > E_{\text{threshold}}$$



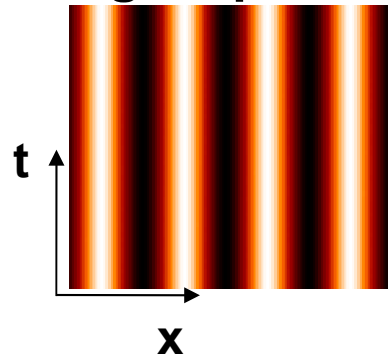
**SIGNAL EMISSION**

spatial dependence

$$\Delta_1 < 0$$



signal pattern



$$k_c = \frac{1}{\lambda_c} = \sqrt{\frac{-\Delta_1}{2}}$$

## EMBEDDING THE PHOTONIC CRYSTAL

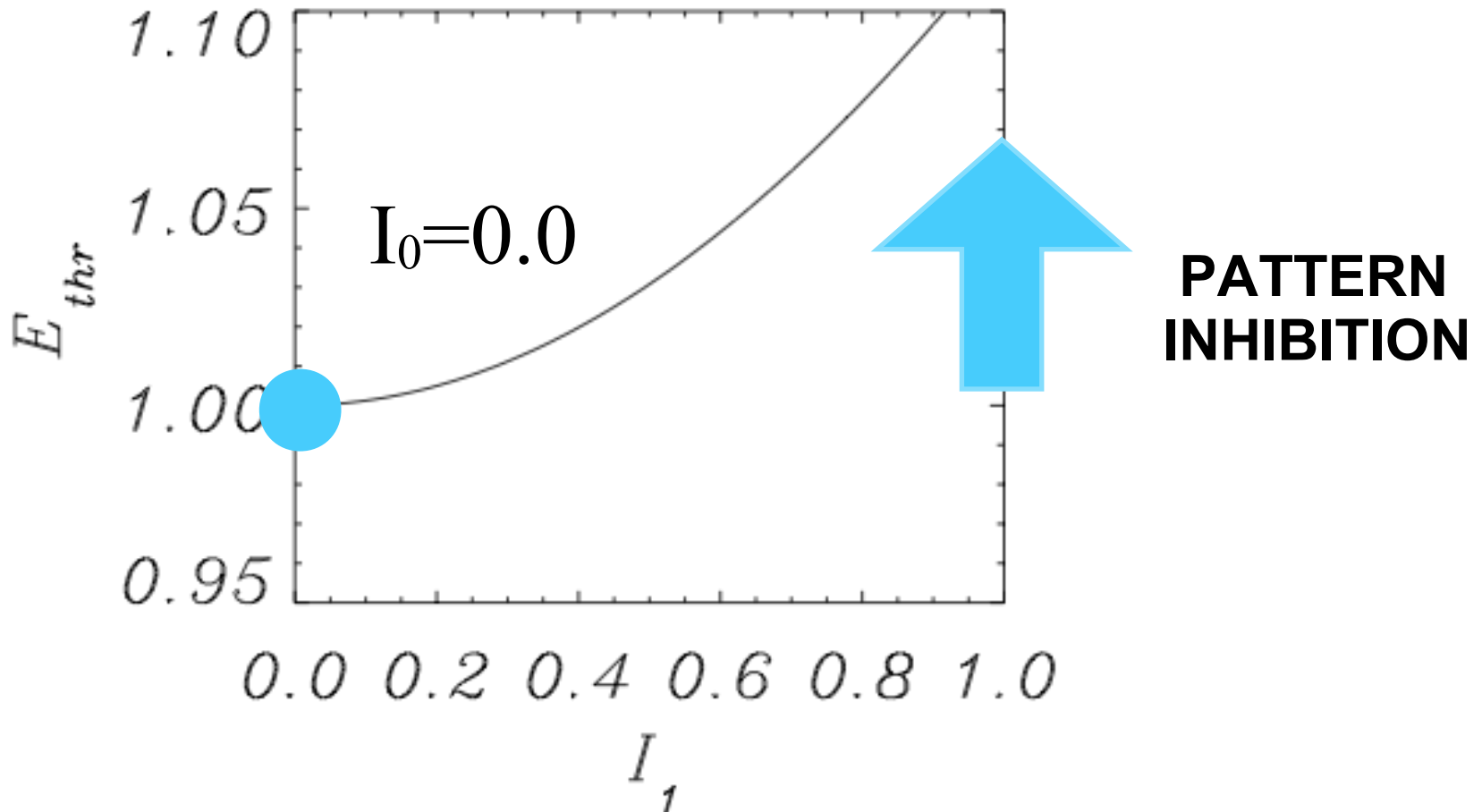
$$\left\{ \begin{array}{l} \text{modulation} \\ \text{amplitudes: } I_0, I_1 \\ \text{modulation} \\ \text{wavelength: } \lambda_p \propto \lambda_c \end{array} \right.$$



