

Einstein Refrigerator

Patent number US1781541 • November 11, 1930

Albert Einstein
Leo Szilard

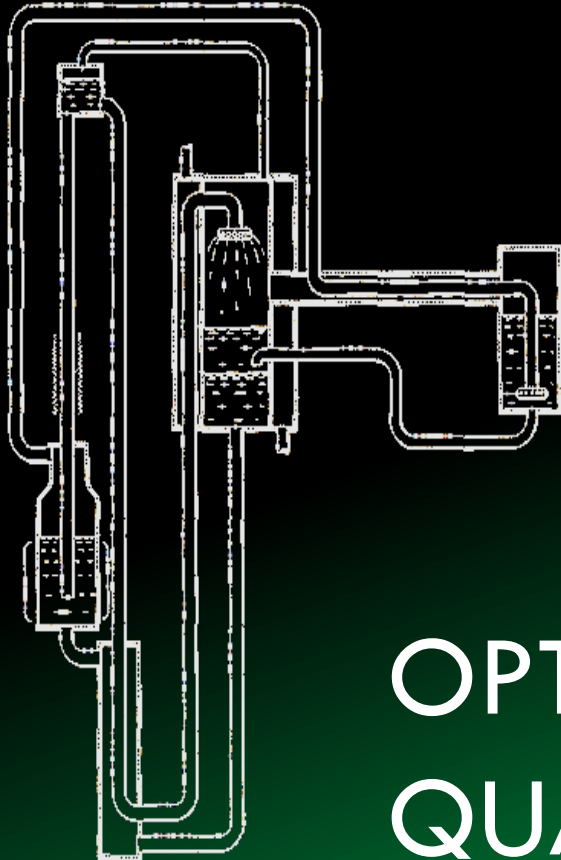


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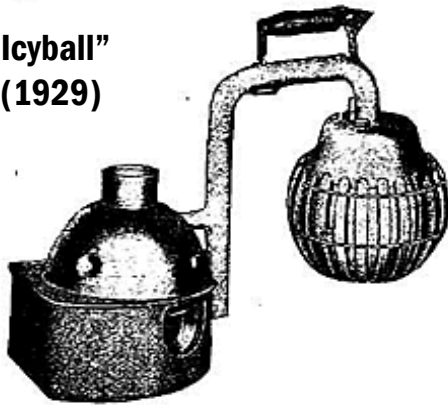
OPTIMAL PERFORMANCE OF QUANTUM REFRIGERATORS

2nd Quantum Thermodynamics
Conference, Palma, April 2015

L.A. Correa, J.P. Palao, D. Alonso, Gerardo Adesso

ABSORPTION REFRIGERATORS

“Icyball”
(1929)



EASY TO HANDLE

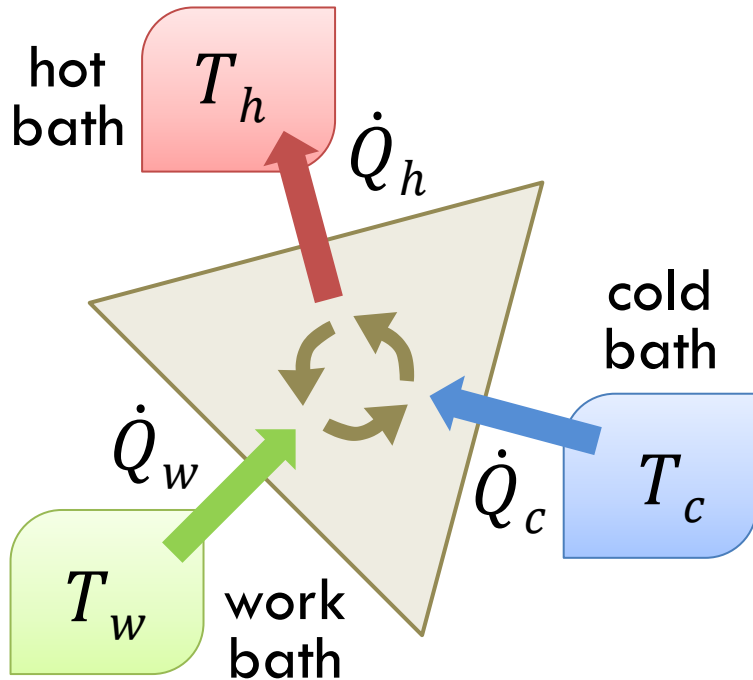
The complete unit which cools after being “charged” by heating, weighs 35 pounds

- Autonomous machines that cool by absorbing heat with no power source
- Used on caravans or in rural areas where main electricity line is missing
- However quite inefficient compared to conventional compression fridges



- *How to understand and possibly improve their optimal performance?*
- *We need to model elementary (quantum) instances of these devices*

THE TRICYCLE



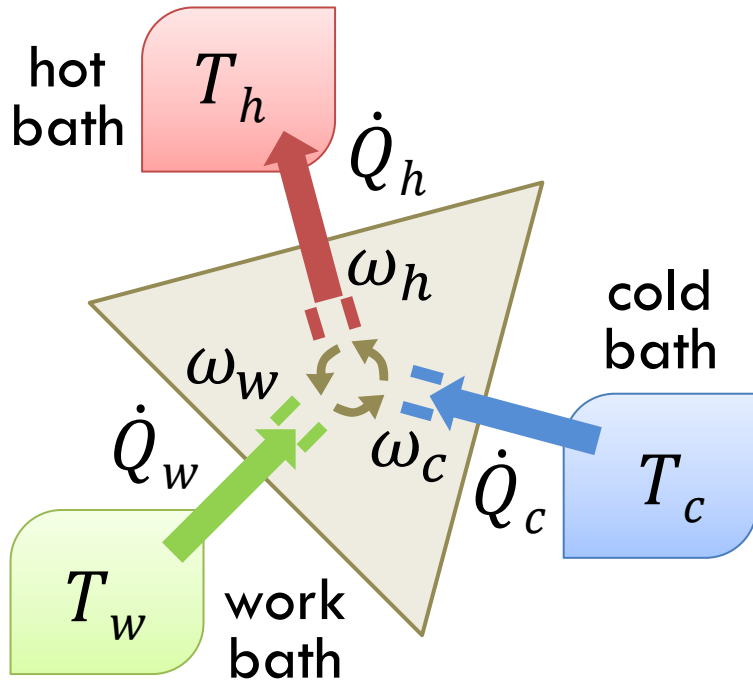
- Prototype of any generic continuous thermal machine
- Includes absorption and power-driven refrigerators ($T_w \rightarrow \infty$), heat engines and heat converters
- Three reservoirs: $T_w > T_h > T_c$
- Heat currents: \dot{Q}_α ($\alpha = w, h, c$)
- **Thermodynamics 101**

1. $\sum_\alpha \dot{Q}_\alpha = 0$ [1st law]

2. $\sum_\alpha \frac{\dot{Q}_\alpha}{T_\alpha} = -\dot{S} \leq 0$ [2nd law]

□ Andresen, Salamon & Berry,
J. Chem. Phys. **66** (1977)

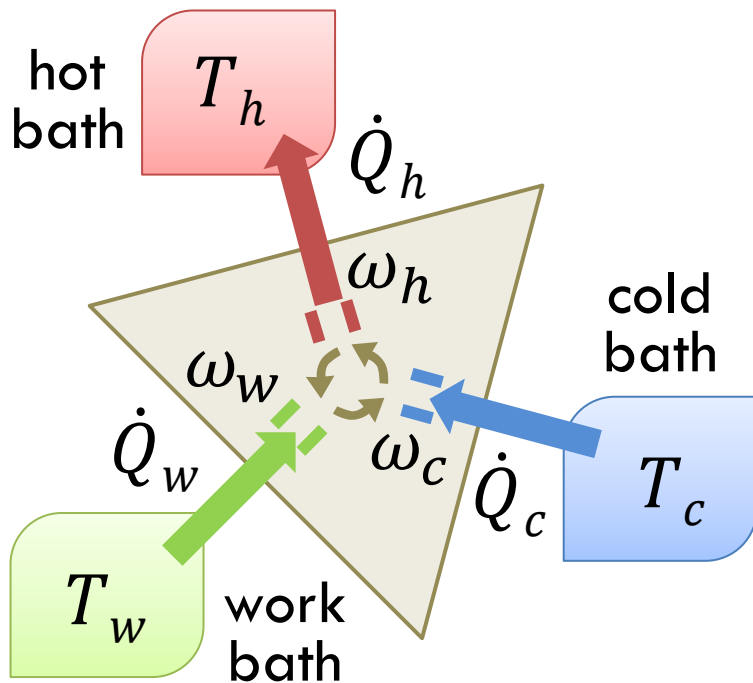
THE QUANTUM TRICYCLE



- Selective coupling to the baths via filtered frequencies ω_α
- In absence of friction, heat leaks, etc.: single stationary rate J
- Heat currents: $\dot{Q}_\alpha = \pm \omega_\alpha J$
- **Thermodynamics 101**
 1. $\sum_\alpha \dot{Q}_\alpha = 0$ [1st law]
 2. $\sum_\alpha \frac{\dot{Q}_\alpha}{T_\alpha} = -\dot{S} \leq 0$ [2nd law]
- Resonance: $\omega_w = \omega_h - \omega_c$

□ Kosloff & Levy, *Annu. Rev. Phys. Chem.* **65** (2014)