**RICH PHENOMENOLOGY**

# MAIN RESULTS

## CONTROL OF INSTABILITIES THRESHOLD WITH PHOTONIC CRYSTALS



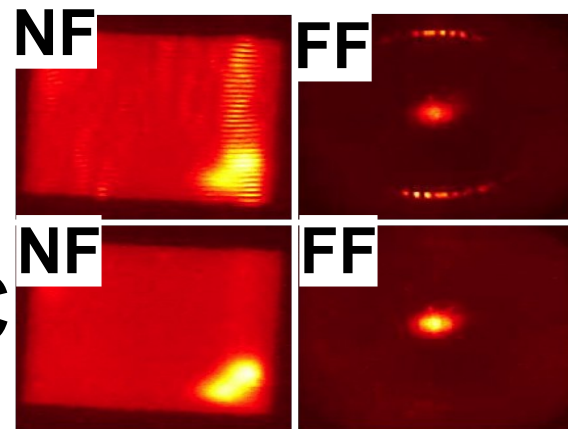
APPLIED PHYSICS LETTERS 93, 151114 (2008)

# Control of broad-area vertical-cavity surface emitting laser emission by optically induced photonic crystals

Bernd Terhalle,<sup>1,a)</sup> Neal Radwell,<sup>2</sup> Patrick Rose,<sup>1</sup> Cornelia Denz,<sup>1</sup> and Thorsten Ackemann<sup>2</sup>  
<sup>1</sup>Institut für Angewandte Physik and Center for Nonlinear Science (CeNoS), Westfälische Wilhelms-Universität Münster, Corrensstraße 2/4, 48149 Münster, Germany  
<sup>2</sup>SUPA and Department of Physics, University of Strathclyde, Glasgow, G40NG Scotland, United Kingdom

no PC

with PC



# Experimental control of pattern formation by photonic lattices

November 1, 2008 / Vol. 33, No. 21 / OPTICS LETTERS

N. Marsal,<sup>1,\*</sup> D. Wolfersberger,<sup>1</sup> M. Sciamanna,<sup>1</sup> G. Montemezzani,<sup>1</sup> and D. N. Neshev<sup>2</sup>