QUANTUM ABSORPTION FRIDGE

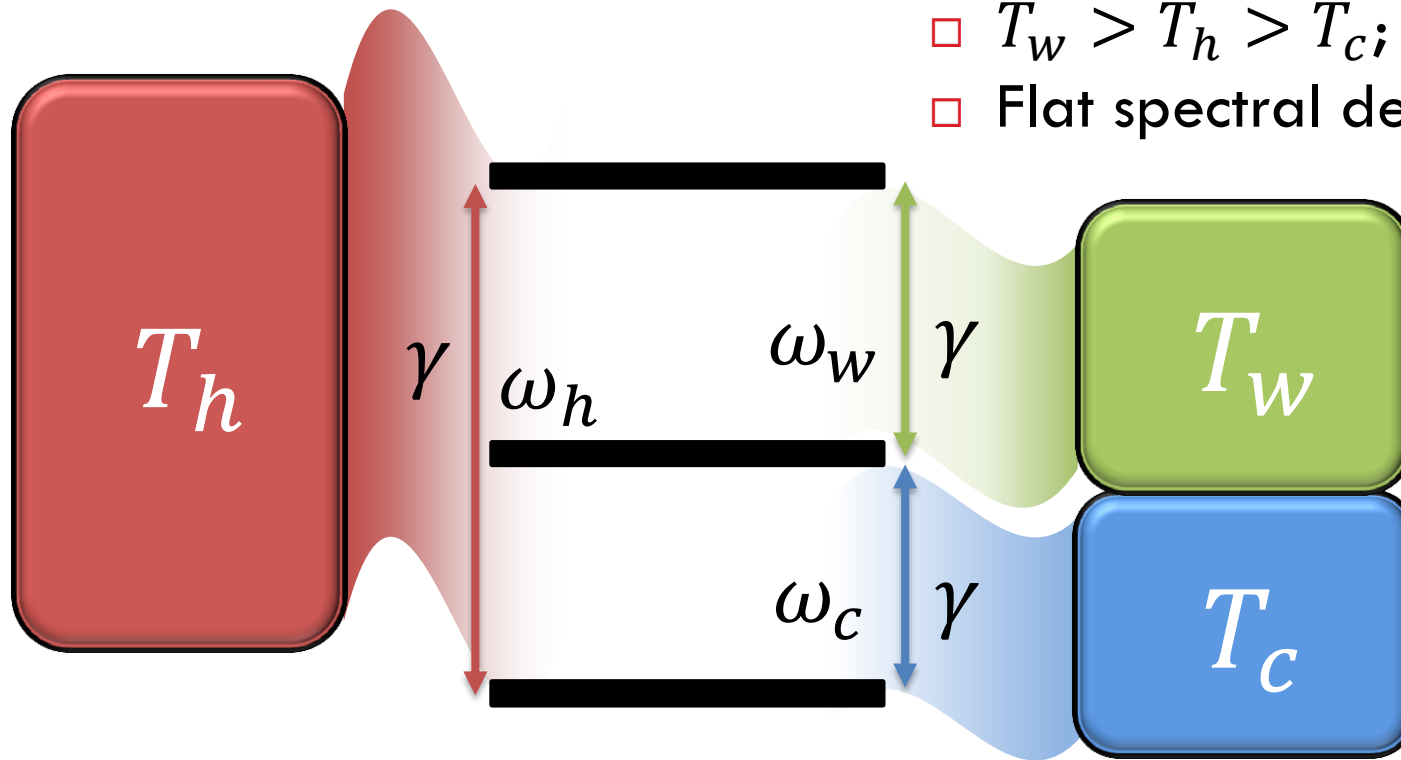


- $T_w > T_h > T_c$; $\omega_w = \omega_h - \omega_c$
- Cooling window:

$$\omega_c \leq \omega_c^{\max} = \frac{(T_w - T_h)T_c}{(T_w - T_c)T_h} \omega_h$$
- Cooling power: \dot{Q}_c
- Coefficient of performance (COP): $\varepsilon = \frac{\dot{Q}_c}{\dot{Q}_w} \leq \varepsilon_C$
- Carnot COP: $\varepsilon_C = \frac{1 - \frac{T_h}{T_w}}{\frac{T_h}{T_c} - 1}$
- For reversible machines, $\varepsilon \rightarrow \varepsilon_C$ at vanishing cooling power

□ Kosloff & Levy, *Annu. Rev. Phys. Chem.* **65** (2014)

QUANTUM ABSORPTION FRIDGE/1



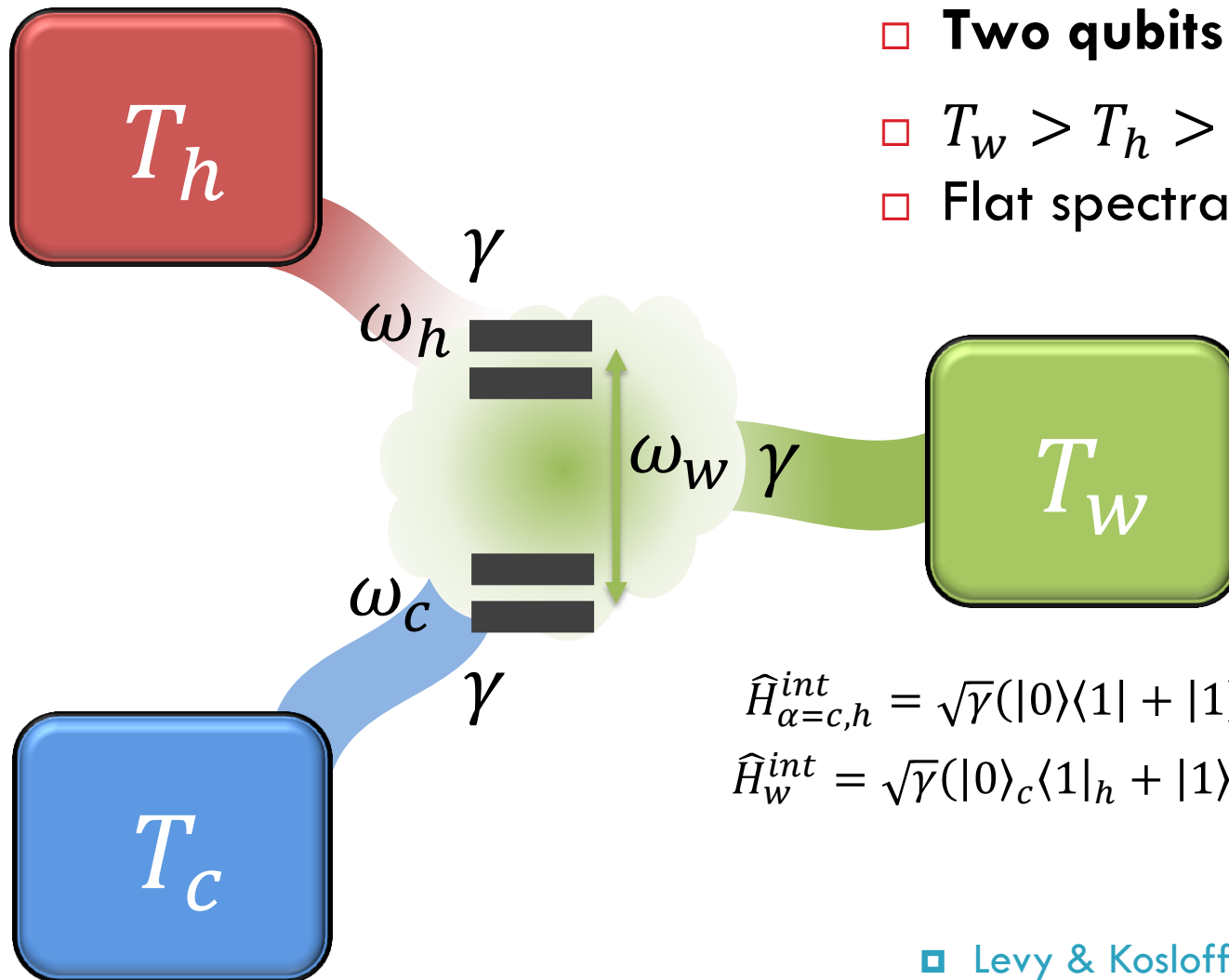
- **One qutrit** (3-level maser)
- $T_w > T_h > T_c$; $\omega_w = \omega_h - \omega_c$
- Flat spectral densities

$$\hat{H}_\alpha^{int} = \sqrt{\gamma}(|0\rangle\langle 1| + |1\rangle\langle 0|)_\alpha \otimes \hat{B}_\alpha$$

$$\hat{B}_\alpha = \sum_\mu k_{\alpha,\mu} \sqrt{\omega_\mu} (\hat{b}_{\alpha,\mu} + \hat{b}_{\alpha,\mu}^\dagger)$$

- Geusic, Bios & Scovil, *Phys. Rev. Lett.* **2** (1959)
- Palao, Kosloff & Gordon, *Phys. Rev. E* **64** (2001)

QUANTUM ABSORPTION FRIDGE/2

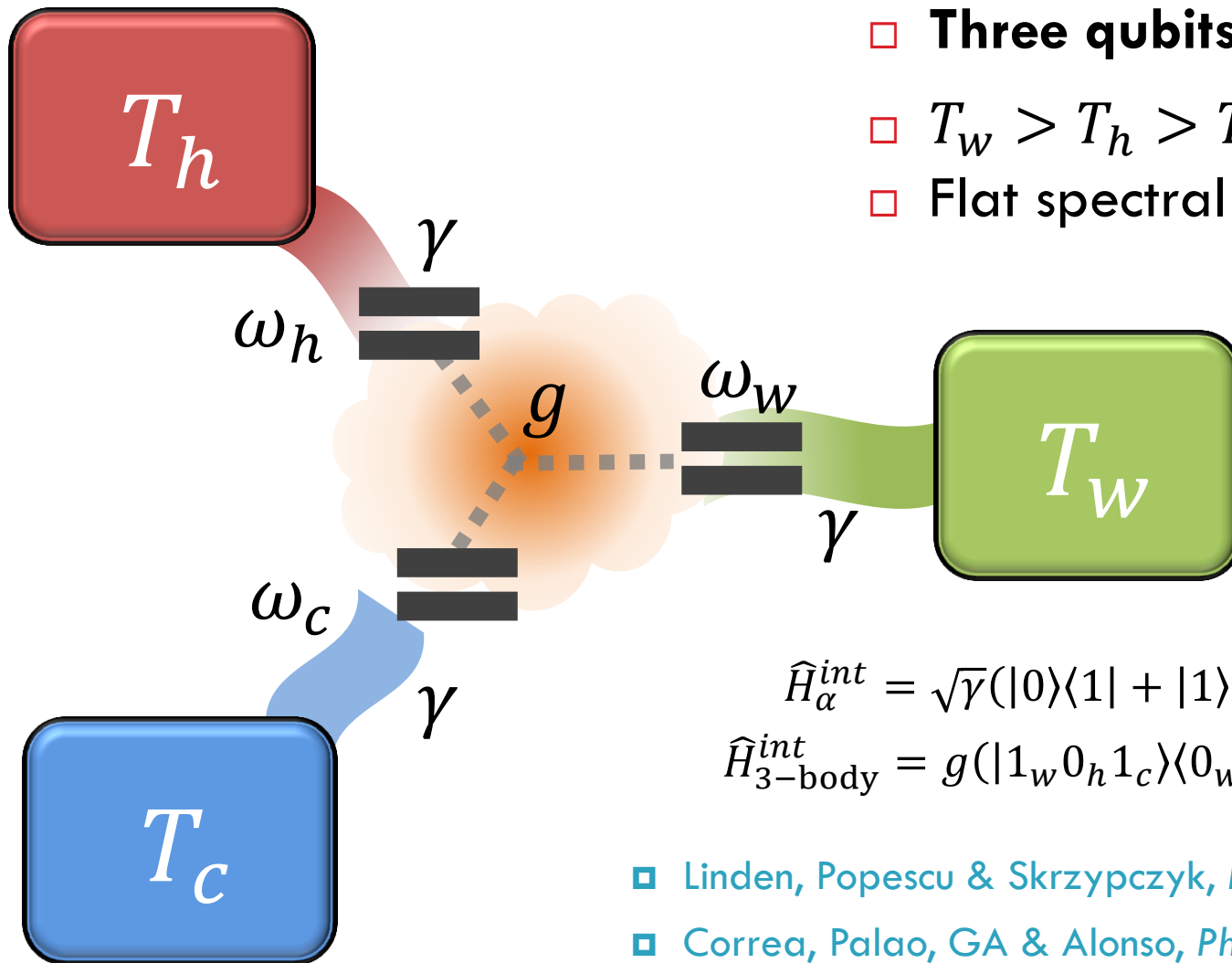


- **Two qubits**
- $T_w > T_h > T_c$; $\omega_w = \omega_h - \omega_c$
- Flat spectral densities

$$\hat{H}_{\alpha=c,h}^{int} = \sqrt{\gamma}(|0\rangle\langle 1| + |1\rangle\langle 0|)_{\alpha} \otimes \hat{B}_{\alpha}$$

$$\hat{H}_w^{int} = \sqrt{\gamma}(|0\rangle_c\langle 1|_h + |1\rangle_c\langle 0|_h) \otimes \hat{B}_w$$

QUANTUM ABSORPTION FRIDGE/3

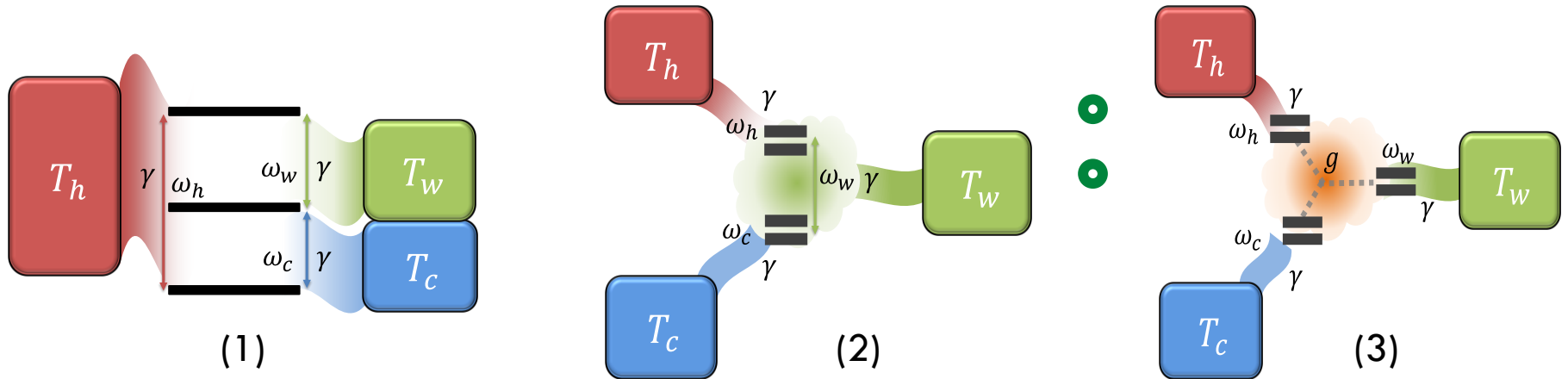


- **Three qubits**
- $T_w > T_h > T_c$; $\omega_w = \omega_h - \omega_c$
- Flat spectral densities

$$\hat{H}_\alpha^{int} = \sqrt{\gamma}(|0\rangle\langle 1| + |1\rangle\langle 0|)_\alpha \otimes \hat{B}_\alpha$$
$$\hat{H}_{3\text{-body}}^{int} = g(|1_w 0_h 1_c\rangle\langle 0_w 1_h 0_c| + h.c.)$$

- Linden, Popescu & Skrzypczyk, *Phys. Rev. Lett.* **105** (2010)
- Correa, Palao, GA & Alonso, *Phys. Rev. E* **87** (2013)

QUANTUM ABSORPTION FRIDGES

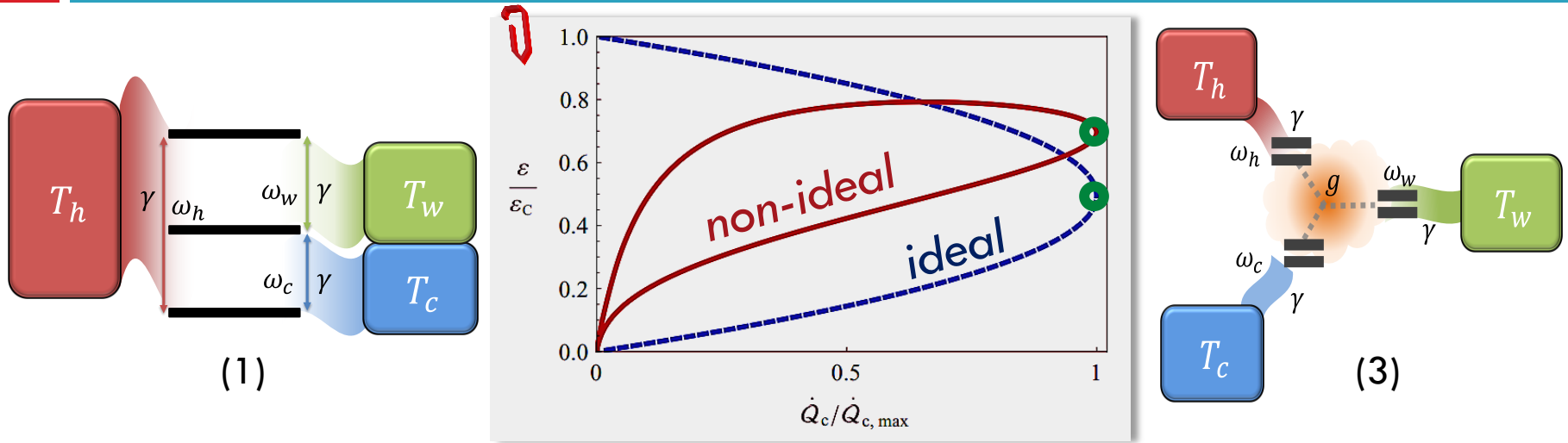


□ Models (1) and (2) are ideal reversible devices which can attain the Carnot COP