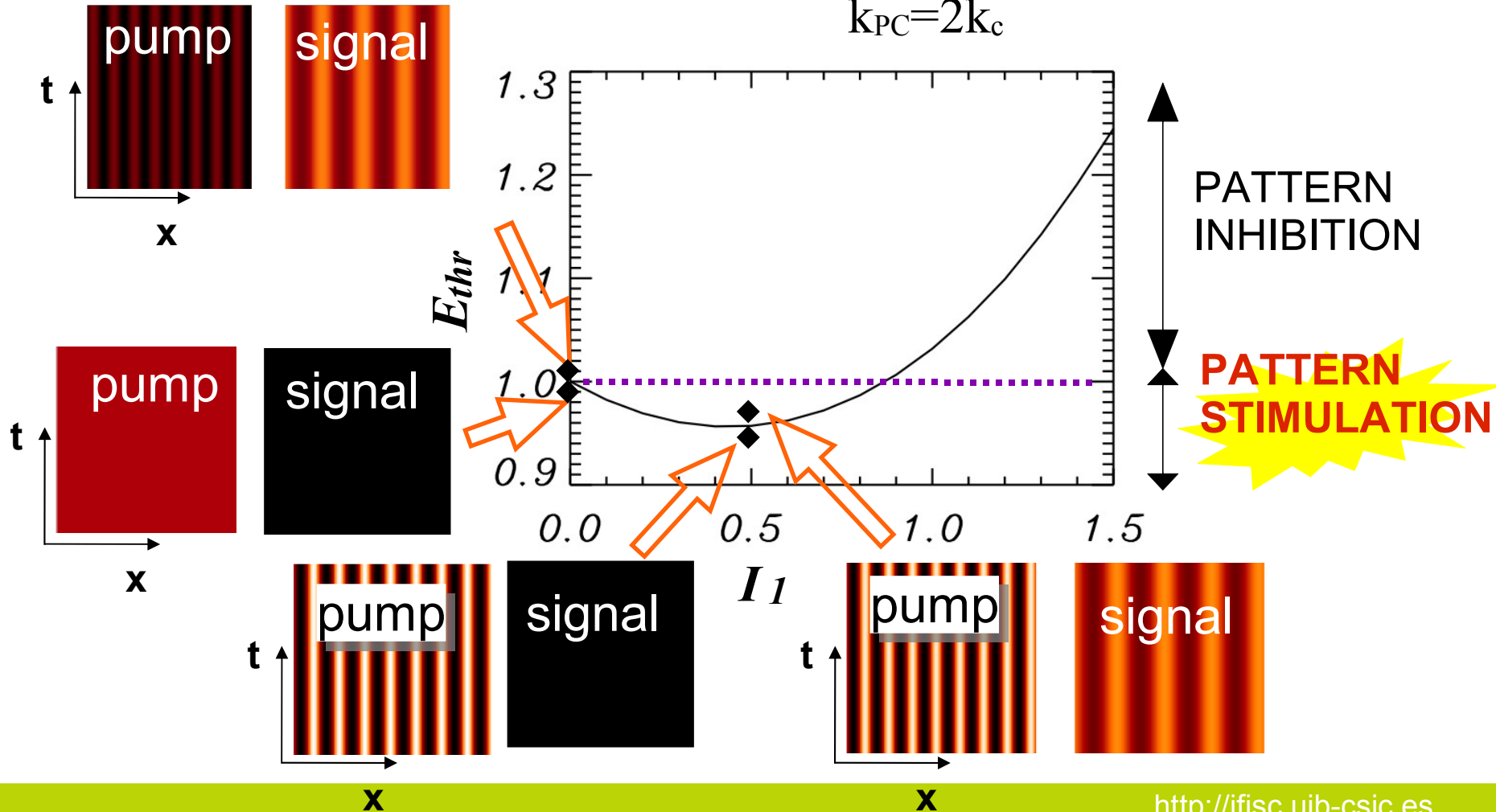
<sup>1</sup>Laboratoire Matériaux Optiques, Photoniques et Systèmes (LMOPS), CNRS UMR 7132, Unité de Recherche Commune à Supélec et Université Paul Verlaine de Metz, France

<sup>2</sup>Nonlinear Physics Centre, Research School of Physical Sciences and Engineering, Australian National University, Canberra, 0200 ACT, Australia