□ Model (3) is non-ideal due to the delocalised dissipation effects

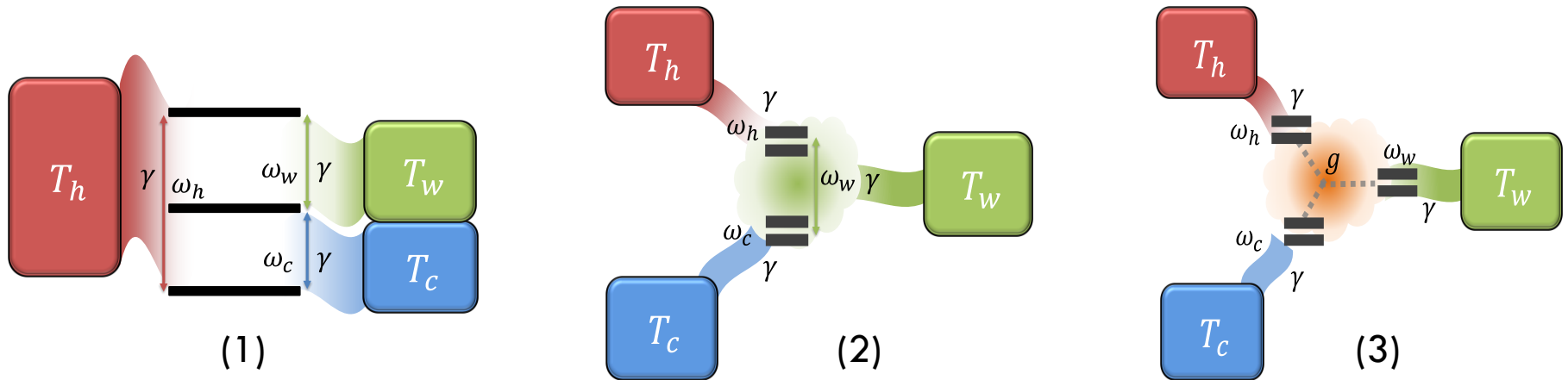
- Other models: Mari & Eisert, *Phys. Rev. Lett.* **108** (2012); Boukobza & Ritsch, *Phys. Rev. A* **87** (2013); Gelbwaser-Klimovsky, Alicki & Kurizki, *Phys. Rev. E* **90** (2014); Silva, Skrzypczyk & Brunner, *arXiv* (2015)

QUANTUM ABSORPTION FRIDGES



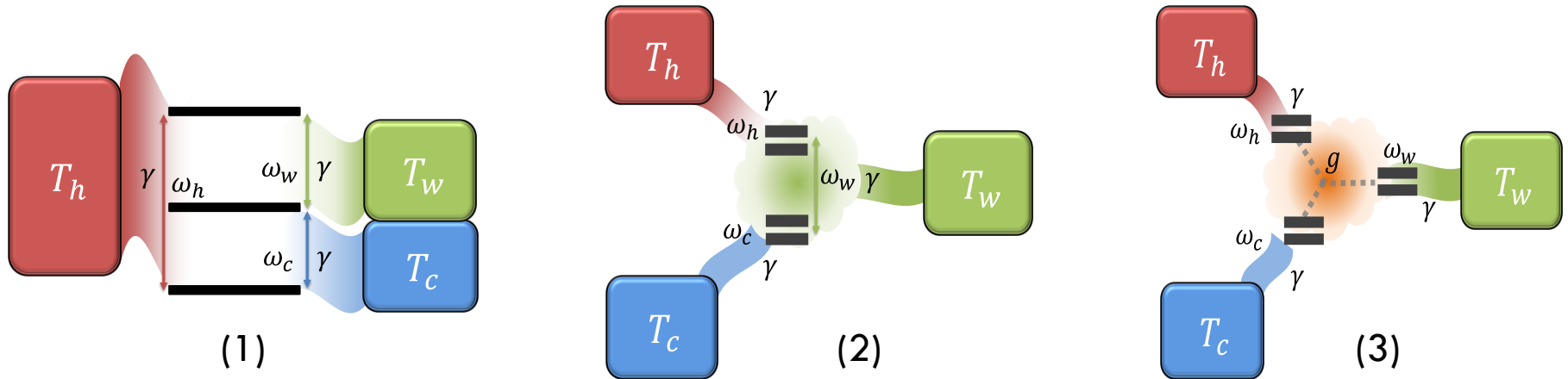
- Models (1) and (2) are ideal reversible devices which can attain the Carnot COP
- Model (3) is non-ideal due to the delocalised dissipation effects
- *We can focus on the optimisation of a more sensible figure of merit: COP ε_* at maximum cooling power*

COP AT MAXIMUM POWER



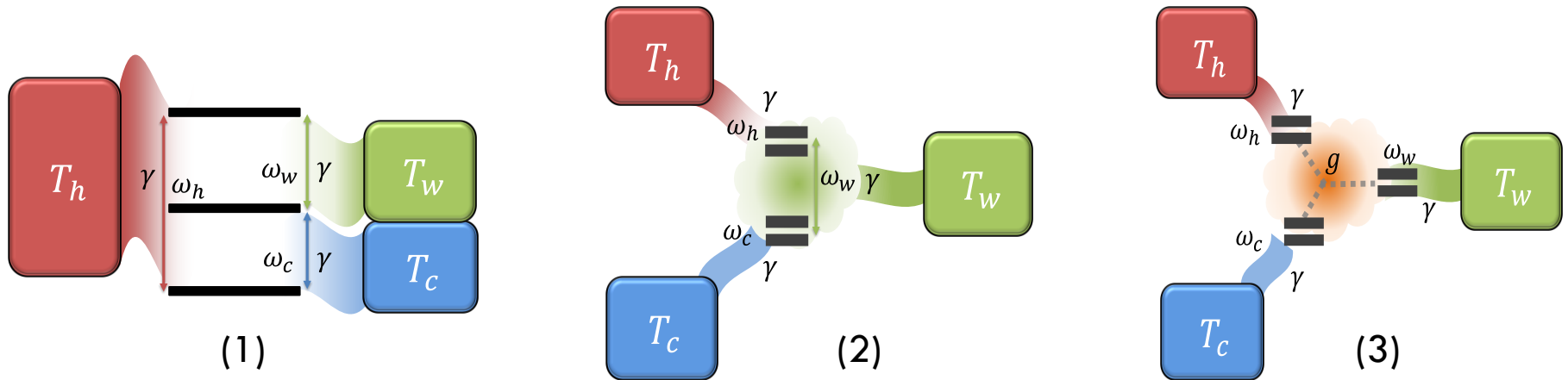
- Weak coupling to the baths: $\gamma \ll \{k_B T_\alpha, \hbar \omega_\alpha, g\}$
- Born, Markov, and rotating wave approximations
- Master equation: $\dot{\rho}(t) = (\mathcal{L}_W + \mathcal{L}_h + \mathcal{L}_c)\rho(t)$
- Lindblad dissipators: $\mathcal{L}_\alpha = \sum_\omega (\alpha \omega^{d_\alpha}) \dots$

COP AT MAXIMUM POWER



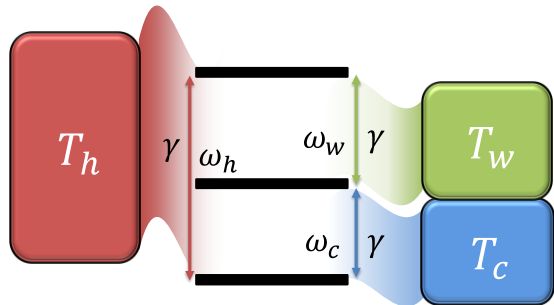
$$\varepsilon_* \leq \frac{d_c}{d_c + 1} \varepsilon_C$$

PERFORMANCE BOUND: $\varepsilon_* \leq \frac{d_c}{d_c+1} \varepsilon_C$

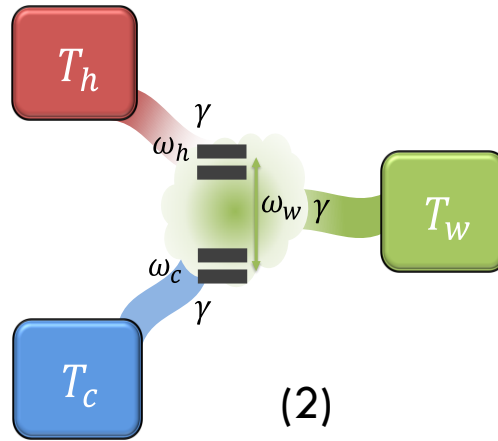


- ❑ Rigorously proven for models (1) and (2)
- ❑ Valid for any multistage refrigerator built upon (1)
- ❑ Verified numerically for model (3) as well
- ❑ Tight: saturated for $T_c \ll T_h$, $\omega_w \ll T_{w,h}$ (i.e. $\varepsilon_C \rightarrow 0$)

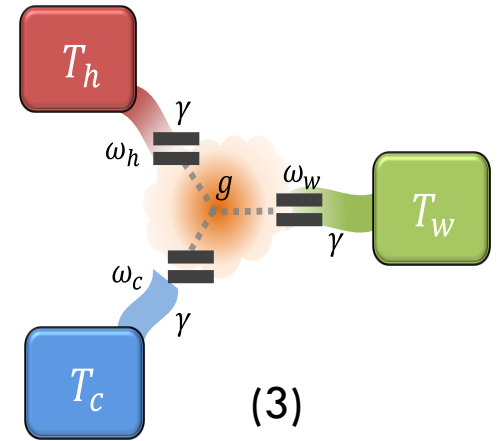
PERFORMANCE BOUND: $\varepsilon_* \leq \frac{d_c}{d_c+1} \varepsilon_C$



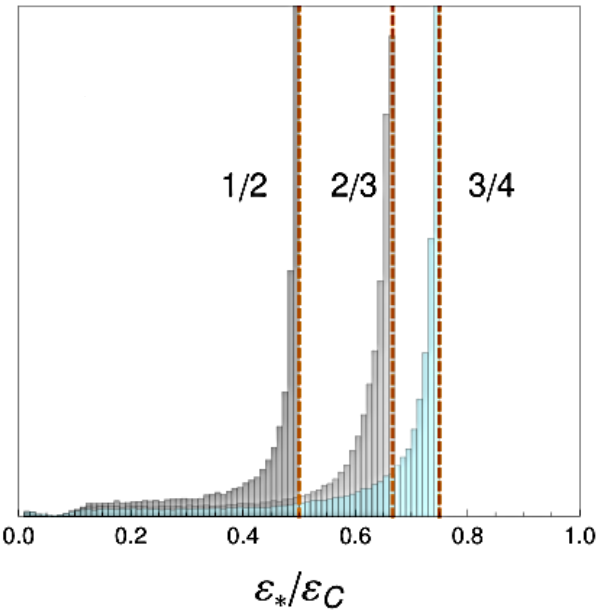
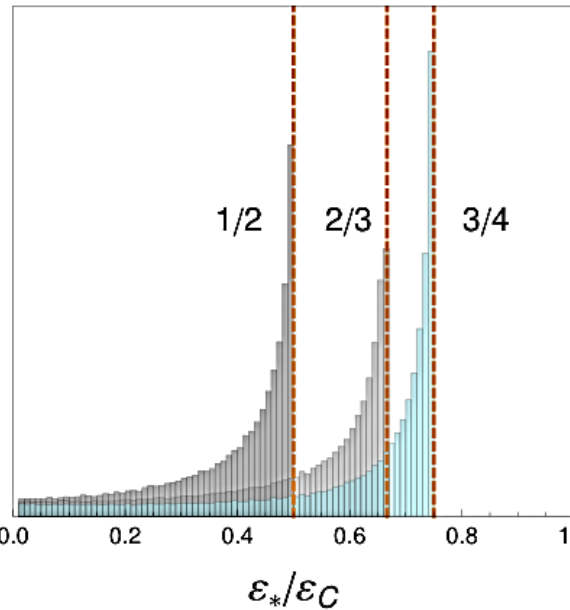
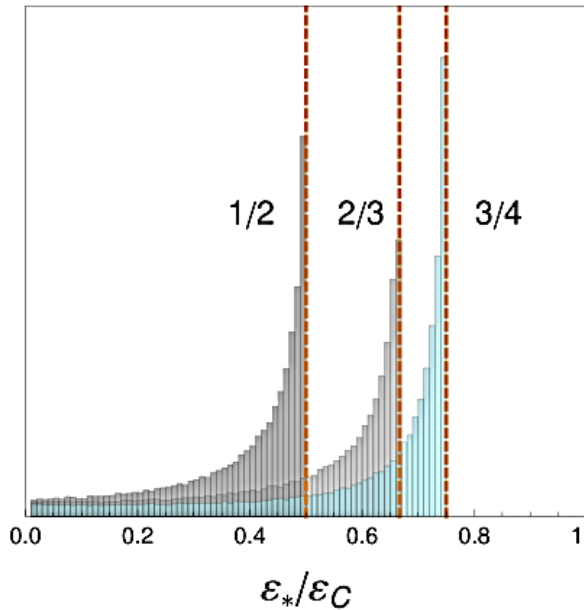
(1)



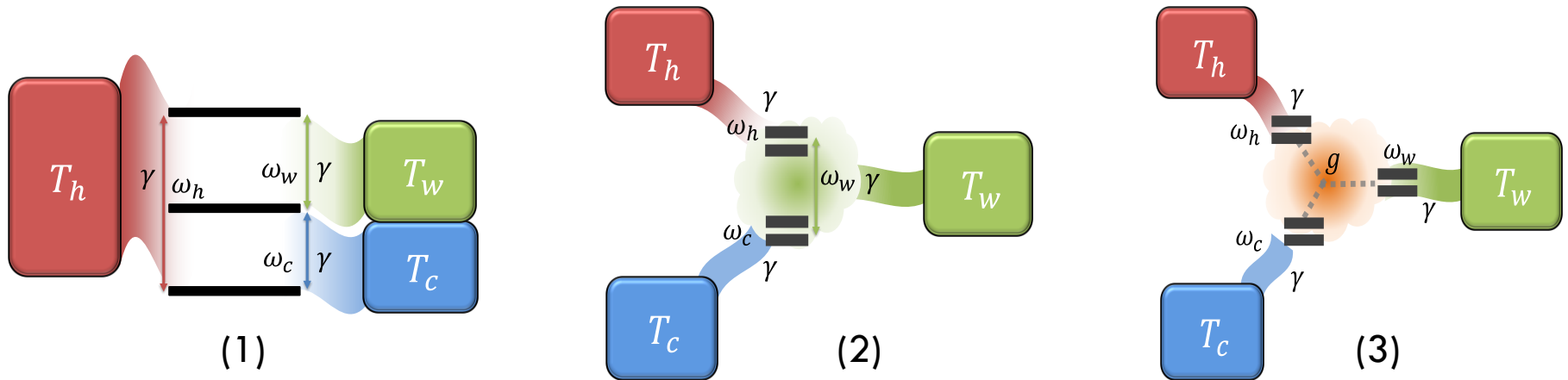
(2)



(3)



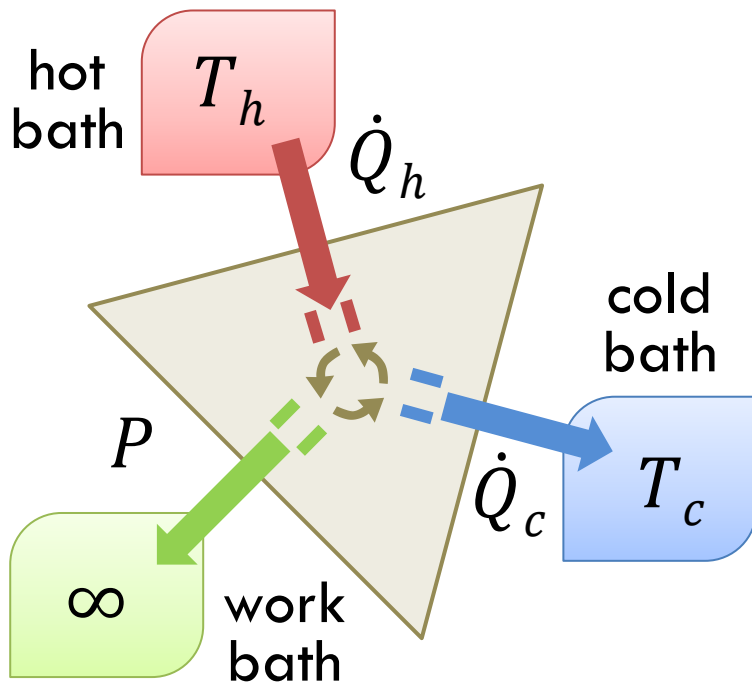
PERFORMANCE BOUND: $\varepsilon_* \leq \frac{d_c}{d_c+1} \varepsilon_C$



- The bound is clearly **model-independent** and holds for all known embodiments of quantum absorption fridges

IS IT UNIVERSAL ?

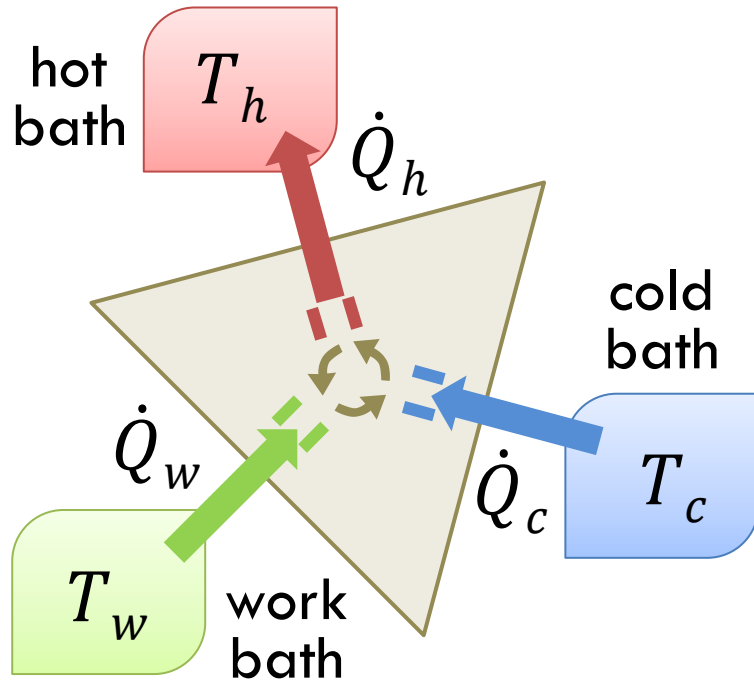
UNIVERSALITY: HEAT ENGINES



- Carnot efficiency: $\eta_C = 1 - T_c/T_h$
- **Endoreversible regime:** the main source of irreversibility is the imperfect thermal contact
- Effective temperature $T'_h \leq T_h$
- Efficiency at max power for endoreversible engines: $\eta_* = 1 - \sqrt{T_c/T_h}$
 - Yvon '55, Novikov '57; Curzon-Ahlborn '75
- When $\eta_C \rightarrow 0$: $\eta_* \approx \frac{1}{2}\eta_C + \frac{1}{8}\eta_C^2 + \dots$
 - Van der Broeck, *Phys. Rev. Lett.* **95** (2005); Esposito et al, *Phys. Rev. Lett.* **102** (2009)

□ Kosloff & Levy, *Annu. Rev. Phys. Chem.* **65** (2014)

UNIVERSALITY: REFRIGERATORS?