# MAIN RESULTS

## CONTROL OF PATTERN FORMATION THRESHOLD

MORE GENERAL CASE:  $I_0=I_1$ ,  
 $k_{PC}=2k_c$



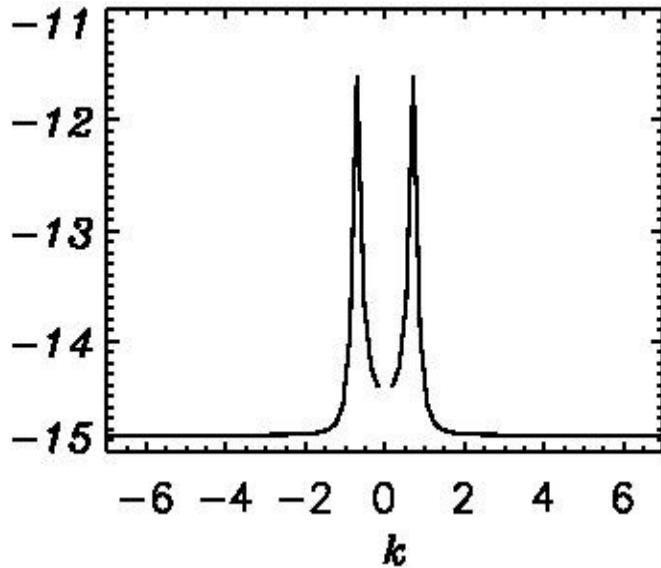


# MAIN RESULTS

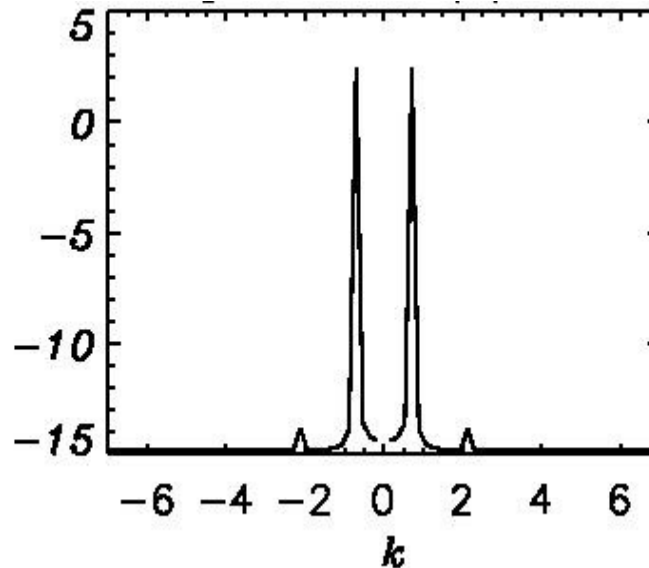
## QUANTUM CORRELATIONS

$\log \langle I_{\text{signal}} \rangle$  without photonic crystal

FAR FIELD



Below threshold



Above threshold

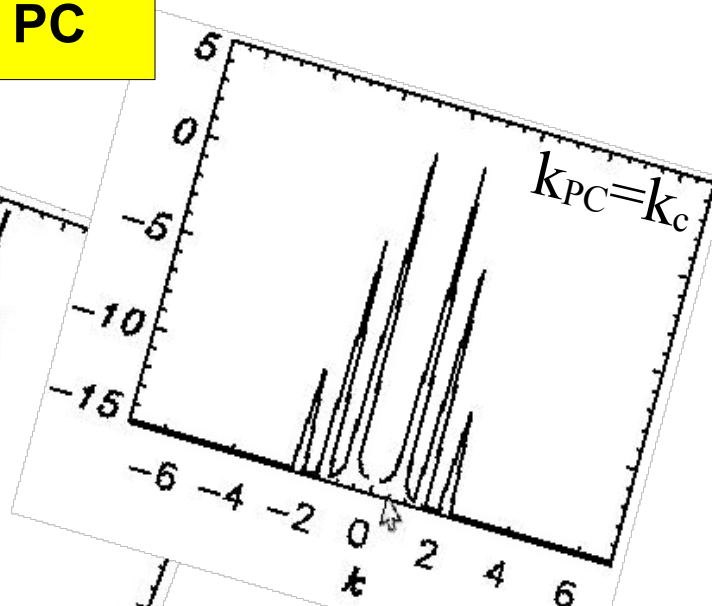
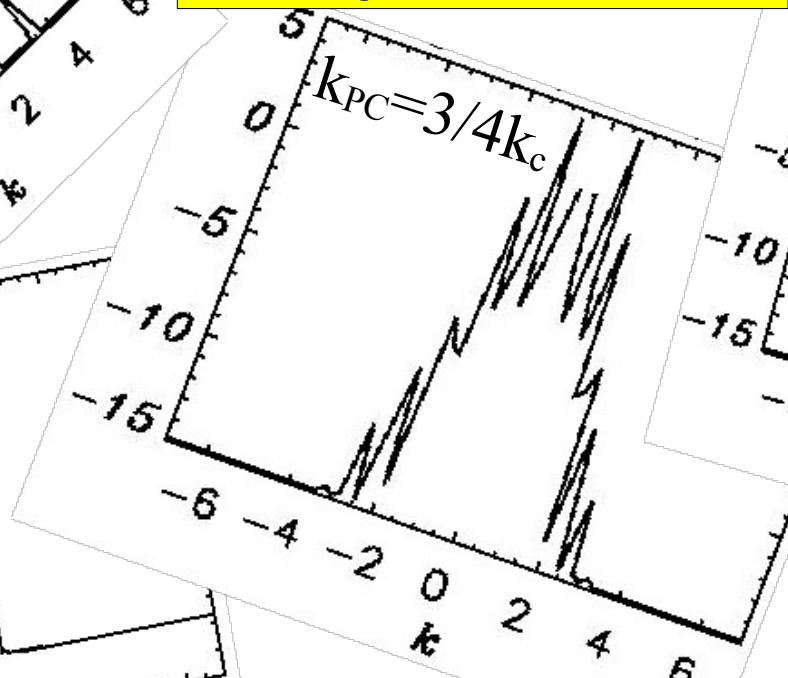
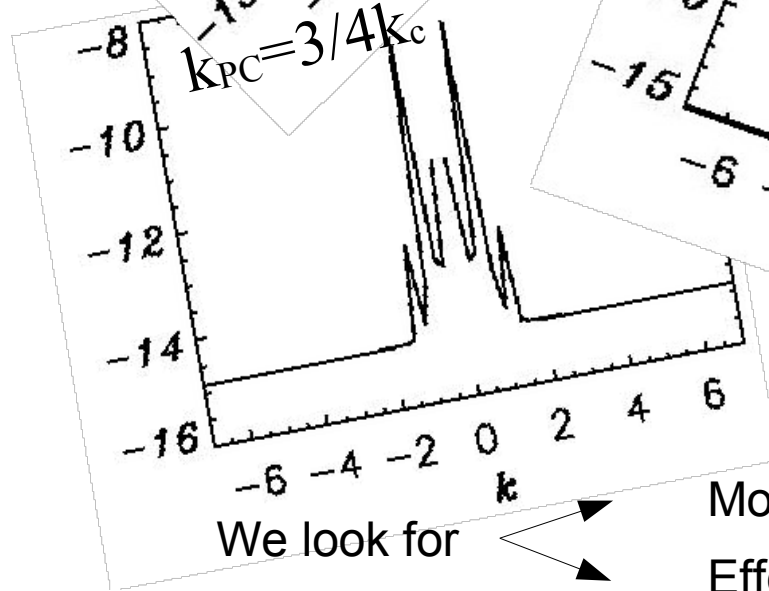
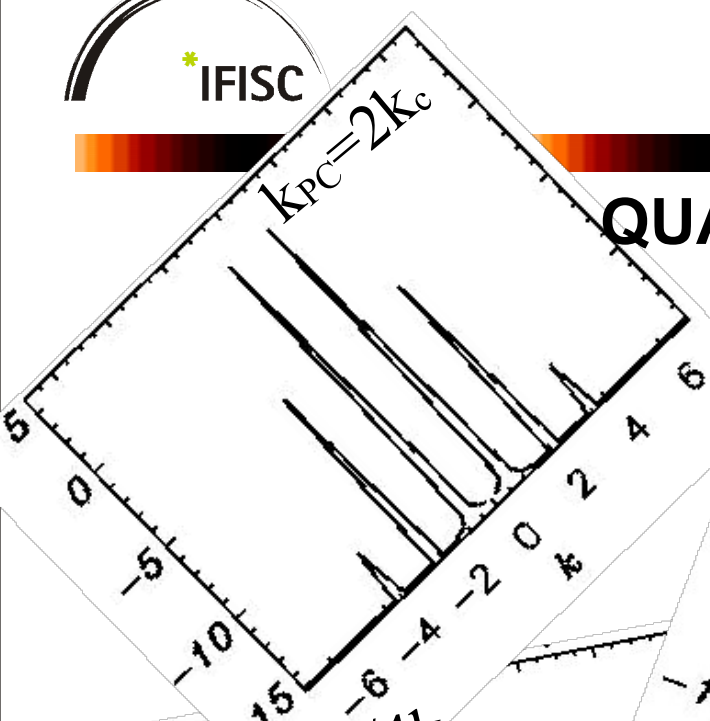
EPR  
entanglement  
between  $k_c$  and  $-k_c$



# MAIN RESULTS

## QUANTUM CORRELATIONS

$\log \langle I_{\text{signal}} \rangle$  WITH PC



MULTIMODE SPATIAL SPECTRUM

SQUEEZING between  $k_c$  and  $-k_c$  GENERALLY PRESERVED

We look for

- More complex superposition of modes
- Effects of spatial locking

# CONCLUSIONS

- Photonic Crystals in OPOs allow to tune the parametric threshold
- Squeezing between  $k_c$  and  $-k_c$  generally preserved when embedding Photonic Crystals

## IN PROGRESS

- Explore role of wavelength and amplitudes of PC
- Two modes squeezing and EPR entanglement

**THANK YOU!**