- **Endoreversible regime:** the main source of irreversibility is the imperfect thermal contact ($T'_\alpha \neq T_\alpha$)
- In the limit $T_c \ll T_h, \omega_w \ll T_{w,h} \dots$
- COP at maximum power for all endoreversible refrigerators:

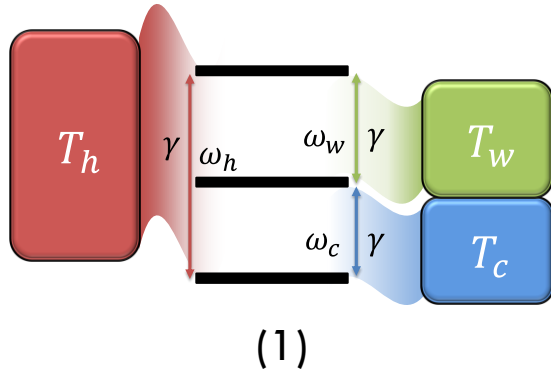
$$\varepsilon_* = \frac{\Lambda \varepsilon_C}{(1 - \Lambda)\varepsilon_C + 1}$$

□ Correa et al, *Phys. Rev. E* **90** (2014)

- But: Λ depends on the bath details!
- **The COP bound cannot be universal**

□ Kosloff & Levy, *Annu. Rev. Phys. Chem.* **65** (2014)

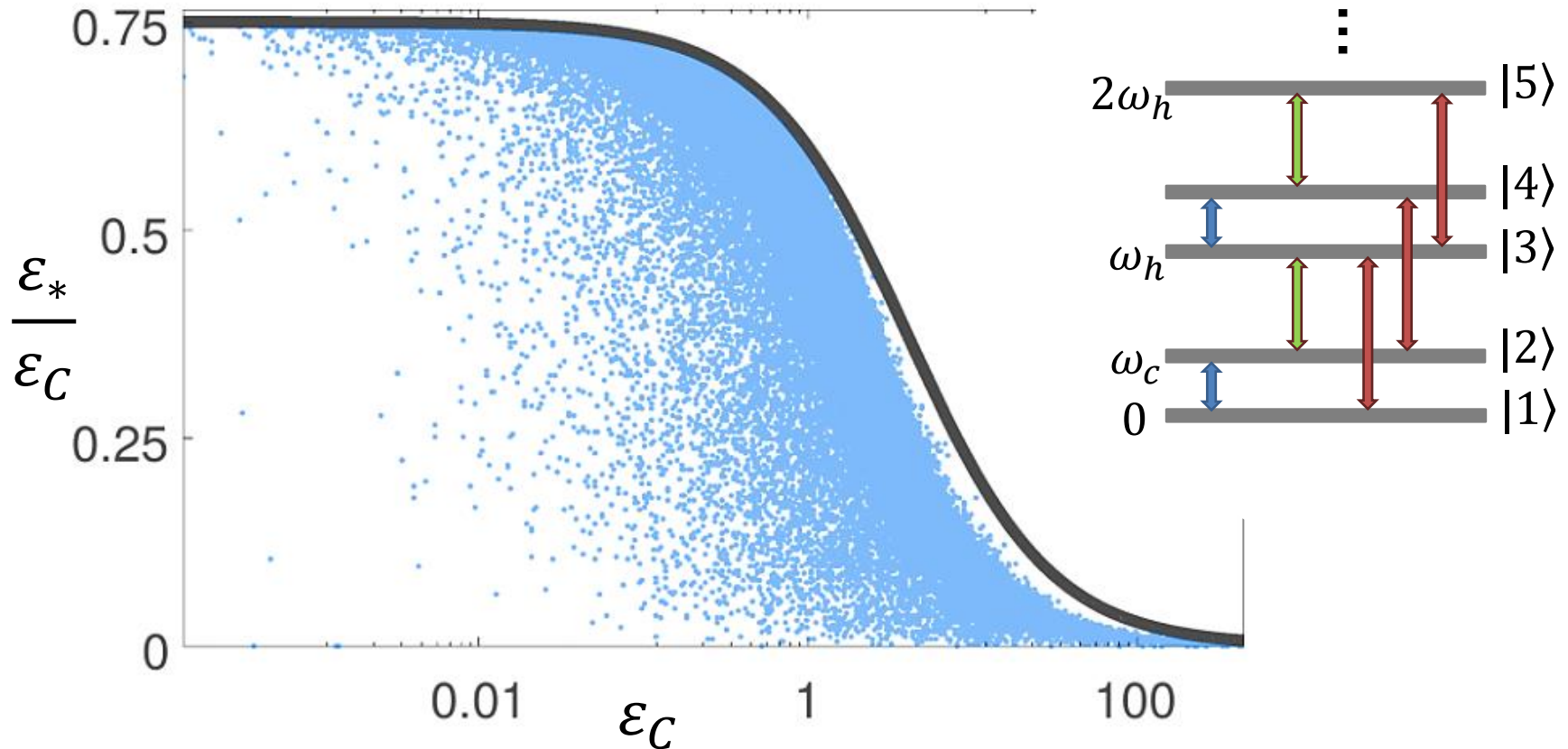
ENDOREVERSIBLE FRIDGE: EXAMPLE



- Model (1): Qutrit; d_α -dimensional baths with flat spectral densities
- We find: $\Lambda = d_c / (d_c + 1)$
- *Sharper performance bound* (although strictly valid only at endoreversibility)

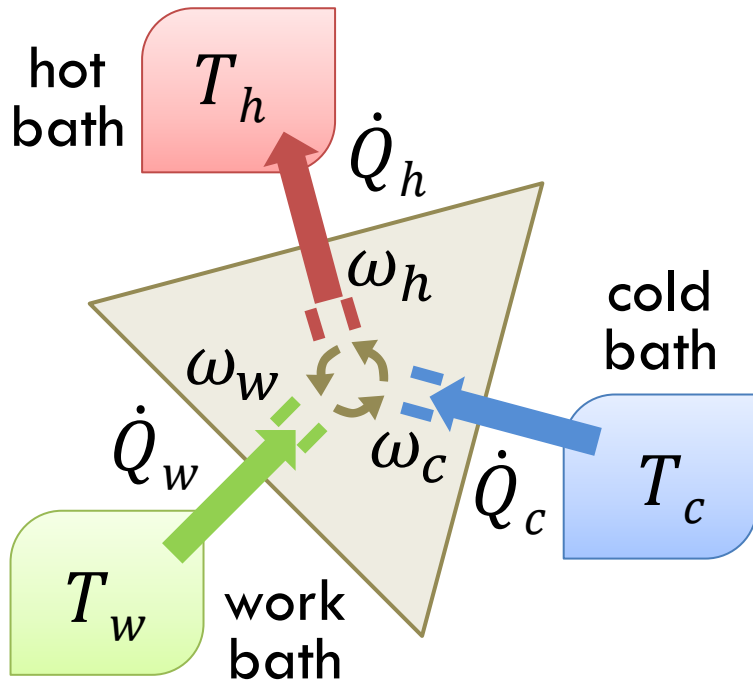
$$\varepsilon_* \leq \frac{d_c}{d_c + 1 + \varepsilon_c} \varepsilon_c$$

TESTING THE BOUND: $\varepsilon_* \leq \frac{d_c}{d_c+1+\varepsilon_C} \varepsilon_C$

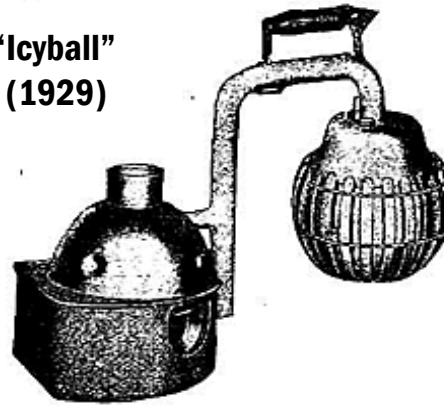


- N -stage quantum absorption refrigerators with three-dimensional unstructured baths ($d_\alpha = 3$)
- Correa et al, *Phys. Rev. E* **90** (2014)

ABSORPTION REFRIGERATORS



“Icyball”
(1929)



EASY TO HANDLE

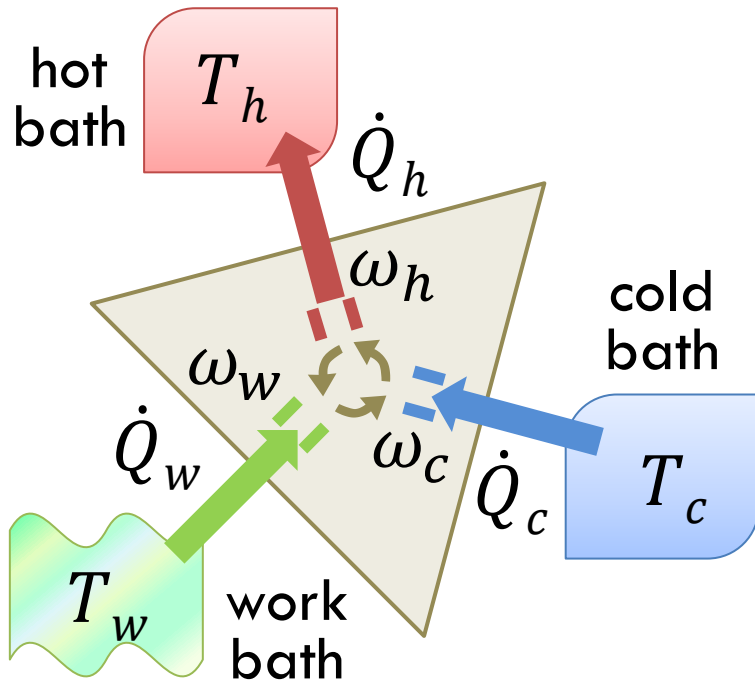
The complete unit which cools after being “charged” by heating, weighs 35 pounds



- *How to understand and possibly improve their optimal performance?*

CAN QUANTUMNESS HELP ?

QUANTUM-ENHANCED FRIDGES



- Work bath: *squeezed thermal* (with squeezing degree r)

- **Squeezing the 2nd law**

$$\frac{\dot{Q}_c}{T_c} + \frac{\dot{Q}_h}{T_h} + \frac{\dot{Q}_w}{\tilde{T}_w(r)} \leq 0, \quad \tilde{T}_w(r) > T_w$$

- Modified master equation:

$$\dot{\rho}(t) = \left(\mathcal{L}_w^{(r)} + \mathcal{L}_h + \mathcal{L}_c \right) \rho(t)$$

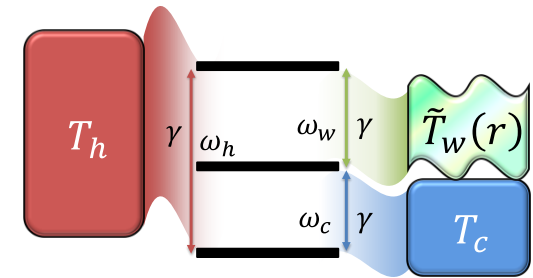
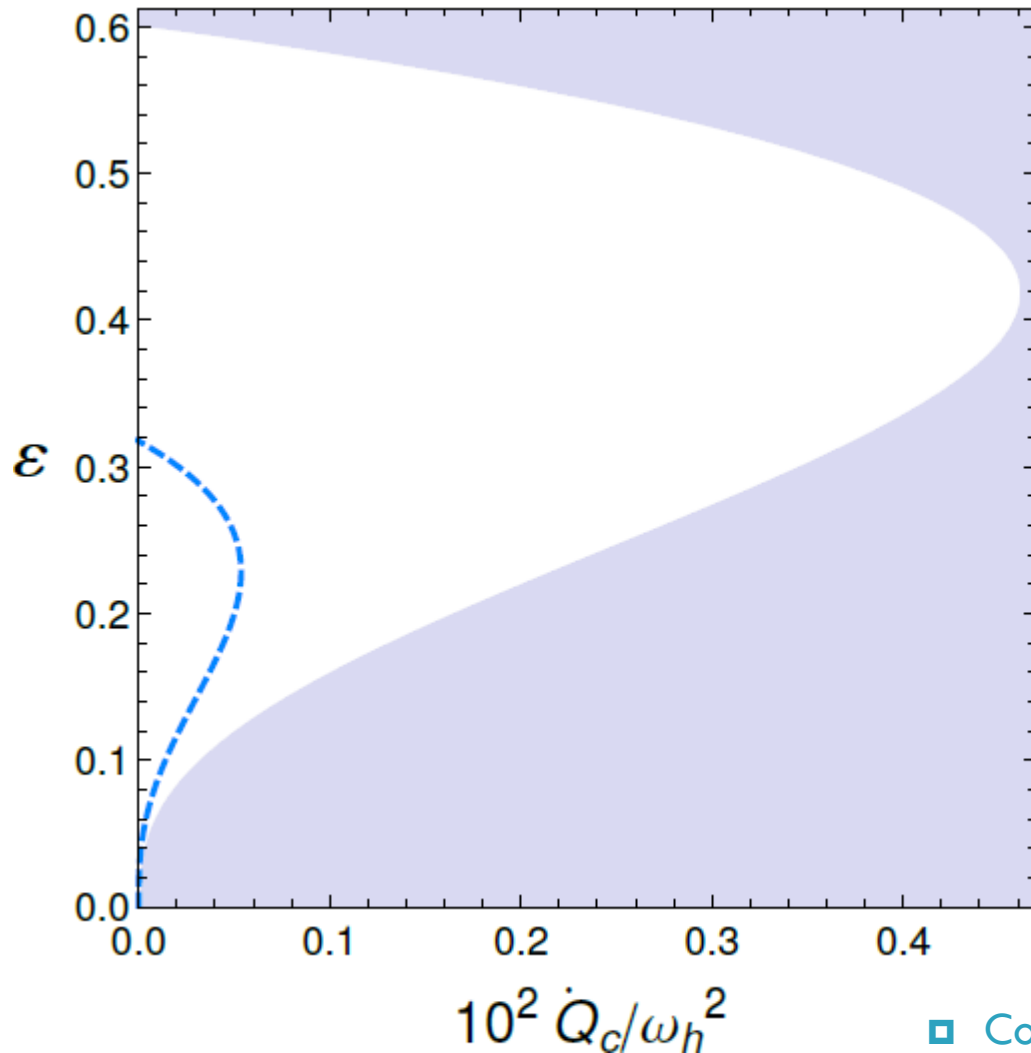
- The Carnot COP increases with r :

$$\varepsilon_C(r) = \frac{1 - \frac{T_h}{\tilde{T}_w(r)}}{\frac{T_h}{T_c} - 1} > \varepsilon_C(0)$$

- Huang, Wang & Yi, *Phys. Rev. E* **86** (2012); Abah & Lutz, *Europhys. Lett.* **106** (2014); Roßnagel et al, *Phys. Rev. Lett.* **112** (2014); Alicki, *arXiv:1401.7865* (2014)

- Correa, Palao, Alonso & *GA Sci Rep* **4** (2014)

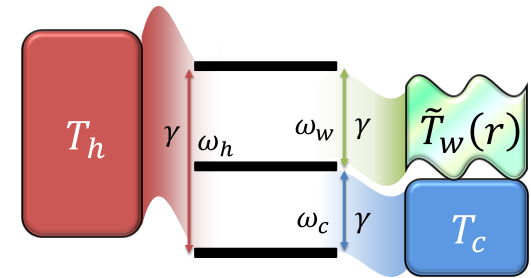
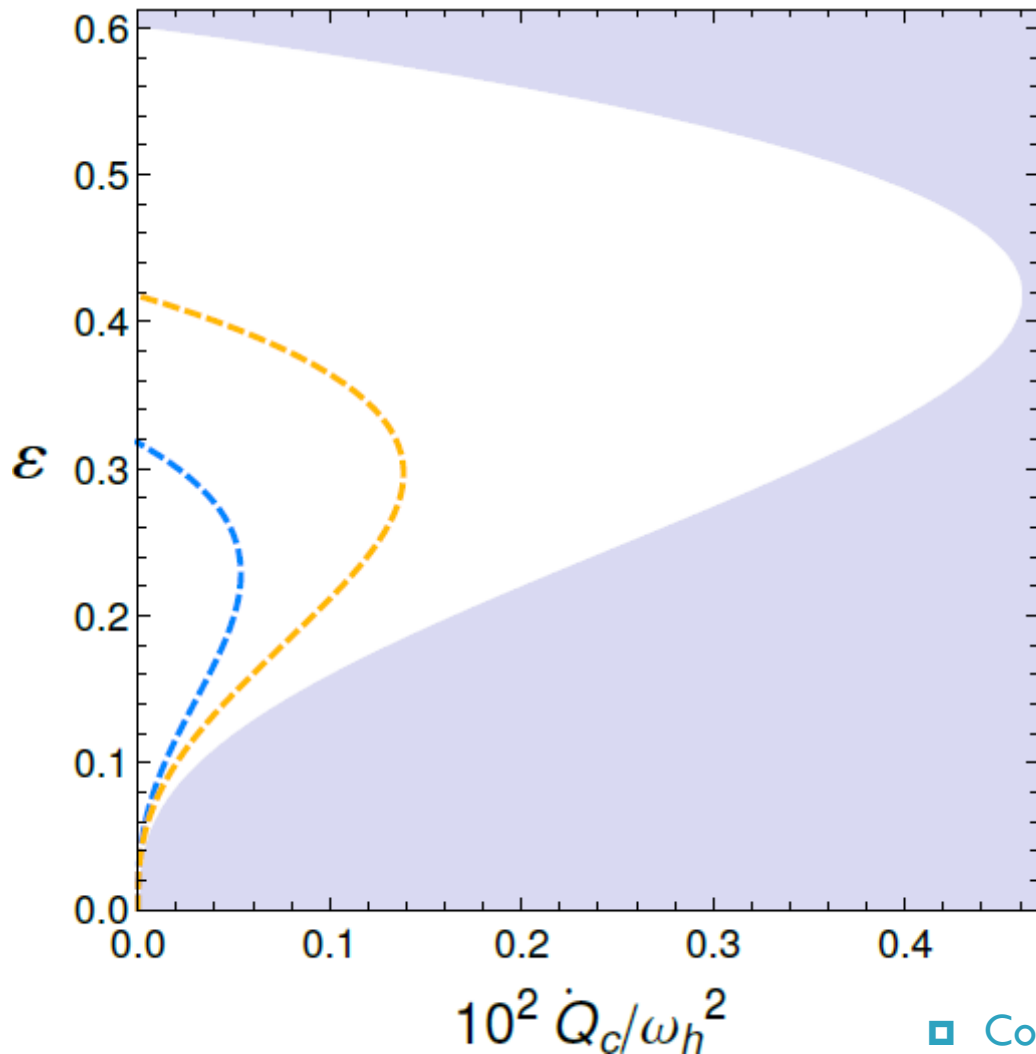
QUANTUM-ENHANCED FRIDGES



--- $r=0.0$

□ Squeezing the 2nd law

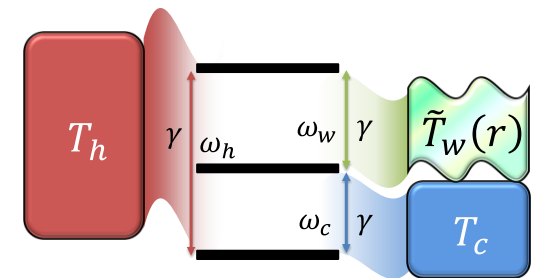
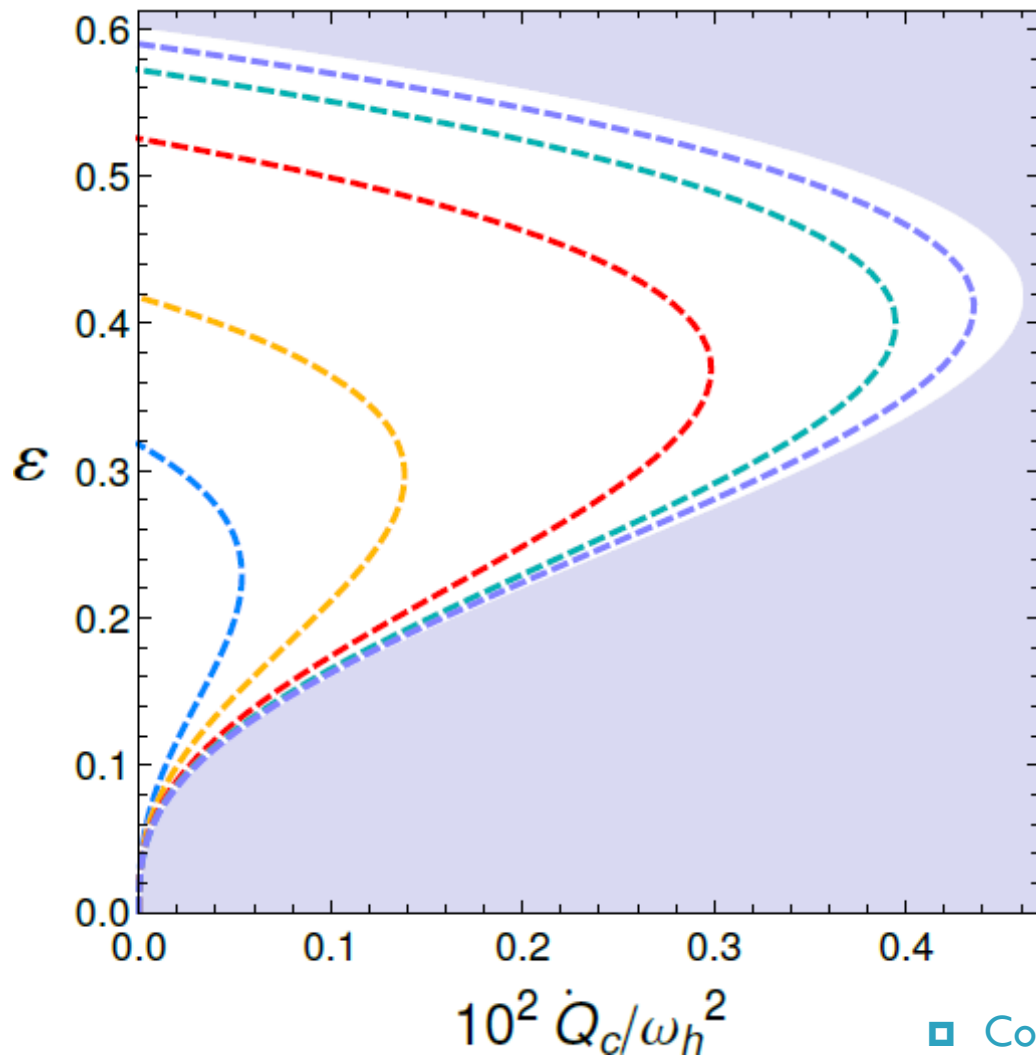
QUANTUM-ENHANCED FRIDGES



--- $r=0.0$
--- $r=0.5$

□ Squeezing the 2nd law

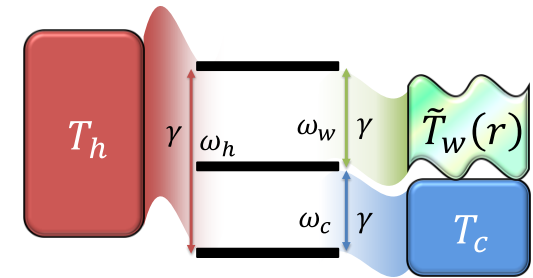
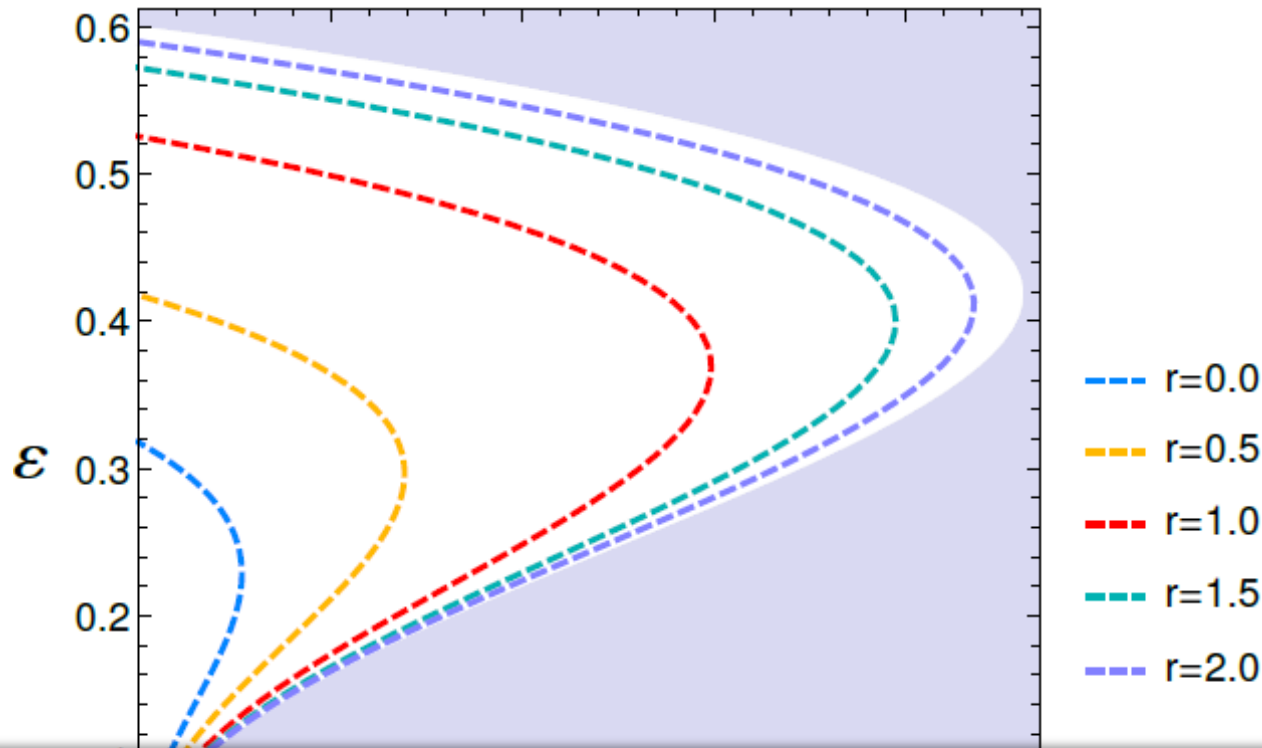
QUANTUM-ENHANCED FRIDGES



- $r=0.0$
- $r=0.5$
- $r=1.0$
- $r=1.5$
- $r=2.0$

□ Squeezing the 2nd law

QUANTUM-ENHANCED FRIDGES



SUMMARY

- Overview of quantum refrigerators and their generic modelling using the framework of *quantum tricycles*
- *Tight bound* $\varepsilon_*/\varepsilon_C \leq d_c/(d_c + 1)$ on the coefficient of performance at maximum cooling power for all known models of quantum absorption refrigerators
- Analogue of Curzon-Ahlborn bound – although not universal – for *endoreversible quantum refrigerators*
- Quantum fluctuations in the work bath (e.g. squeezing) can push the performance *beyond classical limitations*

WHAT IS GENUINELY QUANTUM IN QUANTUM THERMODYNAMICS ?



2nd Quantum Thermodynamics
Conference, Palma, April 2015

L.A. Correa, J.P. Palao, D. Alonso, Gerardo Adesso



- L. A. Correa, J. P. Palao, GA & D. Alonso
Performance bound for quantum absorption refrigerators
Phys. Rev. E **87**, 042131 (2013)
- L. A. Correa, J. P. Palao, D. Alonso & GA
Quantum-enhanced absorption refrigerators
Sci. Rep. **4**, 3949 (2014)
- L. A. Correa, J. P. Palao, GA & D. Alonso
Optimal performance of endoreversible quantum refrigerators
Phys. Rev. E **90**, 062124 (2014)



THANK YOU

